

Higgs characterisation

- beyond leading order

Kentarou Mawatari

(Vrije Universiteit Brussel and International Solvay Institutes)

[arXiv: 1306.6464]

The FeynRules and MadGraph5 framework

[FeynRules model](#)

P. de Aquino, K. Mawatari (Vrije U. Brussel)

[MadWeight](#)

P. Artoisenet (Nikhef)

[aMC@NLO](#)

F. Demartin, F. Maltoni, M. Zaro (UC Louvain)

R. Frederix, S. Frixione (CERN)

P. Torrielli (Zurich)

[spin2 in aMC@NLO](#)

M.K. Mandal (Harish-Chandra)

P. Mathews, S. Seth (Saha Inst.)

V. Ravindran (CIT)

about 50 years ago...



BROKEN SYMMETRY AND THE MASS OF GAUGE VECTOR MESONS*

F. Englert and R. Brout

Faculté des Sciences, Université Libre de Bruxelles, Bruxelles, Belgium

(Received 26 June 1964)

BROKEN SYMMETRIES, MASSLESS PARTICLES AND GAUGE FIELDS

P. W. HIGGS

Tait Institute of Mathematical Physics, University of Edinburgh, Scotland

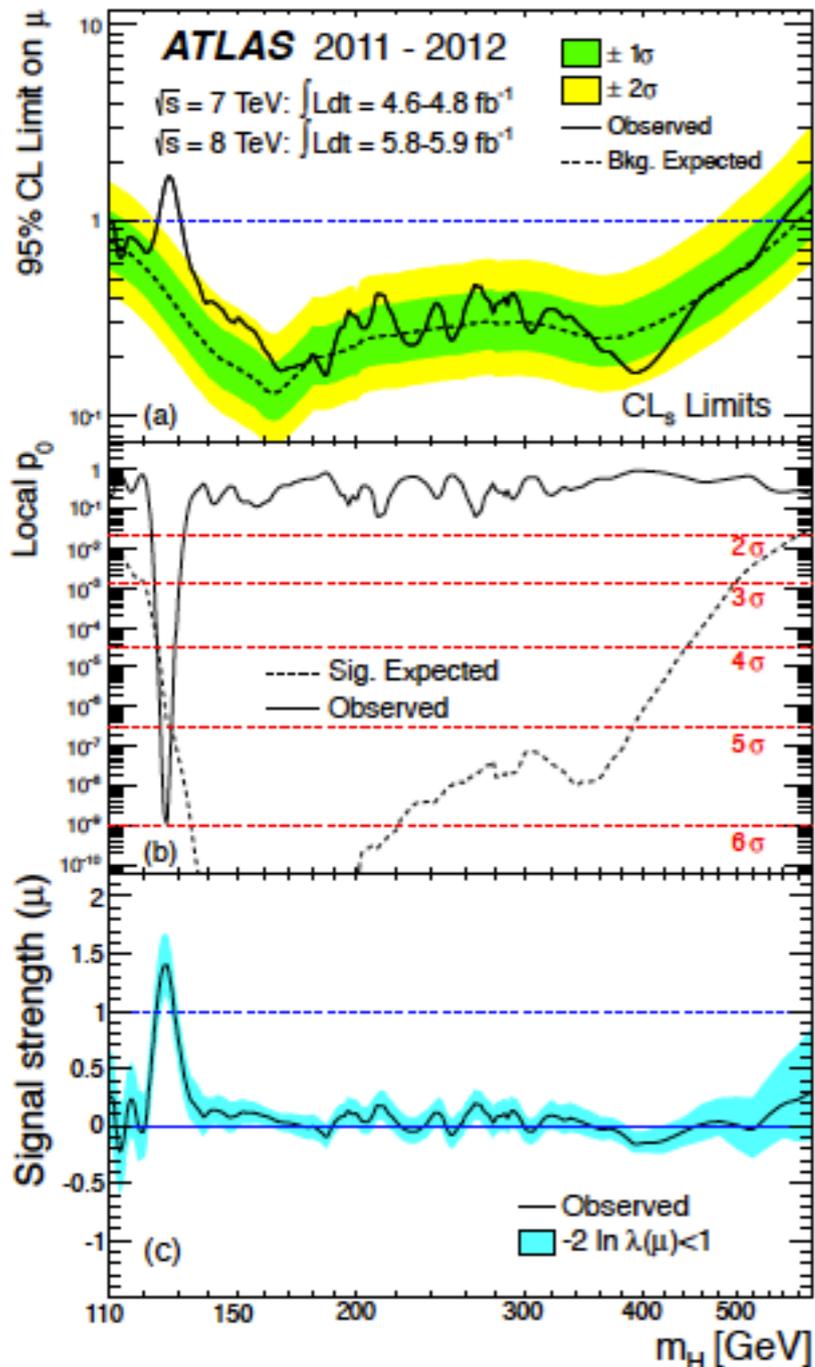
Received 27 July 1964

July 4th, 2012

Observation of a New Particle in the Search for the Standard Model Higgs Boson with the ATLAS Detector at the LHC

[arXiv: 1207.7214]

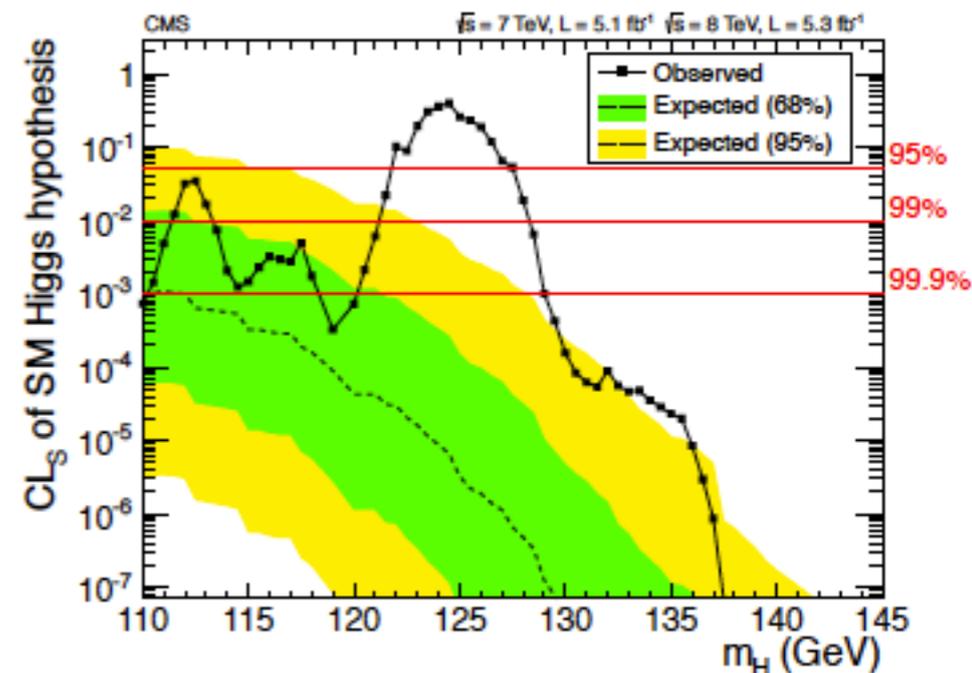
The ATLAS Collaboration



Observation of a new boson at a mass of 125 GeV with the CMS experiment at the LHC

[arXiv: 1207.7235]

The CMS Collaboration



July 4th, 2013

arXiv:1307.1432v1 [hep-ex] 4 Jul 2013

Evidence for the spin-0 nature of the Higgs boson using ATLAS data

The ATLAS Collaboration

Abstract

Studies of the spin and parity quantum numbers of the Higgs boson are presented, based on proton–proton collision data collected by the ATLAS experiment at the LHC. The Standard Model spin–parity $J^P = 0^+$ hypothesis is compared with alternative hypotheses using the Higgs boson decays $H \rightarrow \gamma\gamma$, $H \rightarrow ZZ^* \rightarrow 4\ell$ and $H \rightarrow WW^* \rightarrow \ell\nu\ell\nu$, as well as the combination of these channels. The analysed dataset corresponds to an integrated luminosity of 20.7 fb^{-1} collected at a centre–of–mass energy of $\sqrt{s} = 8 \text{ TeV}$. For the $H \rightarrow ZZ^* \rightarrow 4\ell$ decay mode the dataset corresponding to an integrated luminosity of 4.6 fb^{-1} collected at $\sqrt{s} = 7 \text{ TeV}$ is added. The data are compatible with the Standard Model $J^P = 0^+$ quantum numbers for the Higgs boson, whereas all alternative hypotheses studied in this letter, namely some specific $J^P = 0^-, 1^+, 1^-, 2^+$ models, are excluded at confidence levels above 97.8%. This exclusion holds independently of the assumptions on the coupling strengths to the Standard Model particles and in the case of the $J^P = 2^+$ model, of the relative fractions of gluon–fusion and quark–antiquark production of the spin-2 particle. The data thus provide evidence for the spin-0 nature of the Higgs boson, with positive parity being strongly preferred.



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➔ determination of **the Higgs Lagrangian**

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- **the structure of the operators**, linked to the spin/
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A framework for Higgs characterisation

[arXiv: 1306.6464]

P. Artoisenet,^a P. de Aquino,^b F. Demartin,^c R. Frederix,^d S. Frixione,^{d,e} F. Maltoni,^c
M. K. Mandal,^f P. Mathews,^g K. Mawatari,^b V. Ravindran,^h S. Seth,^g P. Torrielli,ⁱ
M. Zaro^c

ABSTRACT: We introduce a complete framework, based on an effective field theory approach, that allows one to perform characterisation studies of the boson recently discovered at the LHC, for all the relevant channels and in a consistent, systematic and accurate way.

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- beyond-leading-order effects in QCD
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 - higher order QCD effects on spin observables
- Summary

FeynRules in a nutshell

Christensen, Duhr, Fuks, <http://feynrules.irmp.ucl.ac.be>

- a Mathematica package that allows to derive Feynman rules from a Lagrangian.
- allows to export the Feynman rules to various matrix element generators, e.g. MadGraph.
- The only requirements on the Lagrangian are:
 - ✓ All indices need to be contracted.
 - ✓ Locality.
 - ✓ Supported field types: spin-0, 1/2, 1, 3/2, and 2.

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[arxiv:1308.1668] see B.Oexl talk.

Higgs Characterisation model

- We implemented an effective Lagrangian featuring bosons $X(J^P=0^+,0^-,1^+,1^-,2^+)$ in FeynRules.
 - ▶ **Effective field theory** approach, valid up to a cutoff scale Λ
 - ▶ Only **one new bosonic state** $X(J^P)$ at the EW scale (No other state below the cutoff Λ)
 - ▶ Any new physics is described by the lowest dimensional operators.

The parametrization is based on the recent work [Englert, Goncalves-Netto, KM, Plehn (2013)].

