#### Moduli-induced axion problem

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T.Higaki, KN, F.Takahashi, JHEP1307,005 (2013) [1304.7987]

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#### What we have shown :

moduli

axion

• Kahler moduli :  $T_j = \tau_j + ia_j$ 

 Moduli decays into very light axion :  $au_j o 2a_j$  Too much axionic dark radiation in light of PLANCK

# Brief review of moduli problem

## Moduli Problem

[ Coughlan et al. (1983), Ellis et al. (1986), Banks et al. (1993), de Carlos et al. (1993) ]

 Moduli = Light scalar field in compactification of extra dimensions in String theory

• At H~m, moduli begins to oscillate around minimum with typical amplitude  $\sim M_P$ 

## Moduli Problem

#### Moduli abundance

$$\frac{\rho_T}{s} = \frac{1}{8} T_R \left(\frac{z_i}{M_P}\right)^2 \sim 10^5 \text{GeV} \left(\frac{T_R}{10^6 \text{GeV}}\right) \left(\frac{z_i}{M_P}\right)^2$$

Moduli lifetime

 $T_R$ : reheat temperature  $z_i$ : moduli initial amplitude

$$au_T \sim \left(\frac{m_T^3}{M_P^2}\right)^{-1} \sim 10^4 \mathrm{sec} \left(\frac{1\mathrm{TeV}}{m_T}\right)^3$$

Big bang nucleosynthesis constraint

[Kawasaki, Kohri, Moroi (2004)]

$$\frac{\rho_T}{s} \lesssim 10^{-14} \text{GeV}$$

## Moduli Problem

#### Moduli abundance

 $\frac{\rho_T}{s} = \frac{1}{8} T_R \left(\frac{z_i}{M_P}\right)^2 \sim 10^5 \text{GeV} \left(\frac{T_{\text{transform}}}{m_T}\right)^2$ • Moduli lifeting in product temperature initial amplitude  $N_P \sim 10^4 \sec \left(\frac{1\text{TeV}}{m_T}\right)^3$ 

Big bang nucleosynthesis constraint

[Kawasaki, Kohri, Moroi (2004)]

$$\frac{\rho_T}{s} \lesssim 10^{-14} \text{GeV}$$

- Moduli decay before BBN  $(m_T \gg \mathcal{O}(10) \,\mathrm{TeV})$ 
  - Heavy SUSY moduli (e.g., KKLT)  $m_T \gg m_{3/2}$

#### • Heavy non-SUSY moduli

 $m_T \lesssim m_{3/2}$ 

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Moduli-induced gravitino problem
[Endo, Hamaguchi, Takahashi (2006), Nakamura, Yamaguchi (2006)]

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Moduli-induced axion problem

[ Cicoli, Conlon, Quevedo (2012), Higaki, Takahashi (2012), Higaki, KN, Takahashi (2013) ]

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[ Cicoli, Conlon, Quevedo (2012), Higaki, Takahashi (2012), Higaki, KN, Takahashi (2013) ]

# Moduli-induced axion problem

T.Higaki, KN, F.Takahashi, 1304.7987

#### Moduli in typellB string

- Kahler moduli : TShift symmetry :  $T \rightarrow T + i\alpha$ cf) IOd gauge symmetry  $C_4 \rightarrow C_4 + d\Lambda$
- Kahler potential :  $K = K(T + T^{\dagger})$





Suppose that moduli stabilization does not give axion mass

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$$T (\tau \rightarrow 2a) = \frac{1}{64\pi} \frac{K_{TTT}^2}{K_{TT}^3} m_{\tau}^3$$

$$f(\tau \rightarrow A_{\mu}A_{\mu}) = \frac{N_g}{128\pi} \frac{|\partial_T f_{vis}|^2}{(\text{Re}f_{vis})^2} \frac{m_{\tau}^3}{K_{TT}}$$

$$f_{vis}(T) : \text{gauge kinetic function}$$

$$\Gamma(\tau \rightarrow HH) \simeq \frac{1}{8\pi} \frac{g_T^2}{K_{TT}Z_u Z_d} m_{\tau}^3$$

 $K \supset g(T + T^{\dagger})(H_u H_d + \text{h.c.})$ 

Note : decay into their superpartners can also be sizable

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$$\Gamma(\tau \rightarrow 2a) = \frac{1}{64\pi} \frac{K_{TTT}^2}{K_{TT}^3} m_{\tau}^3$$
  