Effective Lagrangian -- spin0

- allows one to recover the SM case easily.
- includes all possible interactions that are generated by gauge-invariant D6 operators above the EW scale
- includes 0^- state couplings typical of SUSY or of generic 2HDM
- allows CP-mixing between 0^+ and 0^- states

parameter	reference value	description
Λ [GeV]	10^3	cutoff scale
$c_\alpha (\equiv \cos \alpha)$	1	mixing between 0^+ and 0^-
κ_i	0, 1	dimensionless coupling parameter

$g_{Xyy'} \times v$	ff	ZZ/WW	$\gamma\gamma$	$Z\gamma$	gg
H	m_f	$2m_{Z/W}^2$	$47\alpha_{EM}/18\pi$	$C(94 \cos^2 \theta_W - 13)/9\pi$	$-\alpha_s/3\pi$
A	m_f	0	$-4\alpha_{EM}/3\pi$	$-2C(8 \cos^2 \theta_W - 5)/3\pi$	$-\alpha_s/2\pi$

Effective Lagrangian -- spin0

$$\mathcal{L}_0^f = - \sum_{f=t,b,\tau} \bar{\psi}_f (c_\alpha \kappa_{Hff} g_{Hff} + i s_\alpha \kappa_{Aff} g_{Aff} \gamma_5) \psi_f X_0$$

$$\mathcal{L}_0^V = \left\{ c_\alpha \kappa_{SM} \left[\frac{1}{2} g_{HZZ} Z_\mu Z^\mu + g_{HWW} W_\mu^+ W^{-\mu} \right] \right. \\ - \frac{1}{4} \left[c_\alpha \kappa_{H\gamma\gamma} g_{H\gamma\gamma} A_{\mu\nu} A^{\mu\nu} + s_\alpha \kappa_{A\gamma\gamma} g_{A\gamma\gamma} A_{\mu\nu} \tilde{A}^{\mu\nu} \right] \\ - \frac{1}{2} \left[c_\alpha \kappa_{HZ\gamma} g_{HZ\gamma} Z_{\mu\nu} A^{\mu\nu} + s_\alpha \kappa_{AZ\gamma} g_{AZ\gamma} Z_{\mu\nu} \tilde{A}^{\mu\nu} \right] \\ - \frac{1}{4} \left[c_\alpha \kappa_{Hgg} g_{Hgg} G_{\mu\nu}^a G^{a,\mu\nu} + s_\alpha \kappa_{Agg} g_{Agg} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \right] \\ - \frac{1}{4} \frac{1}{\Lambda} \left[c_\alpha \kappa_{HZZ} Z_{\mu\nu} Z^{\mu\nu} + s_\alpha \kappa_{AZZ} Z_{\mu\nu} \tilde{Z}^{\mu\nu} \right] \\ - \frac{1}{2} \frac{1}{\Lambda} \left[c_\alpha \kappa_{HWW} W_{\mu\nu}^+ W^{-\mu\nu} + s_\alpha \kappa_{AWW} W_{\mu\nu}^+ \tilde{W}^{-\mu\nu} \right] \\ \left. - \frac{1}{\Lambda} c_\alpha \left[\kappa_{H\partial\gamma} Z_\nu \partial_\mu A^{\mu\nu} + \kappa_{H\partial Z} Z_\nu \partial_\mu Z^{\mu\nu} + \kappa_{H\partial W} (W_\nu^+ \partial_\mu W^{-\mu\nu} + h.c.) \right] \right\} X_0$$

$$V_{\mu\nu} = \partial_\mu V_\nu - \partial_\nu V_\mu \quad (V = A, Z, W^\pm), \quad \tilde{V}_{\mu\nu} = \frac{1}{2} \epsilon_{\mu\nu\rho\sigma} V^{\rho\sigma} \\ G_{\mu\nu}^a = \partial_\mu G_\nu^a - \partial_\nu G_\mu^a + g_s f^{abc} G_\mu^b G_\nu^c,$$

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## INFORMATION FOR FRBLOCK
#####
Block FRBlock
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 2 1.000000e+00 # ca
 3 1.000000e+00 # kSM
 4 1.000000e+00 # kHtt
 5 1.000000e+00 # kAtt
 6 1.000000e+00 # kHbb
 7 1.000000e+00 # kAbb
 8 1.000000e+00 # kHll
 9 1.000000e+00 # kAll
10 1.000000e+00 # kHaa
11 1.000000e+00 # kAaa
12 1.000000e+00 # kHza
13 1.000000e+00 # kAza
14 1.000000e+00 # kHgg
15 1.000000e+00 # kAgg
16 0.000000e+00 # kHzz
17 0.000000e+00 # kAzz
18 0.000000e+00 # kHww
19 0.000000e+00 # kAww
20 0.000000e+00 # kHda
21 0.000000e+00 # kHdz
22 0.000000e+00 # kHdw
```

Effective Lagrangian -- spin0

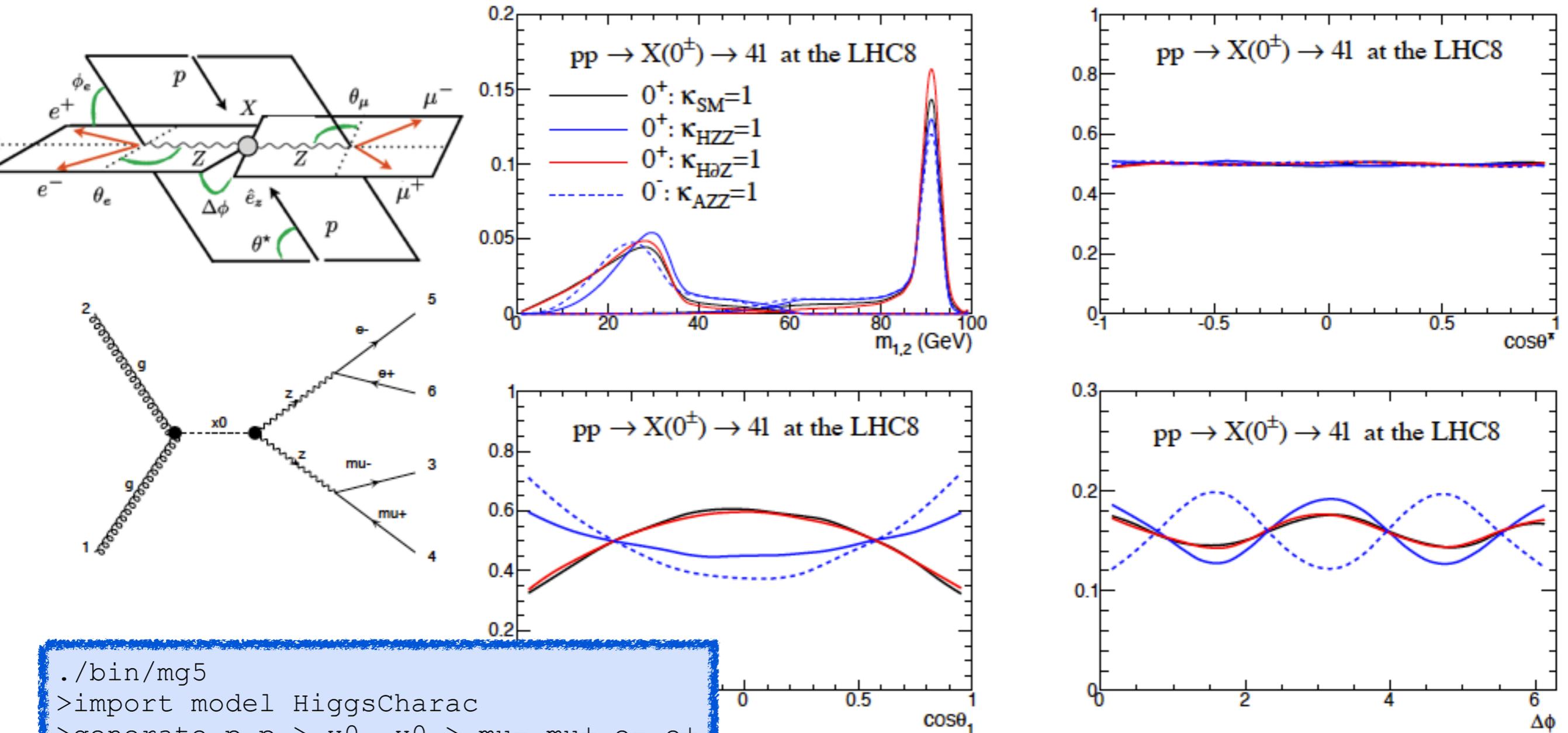
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```

Mass and angular distributions -- spin0



```

./bin/mg5
>import model HiggsCharac
>generate p p > x0, x0 > mu- mu+ e- e+
>output
>launch
    