Branching ratio  
into axion (B<sub>a</sub>) is  
generally O(I)  
$$\Gamma(\tau \rightarrow HH) \simeq \frac{1}{8\pi} \frac{g_T^2}{K_{TT}Z_{\tau}Z_{\tau}}$$

$$\Gamma(\tau \to A_{\mu}A_{\mu}) = \frac{N_g}{128\pi} \frac{|\partial_T f_{\rm vis}|^2}{({\rm Re}f_{\rm vis})^2} \frac{m_{\tau}^3}{K_{TT}}$$

: gauge kinetic function  $f_{\rm vis}(T)$ 

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#### Planck constraint on Neff

- Radiation energy density  $\rho_{\rm rad} = \left[1 + \frac{7}{8}N_{\rm eff}\left(\frac{4}{11}\right)^{4/3}\right]\rho_{\gamma}$
- CMB constraint:

$$N_{\rm eff} = 3.36^{+0.68}_{-0.64} @ 95\% {\rm CL}$$

Planck+WMAP pol+ high I [Ade et al. 1303.5076]

• Axion dark radiation abundance:

$$\Delta N_{\text{eff}} = \frac{43}{7} \left( \frac{10.75}{g_*(T_d)} \right)^{1/3} \frac{B_a}{1 - B_a} \quad \longrightarrow$$

 $B_a \lesssim 0.2$ 

Constraint on moduli stabilization model

#### Let us see some examples.

### I. Large Volume Scenario

#### 2. KKLT String axion model

#### Ex I) Large Volume Scenario

[Balasubramanian et al. (2005), Conlon, Quevedo, Suruliz (2005)]

• Swiss-Cheeze CY:  $\mathcal{V} = \mathcal{V}_0 - \mathcal{V}_{hole}$ The simplest :  $\mathcal{V}_0 = (T_b + T_b^{\dagger})^{3/2}$  $\mathcal{V}_{hole} = (T_s + T_s^{\dagger})^{3/2}$ 



• Kahler and Superpotential $K = -2\ln(\mathcal{V} + \xi)$  $W = W_0 + A_s e^{-2\pi T_s}$ 

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Stabilized by alpha' correction. Volume axion  $(\operatorname{Im} T_b = a_b)$ remains massless

$$V = \frac{\sqrt{\tau_s} b_s^2 |A_s|^2 e^{-2b_s \tau_s}}{\mathcal{V}} - \frac{b_s |A_s W_0| \tau_s e^{-b_s \tau_s}}{\mathcal{V}^2} + \frac{\xi |W_0|^2}{g_s^{3/2} \mathcal{V}^3}$$
  
Minimization  

$$V \sim \tau_b^{3/2} \sim e^{2\pi \tau_s} \sim e^{\frac{2\pi \xi^{2/3}}{g_s}} \gg 1$$
  
Large Volume Scenario (LVS)  
• Kahler and Superpotential  

$$K = -2 \ln(\mathcal{V} + \xi)$$
  

$$W = W_0 + A_s e^{-2\pi T_s}$$
  
Stabilized a la KKLT  

$$m_{\tau_s} \sim m_{a_s}$$
  
Stabilized by alpha'  
correction.  
Volume axion (Im  $T_b = a_b$ )  
remains massless

#### Mass scales

- Moduli masses

**Gravitino mass**  $m_{3/2} \sim e^{K/2} W_0 \sim \frac{1}{\mathcal{V}}$  for  $|W_0| \sim O(1)$  $m_{\tau_s} \sim m_{a_s} \sim \frac{1}{\mathcal{V}}$  $m_{ au_b} \sim rac{1}{\mathcal{V}^{3/2}}$  : Lightest modulus  $m_{a_b} = 0$  :Axion

Soft mass (sequestered scenario)  $m_{\rm soft} \sim \frac{1}{\mathcal{V}^2}$ 

Moduli-matter coupling :  $K_{MSSM} =$ 

E.g.,  $\mathcal{V} \sim 10^7 \longrightarrow$ 

$$\frac{|\Phi_i|^2 + (zH_uH_d + \text{h.c.})}{(T_b + T_b^{\dagger})} \right)$$

$$m_{3/2} \sim 10^{11} \,\mathrm{GeV}$$
  
 $m_{\tau_b} \sim 10^7 \,\mathrm{GeV}$ 

 Moduli decay rate [Cicoli, Conlon, Quevedo (2012), Higaki, Takahashi (2012) Angus, Conlon, Haisch, Powell (2013)]

• Two axion: 
$$\tau_b \to 2a$$
  $\Gamma_a = \frac{1}{48\pi} \frac{m_{\tau_b}^3}{M_P^2}$ 

• Two Higgs:  $\tau_b \to 2H$   $\Gamma_H = \frac{z^2}{24\pi} \frac{m_{\tau_b}^3}{M_P^2}$ 

→ Branching ratio into axion:

$$B_a = \frac{1}{1+2z^2}$$

#### Independent of moduli mass

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#### Independent of moduli mass

Constraint : 
$$B_a < 0.2 \longrightarrow \begin{cases} z \gtrsim 2 \\ Many Higgs doublets \end{cases}$$

cf. z=1 if Higgs has shift symmetry [Hebecker et al. (2012)]

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#### Ex 2) QCD axion in KKLT

[J.Conlon (2006), K.Choi, K.S.Jeong (2006)]

String theoretic QCD axion model

 $K = -2 \ln \mathcal{V}$ 

[K.Choi, K.S.Jeong (2006)]

 $\mathcal{V} = (T_0 + T_0^{\dagger})^{3/2} - \kappa_1 (T_1 + T_1^{\dagger})^{3/2} - \kappa_2 (T_2 + T_2^{\dagger})^{3/2}$  $W = Ae^{-\alpha T_0} + Be^{-\beta (T_1 + nT_2)} + W_0$ 



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Stabilized a la KKLT

 $K = -2 \ln \mathcal{V}$ 



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[J.Conlon (2006), K.Choi, K.S.Jeong (2006)]

 $au_0$ 

String theoretic QCD axion model

 $K = -2 \ln \mathcal{V}$ 

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**KKLT** 

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**D7** 

 $\mathcal{A} \equiv nT_1 - T_2$  is stabilized after uplifting, while  $\operatorname{Im} \mathcal{A} \equiv a$  remains massless. • SM brane wraps cycle T2

SM gauge kinetic function : 
$$f_{\rm vis} = \frac{T_2}{4\pi}$$

$$\mathcal{A} \equiv nT_1 - T_2 \equiv s + ia$$

$$\mathcal{L} = \int d^2 \theta f_{\rm vis} \mathcal{W}_a \mathcal{W}^a + \text{h.c.} \sim \frac{s}{\tau_2} G^a_{\mu\nu} G^{\mu\nu a} + \frac{a}{\tau_2} G^a_{\mu\nu} \tilde{G}^{\mu\nu a}$$



• SM brane wraps cycle T2

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QCD axion to  
solve strong CP problem  
SM D7 brane

• SM brane wraps cycle T2

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Lightest moduli QCD axion to solve strong CP problem

SM D7 brane

Moduli (Saxion) decay rate

$$M_s^3 \equiv \frac{1}{\sqrt{2}} \left( \frac{\sqrt{n^3 \kappa_1^2 + \kappa_2^2}}{n^3 \kappa_1^2} \right) \frac{\mathcal{V}}{\phi^{3/2}} m_s^3$$

 $m_s \sim \mathcal{O}(10^3) \,\mathrm{TeV}$ 

• Two axion : 
$$\Gamma_a \simeq \frac{(n^2 \kappa_1^2 - \kappa_2^2)^2}{768 \pi \kappa_2^3} \frac{M_s^3}{M_P^2}$$

Gauge boson: 
$$\Gamma_g \simeq \frac{\kappa_2}{8\pi} \frac{M_s^3}{M_D^2}$$
 : Not loop suppressed



Decay into gluon is sizable in contrast to (usual) saxion decay in SUSY axion model.

[T.Higaki, KN, F.Takahashi, I 304.7987]

# Detecting/constraining axionic dark radiation

• The presence of axionic dark radiation seems to be ubiquitous in string theory  $\Delta N_{\rm eff} \gtrsim \mathcal{O}(0.1)$ 

- Can we probe it?
  - Axion conversion into X-ray photon in galaxy cluster

[J.Conlon, M.C.D.Marsh, 1305.3603]

- Axion-photon conversion in the early Universe under primordial magnetic field [T.Higaki, KN, F.Takahashi, 1306.6518]
- Any other idea?