```

Effective Lagrangian -- spin 1

- The most general interactions at the lowest canonical dimension:

$$\mathcal{L}_1^f = \sum_{f=q,\ell} \bar{\psi}_f \gamma_\mu (\kappa_{f_a} a_f - \kappa_{f_b} b_f \gamma_5) \psi_f X_1^\mu$$

$$\begin{aligned} \mathcal{L}_1^W = & i\kappa_{W_1} g_{WWZ} (W_{\mu\nu}^+ W^{-\mu} - W_{\mu\nu}^- W^{+\mu}) X_1^\nu + i\kappa_{W_2} g_{WWZ} W_\mu^+ W_\nu^- X_1^{\mu\nu} \\ & - \kappa_{W_3} W_\mu^+ W_\nu^- (\partial^\mu X_1^\nu + \partial^\nu X_1^\mu) \\ & + i\kappa_{W_4} W_\mu^+ W_\nu^- \tilde{X}_1^{\mu\nu} - \kappa_{W_5} \epsilon_{\mu\nu\rho\sigma} [W^{+\mu} (\partial^\rho W^{-\nu}) - (\partial^\rho W^{+\mu}) W^{-\nu}] X_1^\sigma \end{aligned}$$

$$\mathcal{L}_1^Z = -\kappa_{Z_1} Z_{\mu\nu} Z^\mu X_1^\nu - \kappa_{Z_3} X_1^\mu (\partial^\nu Z_\mu) Z_\nu - \kappa_{Z_5} \epsilon_{\mu\nu\rho\sigma} X_1^\mu Z^\nu (\partial^\rho Z^\sigma)$$

- Parity conservation implies that

▶ for X_{1-} $\kappa_{f_b} = \kappa_{V_4} = \kappa_{V_5} = 0$

▶ for X_{1+} $\kappa_{f_a} = \kappa_{V_1} = \kappa_{V_2} = \kappa_{V_3} = 0$

Effective Lagrangian -- spin2

- via the energy-momentum tensor of the SM fields, starting from D5:

$$\mathcal{L}_2^f = -\frac{1}{\Lambda} \sum_{f=q,\ell} \kappa_f T_{\mu\nu}^f X_2^{\mu\nu}$$

$$\mathcal{L}_2^V = -\frac{1}{\Lambda} \sum_{V=Z,W,\gamma,g} \kappa_V T_{\mu\nu}^V X_2^{\mu\nu}$$

► The E-M tensor for QED:

$$T_{\mu\nu}^f = -g_{\mu\nu} \left[\bar{\psi}_f (i\gamma^\rho D_\rho - m_f) \psi_f - \frac{1}{2} \partial^\rho (\bar{\psi}_f i\gamma_\rho \psi_f) \right]$$

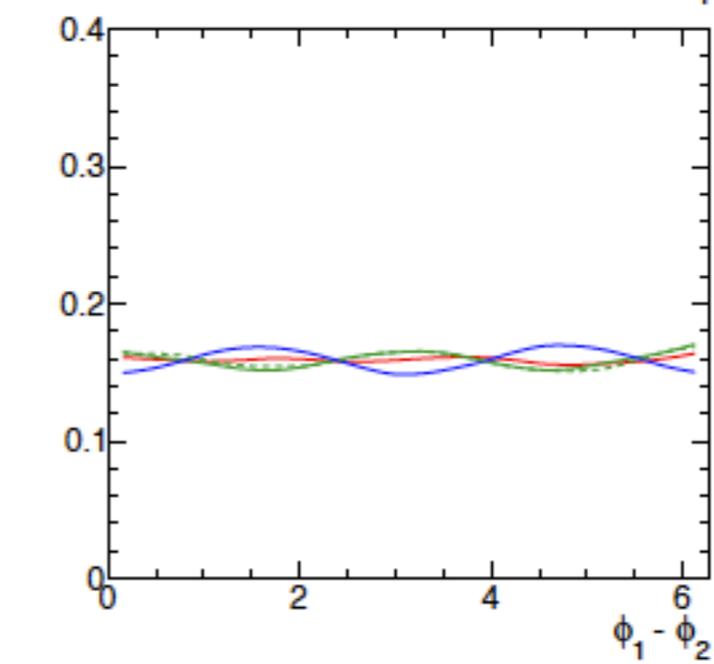
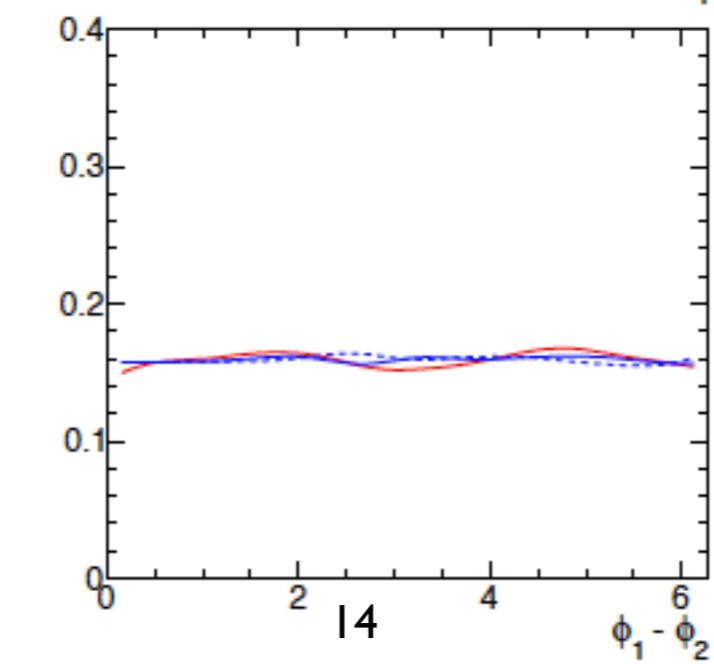
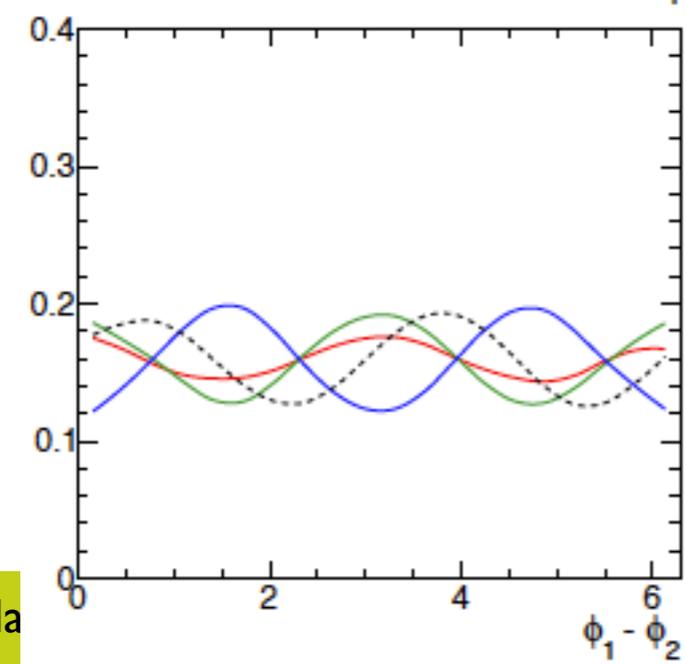
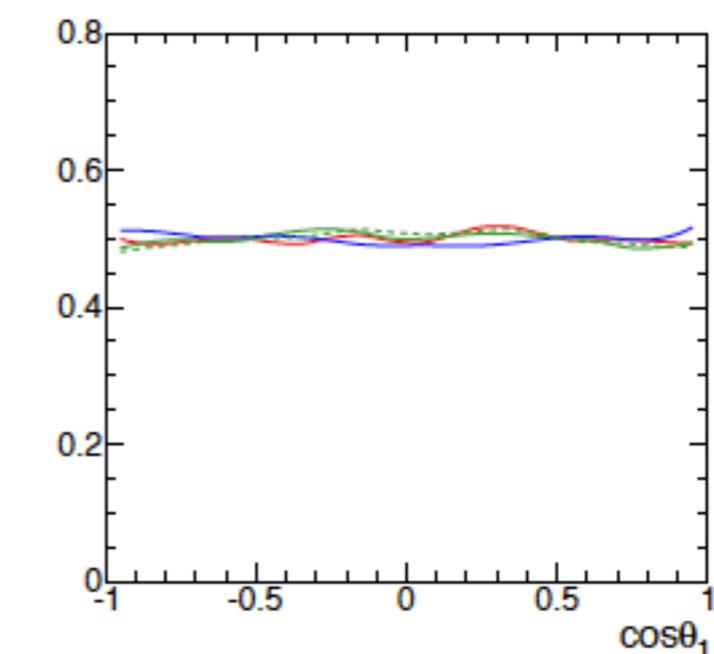
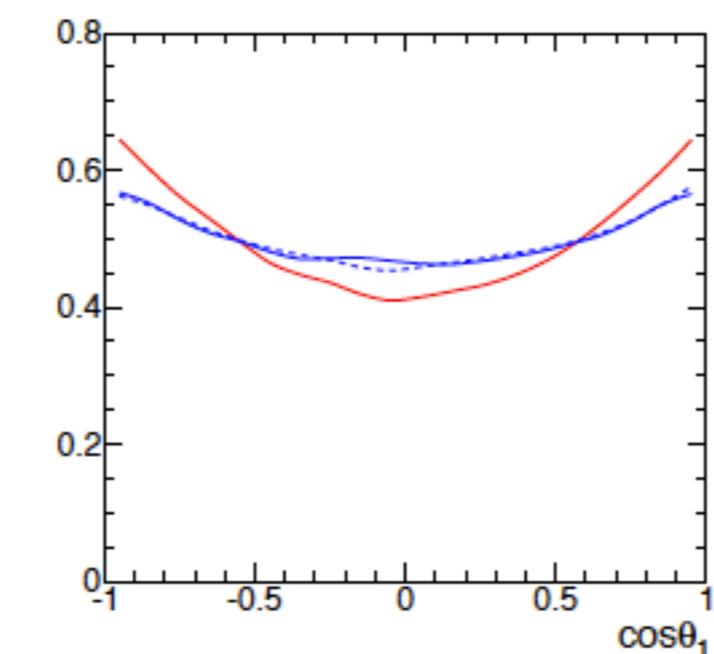
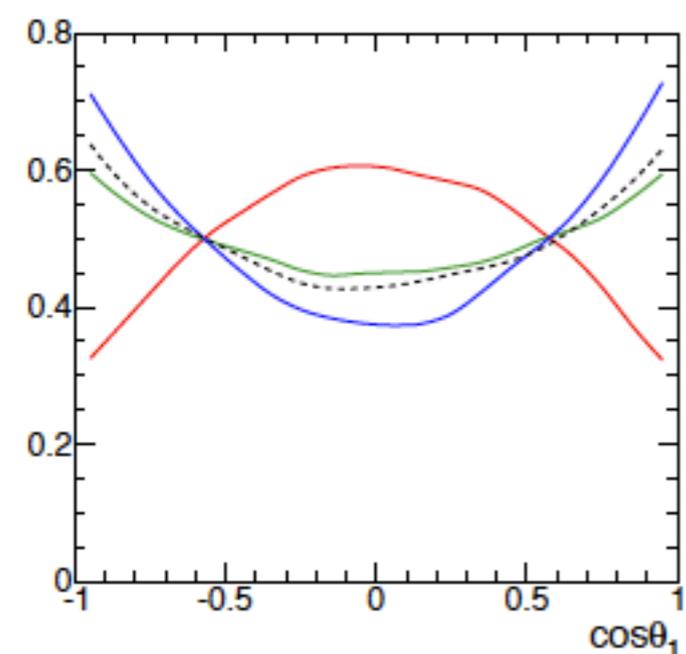
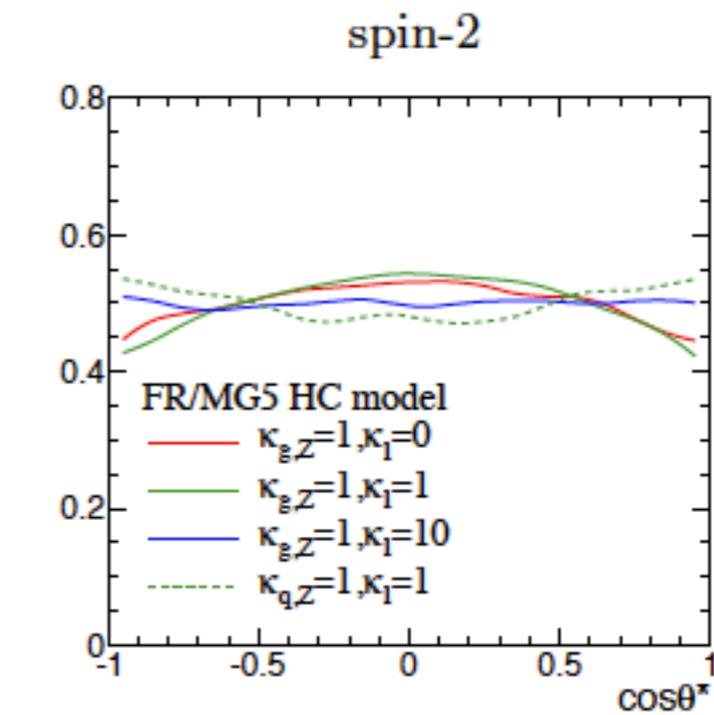
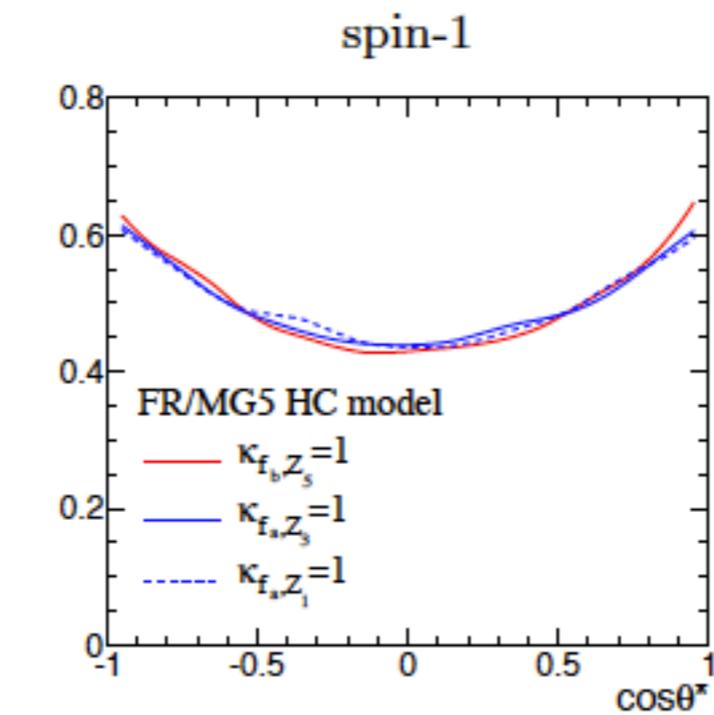