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#### Summary

 Light axions often appear after moduli stabilization Moduli branch into axion is generically O(1)  $\leftrightarrow$  Planck constraint :  $B_a \leq 0.2$ The branch does not depend on moduli mass The problem exists even for heavy moduli  $(m_T \gg \mathcal{O}(10) \,\mathrm{TeV})$ "Moduli-induced axion problem"

# Cosmolog de los compactification model



# Possible Solutions to moduli problem

- I.Thermal inflation for diluting moduli
   [Lyth, Stewart (1996)]
  - Dilution of baryon asymmetry Domain wall problem

• 2.Adiabatic suppression mechanism [A.Linde (1996)]  $V \sim c^2 H^2 T^2 + m_T^2 (T - T_0)^2$   $c \gg 1$ 

Suppression is not exponential but power in C
 High inflation scale & low reheat temp. is needed.
 [KN, F.Takahashi, T.Yanagida (2011)]

#### Moduli abundance

 $V(T) = cH^2T^2 + m_T^2(T - z_0)^2 \quad (c \sim \mathcal{O}(1))$ 

[ For  $c \gg 1$  , see KN, Takahashi, Yanagida, 1109.2073 ]

•  $H_{\text{inf}} \gg m_T$  :  $\Delta T_i \sim z_0 \longrightarrow \frac{\rho_T}{s} \sim \frac{1}{8} T_R \left(\frac{z_0}{M_P}\right)^2$ •  $H_{\text{inf}} \ll m_T$  :  $\Delta T_i \sim \frac{H_{\text{inf}}^2}{m_T^2} z_0 \longrightarrow \frac{\rho_T}{s} \sim \frac{1}{8} T_R \left(\frac{z_0}{M_P}\right)^2 \left(\frac{H_{\text{inf}}}{m_T}\right)^2$  $\left|\frac{\rho_T}{c} \sim 0\right| \qquad (m_{\rm inf} \gg m_T)$   $(m_{\rm inf} \ll m_T)$ [cf. Kallosh-Linde bound] V(T)T $z_0$ 

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- Moduli T  $K = K(T + T^{\dagger})$
- Canonically normalized moduli & axion  $T \langle T \rangle \equiv \frac{\tau + ia}{\sqrt{2K_{TT}}}$ 
  - Moduli decay into axion pair

$$\mathcal{L} = \frac{K_{TTT}}{\sqrt{2}K_{TT}^{3/2}}\tau(\partial a)^2 \quad ----$$

$$\Gamma(\tau \to 2a) = \frac{1}{64\pi} \frac{K_{TTT}^2}{K_{TT}^3} m_{\tau}^3$$

• Moduli decay into axino pair (if kinematically allowed)

$$\mathcal{L} = \frac{1}{\sqrt{2}} \frac{K_{TTT}}{K_{TT}^{3/2}} \tau \left[ -i\tilde{a}^{\dagger} \bar{\sigma}_{\mu} \partial^{\mu} \tilde{a} + i(\partial_{\mu} \tilde{a}^{\dagger}) \bar{\sigma}^{\mu} \tilde{a} \right]$$

$$\Gamma(\tau \to 2\tilde{a}) = \frac{1}{8\pi} \frac{K_{TTT}^2}{K_{TT}^3} m_{\tilde{a}}^2 m_{\tau}$$

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- Coupling to MSSM sector
  - Gauge kinetic function  $f_{vis}(T)$ 
    - Moduli decay into gauge boson pair

Moduli decay into gaugino pair

$$\mathcal{L} = -\left[\frac{1}{4\sqrt{2K_{TT}}(\text{Re}f_{\text{vis}})}\left\{(\partial_T f_{\text{vis}})(F_T^T + F_{\bar{T}}^T) + (\partial_T^2 f_{\text{vis}})F^T\right\}\tau\lambda^a\lambda^a + \text{h.c.}\right]$$

$$\Gamma(\tau \to \lambda \lambda) \simeq \frac{N_g}{128\pi} \frac{|(\partial_T f_{\rm vis})(F_T^T + F_{\bar{T}}^T)|^2}{({\rm Re} f_{\rm vis})^2} \frac{m_\tau}{K_{TT}}$$

Other terms are suppressed by gaugino mass

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#### Coupling to MSSM sector

 $K \supset Z_u |H_u|^2 + Z_d |H_d|^2 + g(T + T^{\dagger}) (H_u H_d + \text{h.c.})$ 

Moduli decay into Higgs boson pair

$$\mathcal{L} \simeq \frac{g_T}{\sqrt{2K_{TT}Z_uZ_d}} (\partial^2 \tau) (H_u H_d + \text{h.c.})$$

$$\Gamma(\tau \to HH) \simeq \frac{1}{8\pi} \frac{g_T^2}{K_{TT} Z_u Z_d} m_\tau^3$$

Other terms are suppressed by Higgs masses

Moduli decay into higgsino pair

 $\mathcal{L} = -\frac{1}{\sqrt{2K_{TT}Z_uZ_d}} \left[ (2g_T + gK_T)m_{3/2} + g_T(F_T^{T*} + F_{\bar{T}}^{T*}) + 2g_{TT}F^{T*} \right] \tau \tilde{H}_u\tilde{H}_d + h.$ 