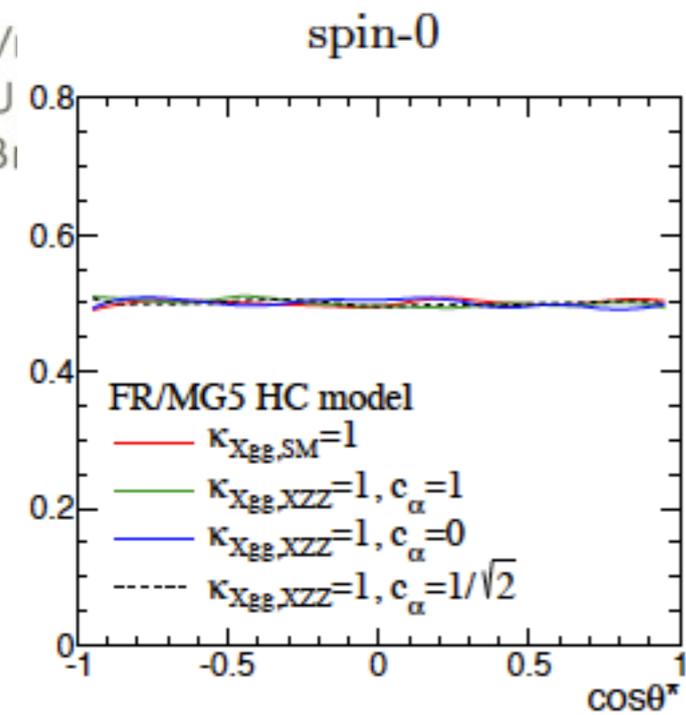
$$+ \left[\frac{1}{2} \bar{\psi}_f i\gamma_\mu D_\nu \psi_f - \frac{1}{4} \partial_\mu (\bar{\psi}_f i\gamma_\nu \psi_f) + (\mu \leftrightarrow \nu) \right],$$

$$T_{\mu\nu}^\gamma = -g_{\mu\nu} \left[-\frac{1}{4} A^{\rho\sigma} A_{\rho\sigma} + \partial^\rho \partial^\sigma A_\sigma A_\rho + \frac{1}{2} (\partial^\rho A_\rho)^2 \right]$$

$$- A_\mu{}^\rho A_{\nu\rho} + \partial_\mu \partial^\rho A_\rho A_\nu + \partial_\nu \partial^\rho A_\rho A_\mu,$$



V
U
B



All the relevant channels can be simulated
in a consistent, systematic and accurate way.
e.g. VBF ($pp \rightarrow jjX$)

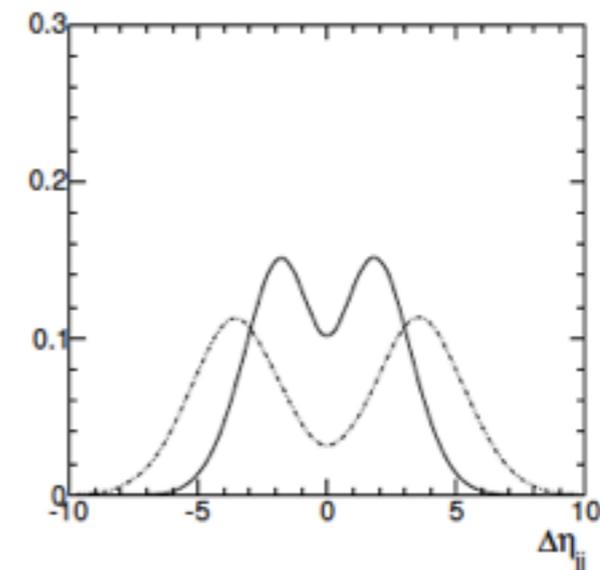
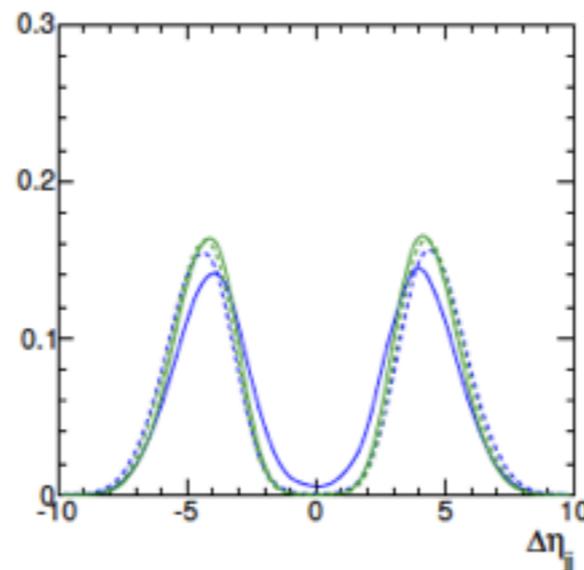
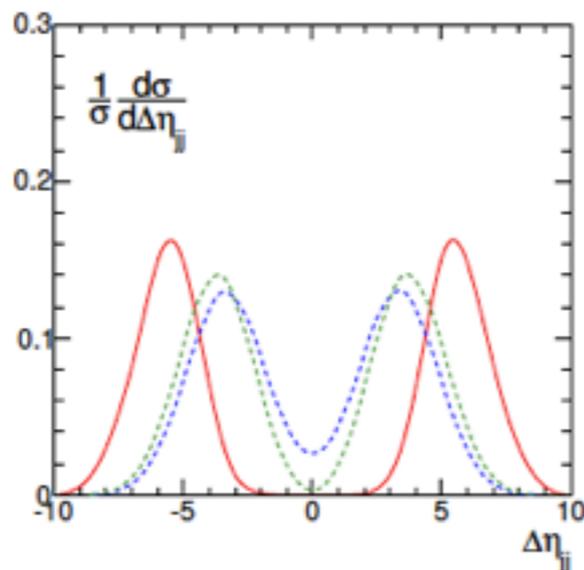
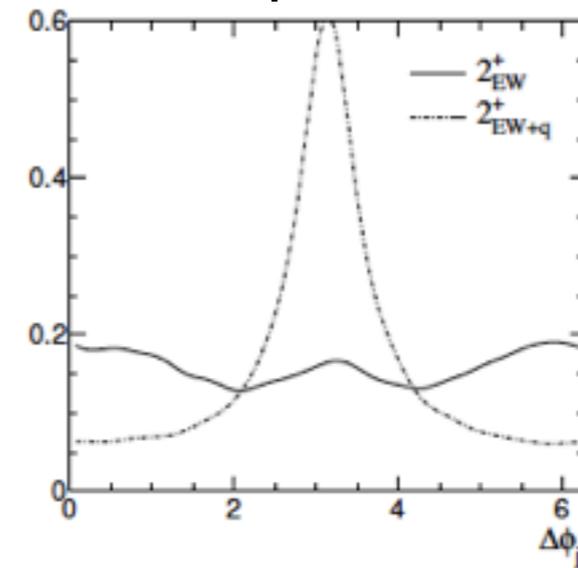
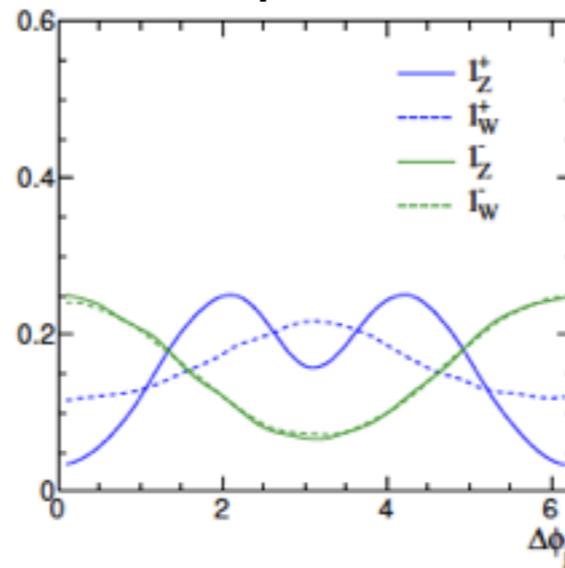
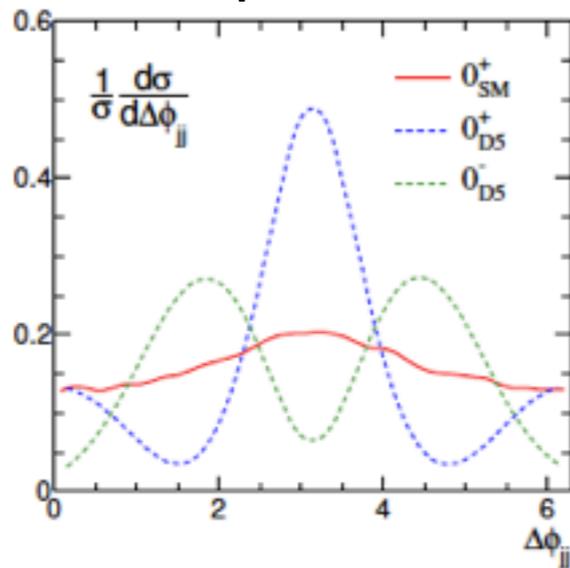
Englert, Goncalves-Netto, KM, Plehn (2013)