 $\longrightarrow \qquad \Gamma(\tau \to \tilde{H}\tilde{H}) = \frac{1}{8\pi} \frac{|c_{\tau\tilde{h}\tilde{h}}|^2}{K_{TT}Z_u Z_d} m_\tau$ 

Other terms are suppressed by higgsino mass

#### Moduli-MSSM matter coupling

[ Conlon, Cremades, Quevedo (2006) ]

#### • SM on singularity

• Kahler potential :  $K_{\text{MSSM}} = \frac{|\Phi_i|^2 + (zH_uH_d + \text{h.c.})}{(T_b + T_b^{\dagger})^a}$  $\longrightarrow y_{\text{phys}} = \frac{e^{K/2}}{\sqrt{Z_i Z_j Z_k}} y = \frac{\tau_b^{-3/2}}{\tau_b^{-3a/2}} y$ 

Physical Yukawa should not depend on V



Soft mass in the no-scale model

$$K = -3\ln\left[T + T^{\dagger} - \frac{1}{3}\{|\Phi|^{2} + z(H_{u}H_{d} + \text{h.c.})\}\right]$$
$$\simeq -3\ln(T + T^{\dagger}) + \frac{|\Phi|^{2} + z(H_{u}H_{d} + \text{h.c.})}{T + T^{\dagger}}$$

 $G^T G_T = 3 \longrightarrow T$  dominantly breaks SUSY

$$m_{\phi}^{2} = e^{G} \left[ \nabla_{\phi} G_{k} \nabla_{\bar{\phi}} G^{k} - R_{\phi \bar{\phi} T \bar{T}} G^{T} G^{\bar{T}} + K_{\phi \bar{\phi}} \right] \qquad \nabla_{\phi} G_{\phi} = \nabla_{\phi} G_{T} = 0$$
$$= m_{3/2}^{2} \left[ K_{\phi \bar{\phi}} - 3K^{T \bar{T}} (K_{\phi \bar{\phi} T \bar{T}} - K^{\phi \bar{\phi}} K_{T \phi \bar{\phi}} K_{\bar{T} \phi \bar{\phi}}) \right] = 0$$

• mu-term in the no-scale model  $\mu = e^{G/2} \nabla_u G_d \qquad \qquad K \supset g(T + T^{\dagger})(H_u H_d + \text{h.c.})$   $= m_{3/2} [g - g_T K^{T\bar{T}} K_T] = 0 \qquad \qquad g = \frac{z}{T + T^{\dagger}}$ 

- SM D7 wrapping on 4-cycle T2
  - Kahler potential :  $K = \frac{(T_2 + T_2^{\dagger})^{\lambda} \{ |Q_i|^2 + z(H_u H_d + \text{h.c.}) \}}{\mathcal{V}^{2/3}}$  $\longrightarrow y_{\text{phys}} = \frac{e^{K/2}}{\sqrt{Z_i Z_j Z_k}} y \sim \tau_2^{-3\lambda/2} y$
  - Yukawa dependence on T2

#### Moduli-MSSM Gauge coupling

• DBI action

gauge field on Dp brane

$$S_{\text{DBI}} = -\mu_p \int_{p+1} d^{p+1} x e^{-\phi} \sqrt{-\det(G + B - 2\pi\alpha' F)}$$
Dp brane worldvolume Dp brane tension
$$\supset \frac{\alpha'^{-(p-3)/2}}{4g_s(2\pi)^{p-2}} \int d^{p+1} x \sqrt{-g} \operatorname{tr} F_{\mu\nu} F^{\mu\nu} \qquad \mu_p = \frac{\alpha'^{-(p+1)/2}}{(2\pi)^p}$$
Ad gauge coupling:
$$\boxed{\frac{1}{g_{\text{YM}}^2} = \frac{\alpha'^{(3-p)/2}}{g_s(2\pi)^{p-2}} V_{p-3}} \text{Kahler moduli}$$
Chern-Simons action :Dp-brane  $\leftrightarrow$  R-R fields
$$S_{\text{CS}} = \mu_p \int_{p+1} C_q \wedge e^{2\pi\alpha' F - B_2}$$

$$\supset \mu_p \int_{p+1} C_{p+1} + 2\pi\alpha' \int_{p+1} C_{p-1} \wedge \operatorname{tr} F + 2\pi^2 \alpha'^2 \int_{p+1} C_{p-3} \wedge \operatorname{tr} F^2$$

( )