di-jet correlations

spin-0

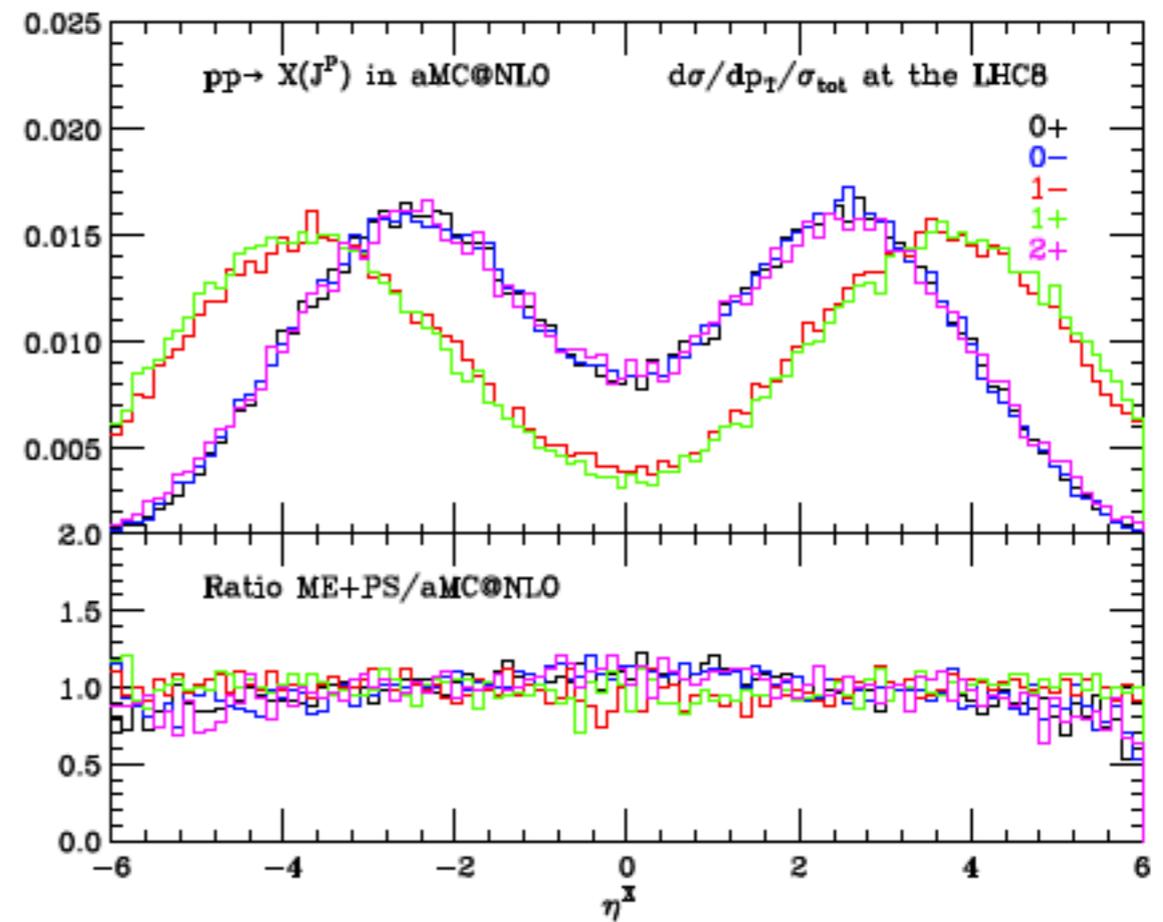
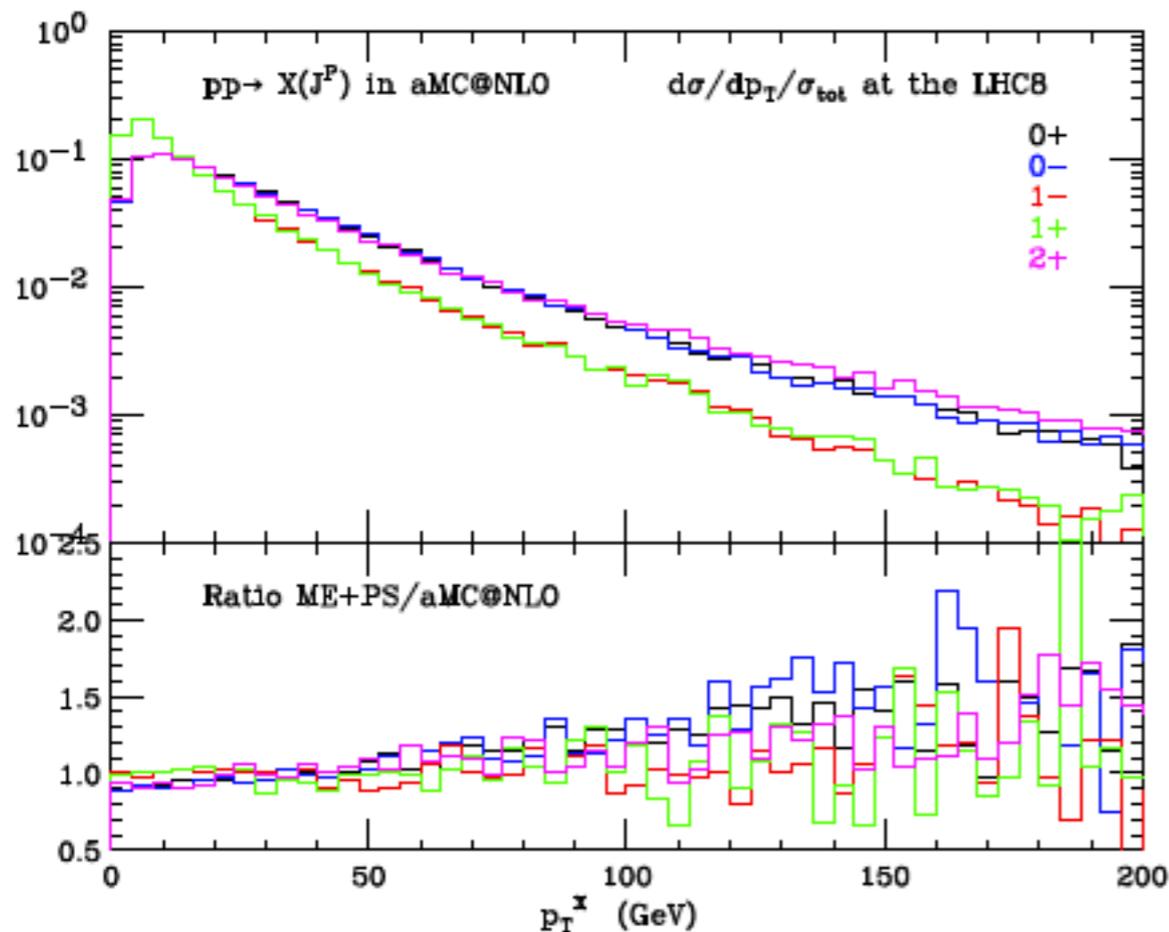
spin-1

spin-2



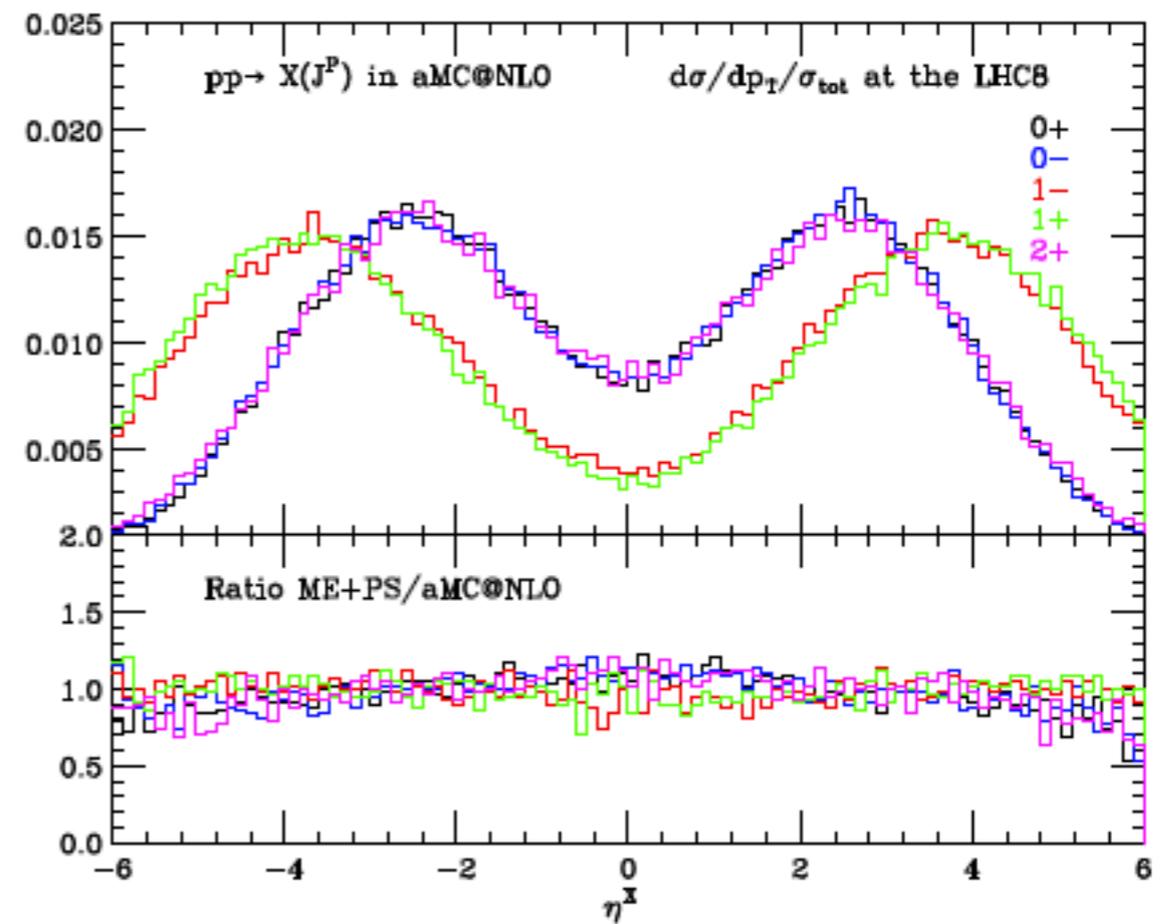
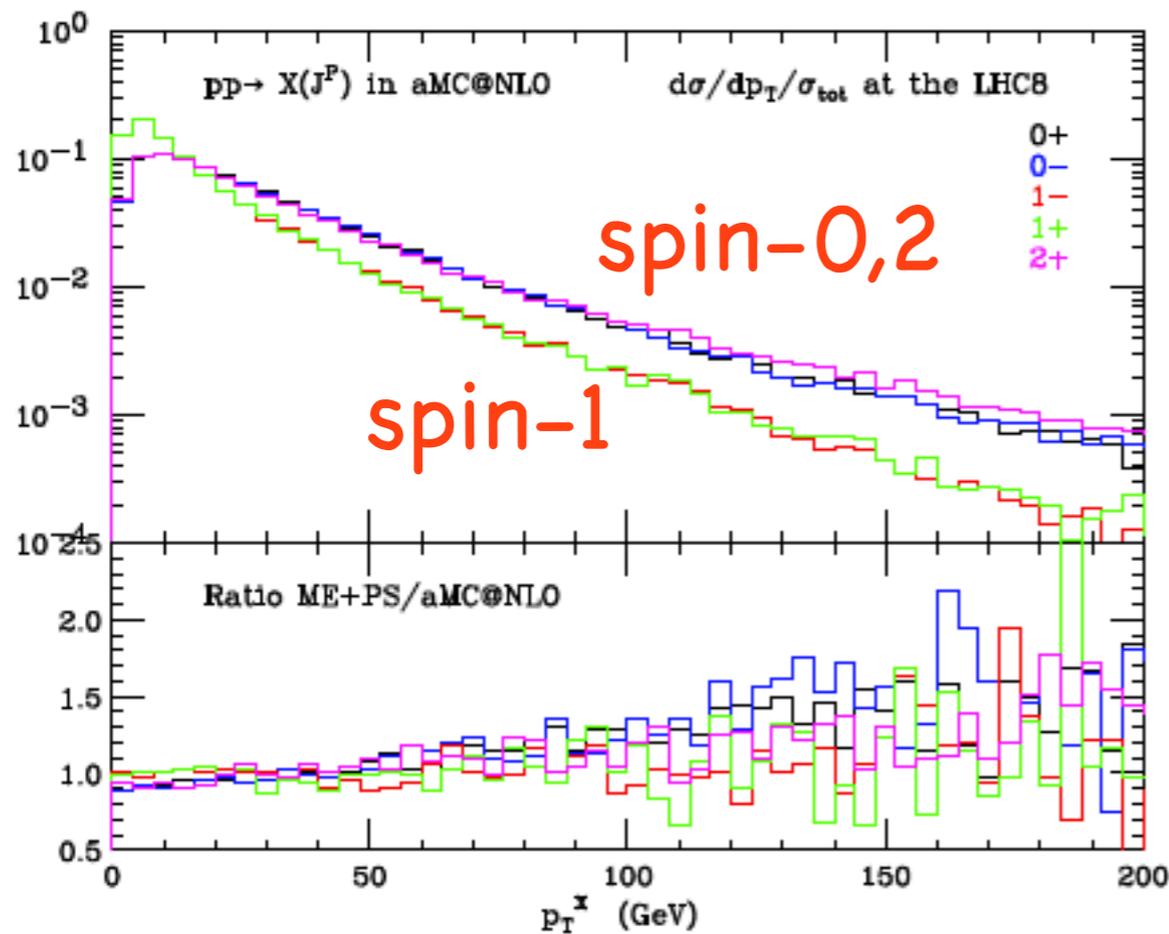
Higher order effects in QCD

- The LO predictions can be systematically improved by including the effects due to the emission of QCD partons.
 - ▶ LO Matrix-Element/Parton-Shower merging [ME+PS]
 - ▶ full-NLO matrix element with parton-shower [aMC@NLO]



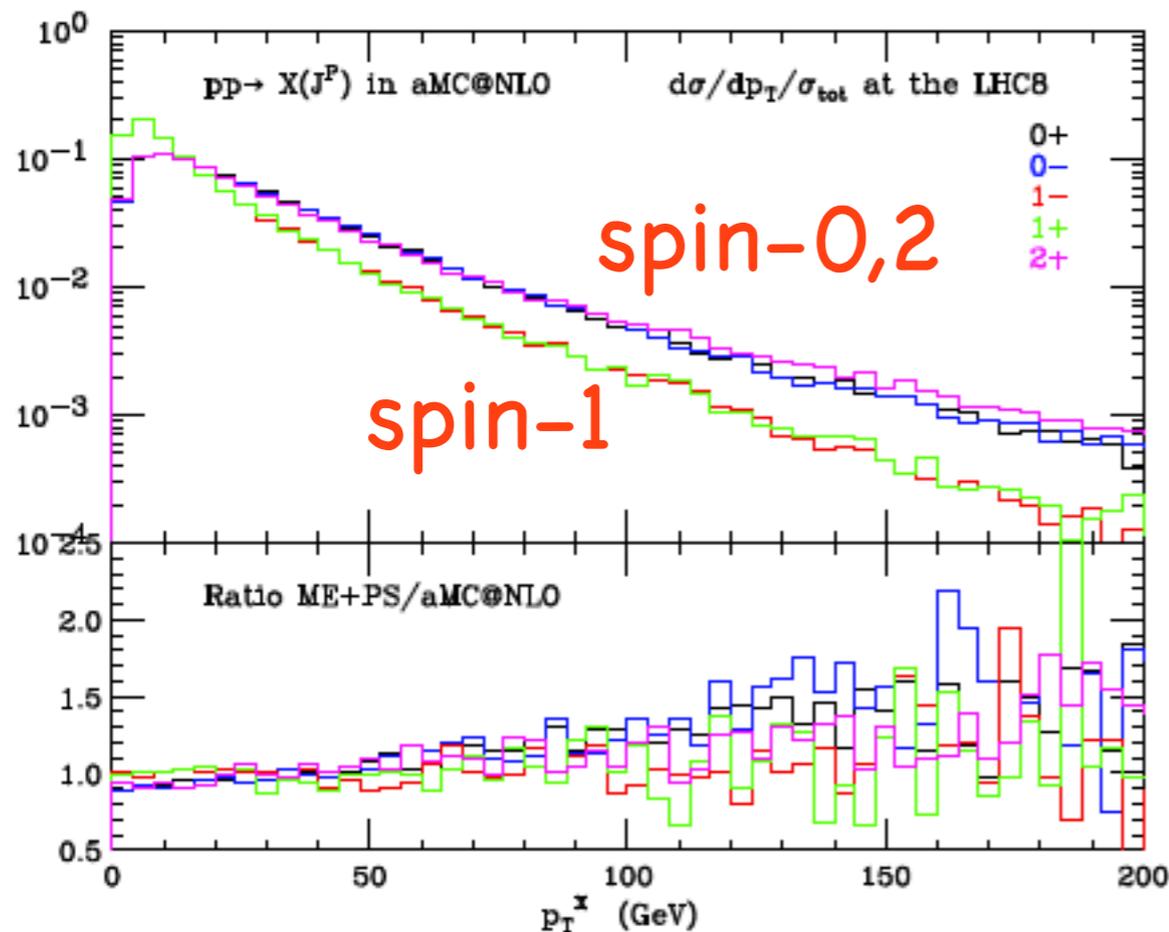
Higher order effects in QCD (I)

inclusive production in $pp \rightarrow X(J^P)$

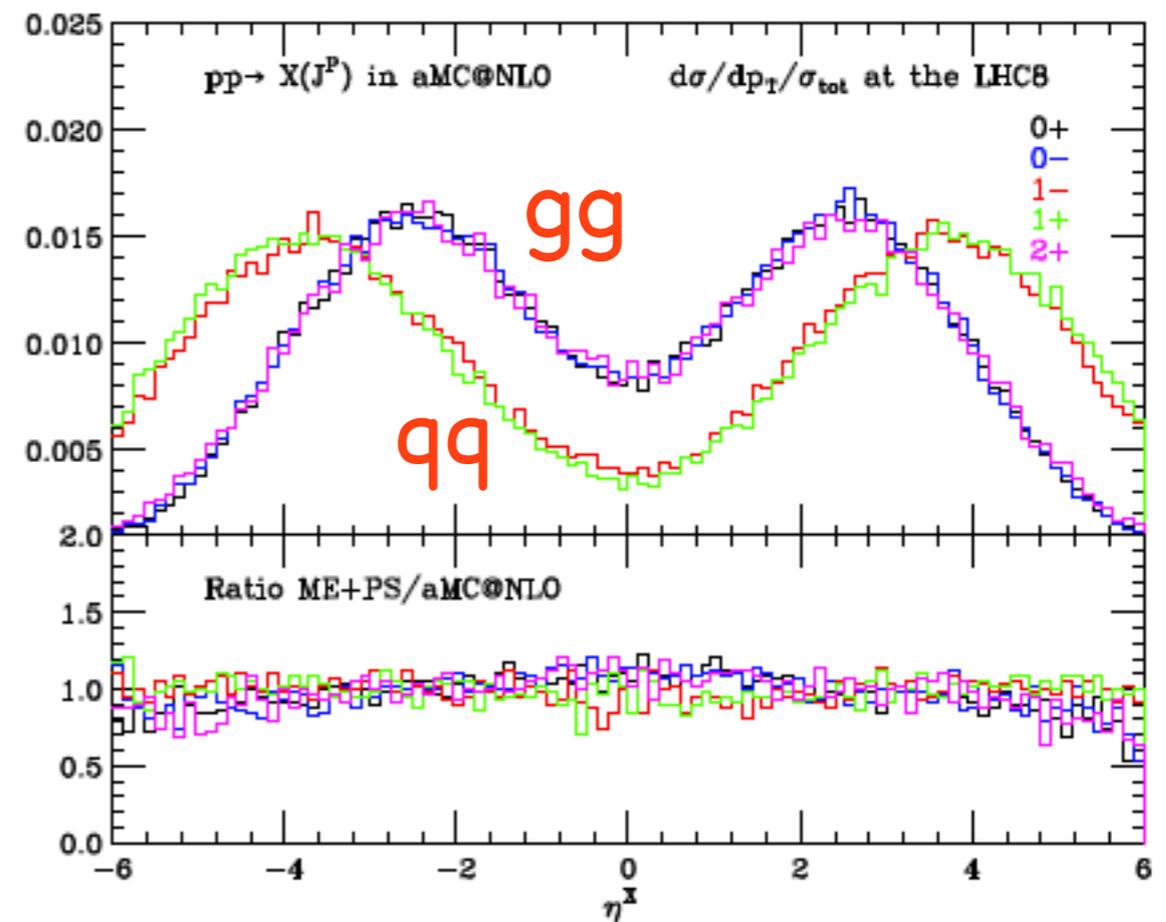


Higher order effects in QCD (I)

inclusive production in $pp \rightarrow X(J^P)$



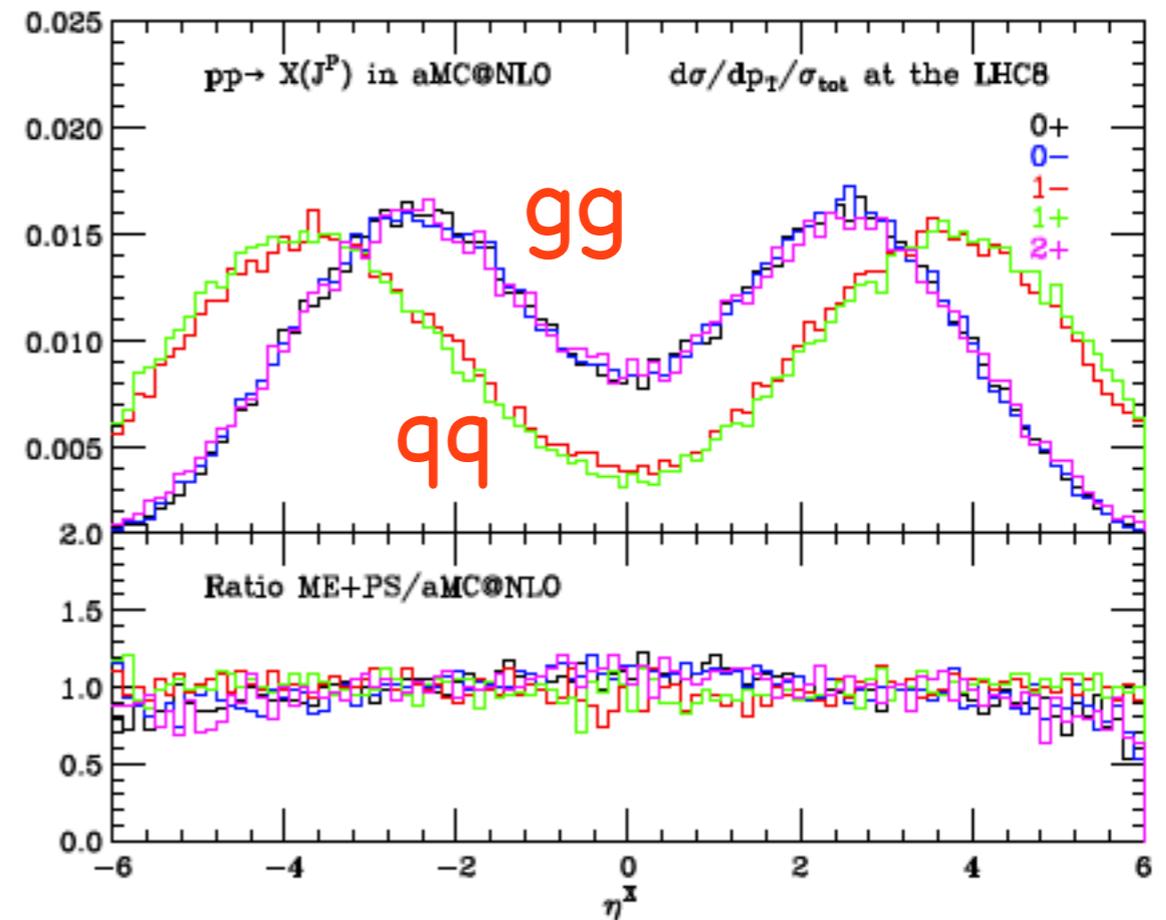
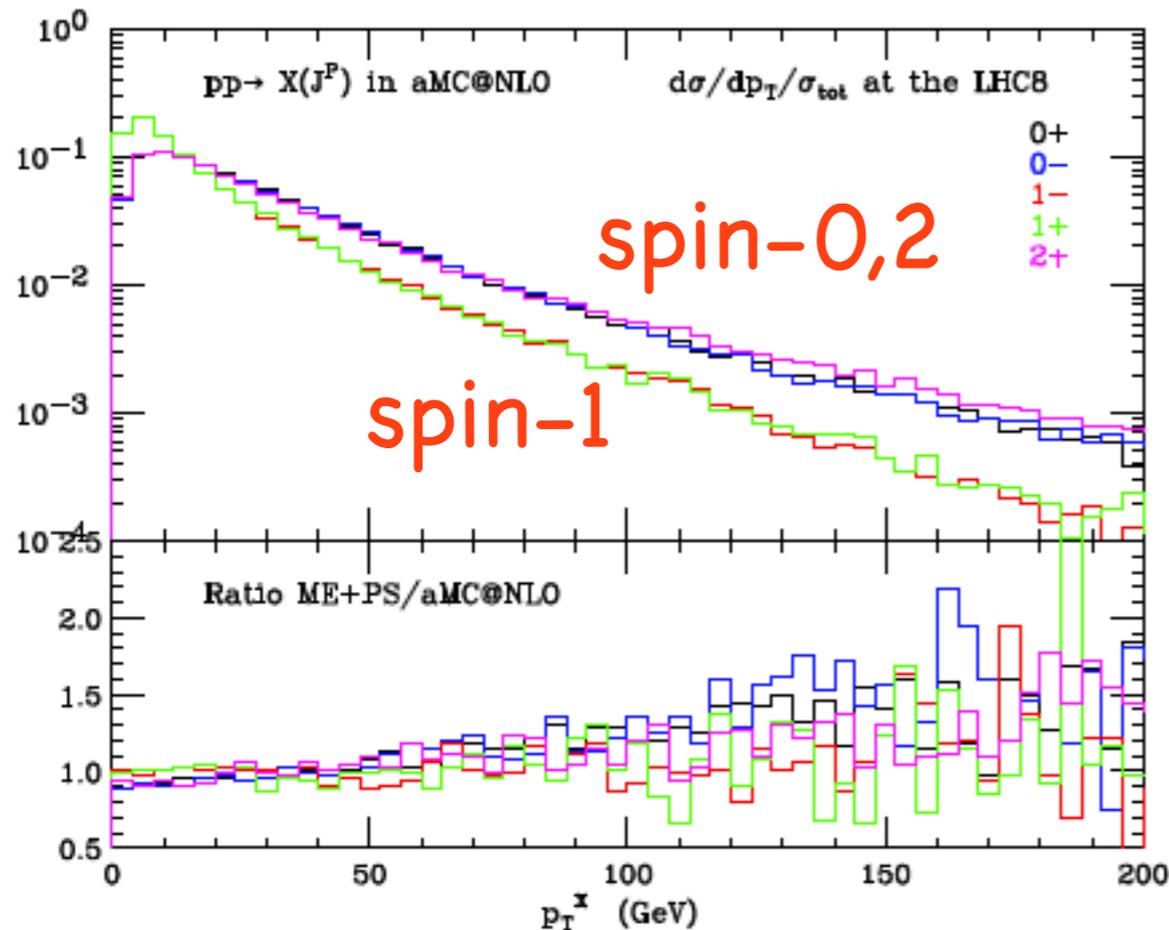
The matched sample is harder than aMC@NLO at large p_T due to the extra 2 ME patrons in the matched sample.



The different shapes are due to the different initial state.

Higher order effects in QCD (I)

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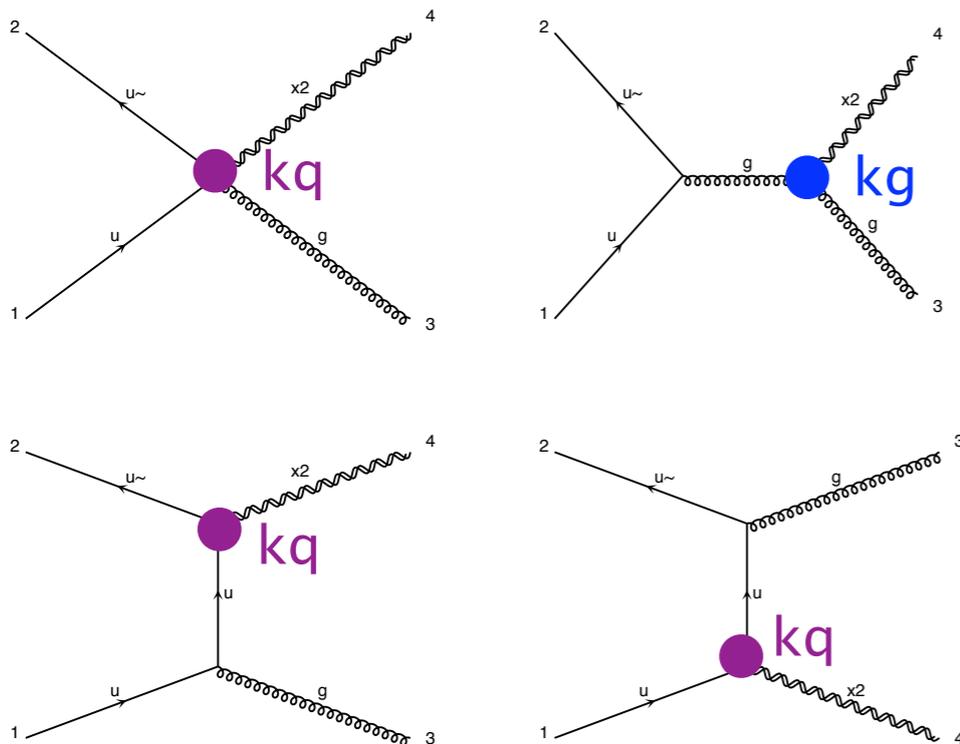
The different shapes are due to the different initial state.

excellent agreement between
ME+PS and aMC@NLO

Higher order effects in QCD (II)

unitarity-violating behavior of models with a spin-2 state

$$\mathcal{L} = -\frac{1}{\Lambda} \kappa_q T_{\mu\nu}^q X_2^{\mu\nu} - \frac{1}{\Lambda} \kappa_g T_{\mu\nu}^g X_2^{\mu\nu}$$



$$|\mathcal{M}|^2 \propto s/\Lambda^2 \quad \text{for } \kappa_q = \kappa_g$$

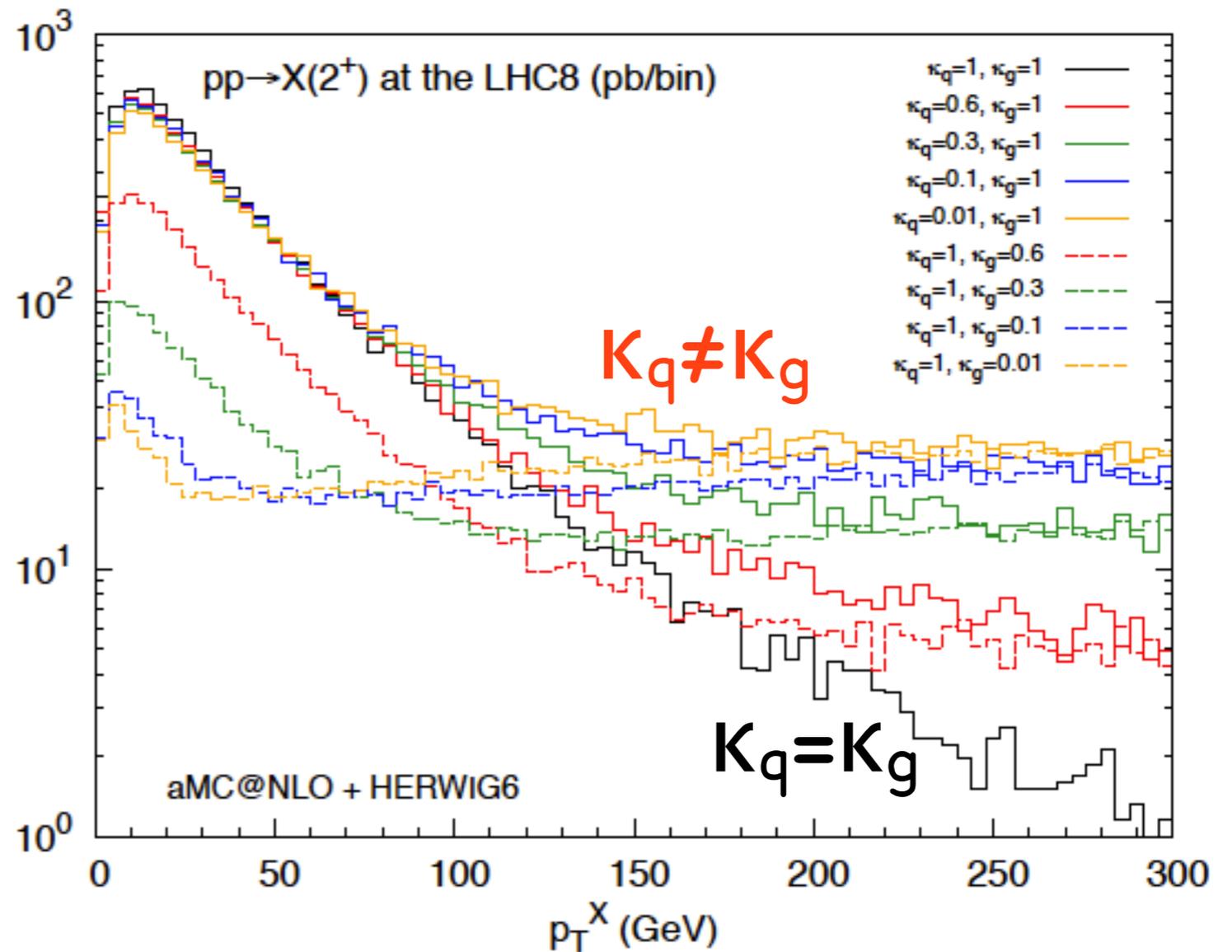
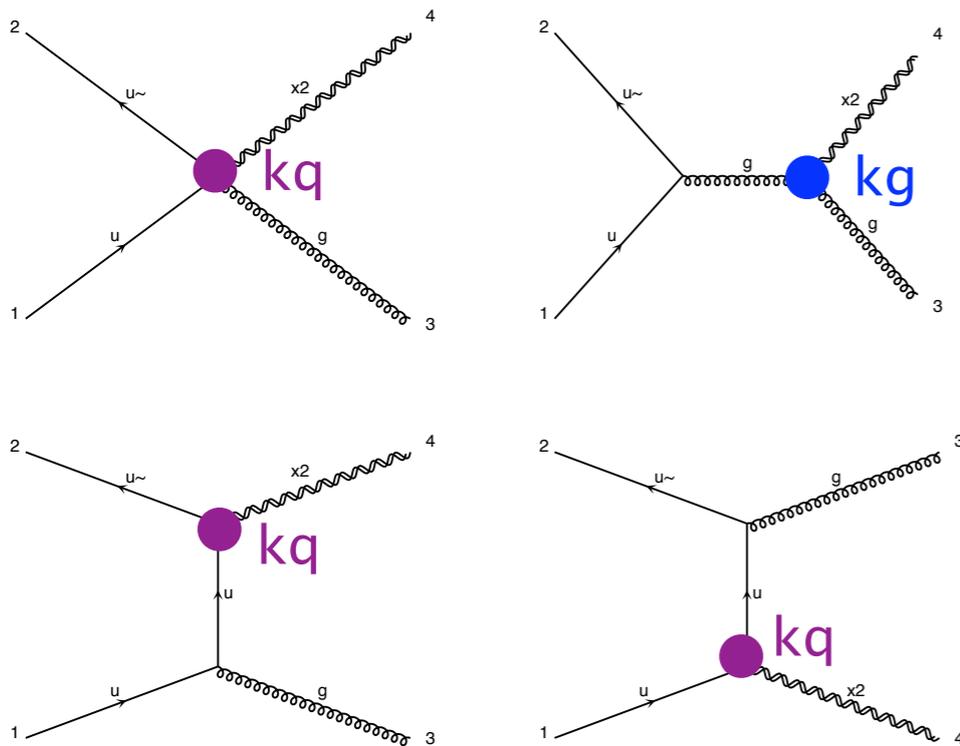
$$|\mathcal{M}|^2 \propto s^3/m^4\Lambda^2 \quad \text{for } \kappa_q \neq \kappa_g$$

$$|\mathcal{M}|^2 = \frac{N}{\Lambda^2 s t u m^4} \left\{ 3\kappa_g^2 m^4 [2m^4 - 2m^2(t+u) + t^2 + u^2] [m^4 - m^2(t+u) + 4tu] \right. \\ \left. + (\kappa_q - \kappa_g) 6\kappa_g m^4 s [m^6 + m^2 s(s+2u) - 2su(s+u)] \right. \\ \left. + (\kappa_q - \kappa_g)^2 s [6m^{10} - 6m^8(t+u) + 3m^6(t^2 + u^2) - 12m^4 tu(t+u) \right. \\ \left. + 2m^2 tu(t^2 + 12tu + u^2) - 2tu(t^3 + t^2 u + tu^2 + u^3)] \right\}, \quad (4.2)$$

Higher order effects in QCD (II)

unitarity-violating behavior of models with a spin-2 state

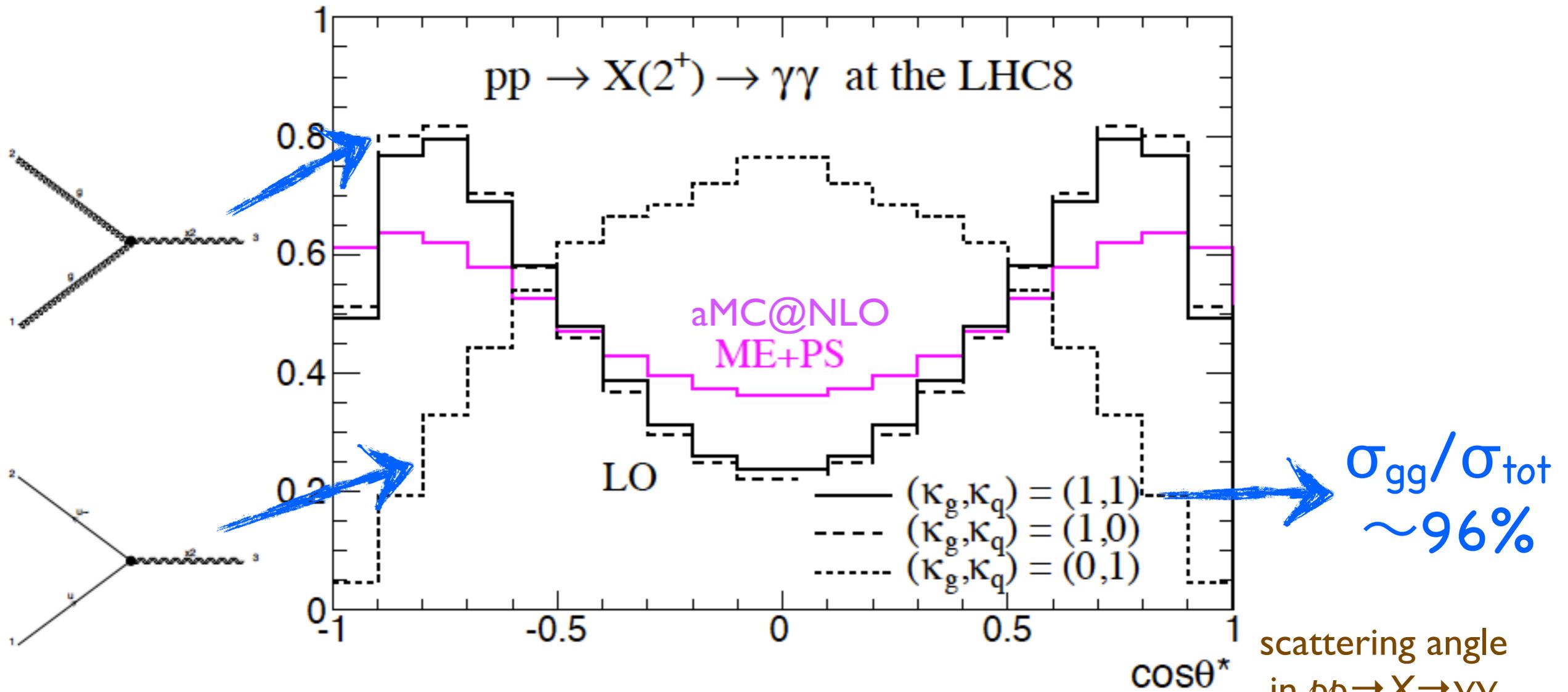
$$\mathcal{L} = -\frac{1}{\Lambda} \kappa_q T_{\mu\nu}^q X_2^{\mu\nu} - \frac{1}{\Lambda} \kappa_g T_{\mu\nu}^g X_2^{\mu\nu}$$



A model with non-universal couplings dramatically changes the $p_T(X)$ spectrum.

Higher order effects in QCD (III)

on spin observables for a spin-2 state



$$\frac{d\sigma(gg)}{d \cos \theta^*} \propto |d_{22}^2(\theta^*)|^2 + |d_{2-2}^2(\theta^*)|^2 = \frac{1}{8}(1 + 6 \cos^2 \theta^* + \cos^4 \theta^*),$$

$$\frac{d\sigma(q\bar{q})}{d \cos \theta^*} \propto |d_{12}^2(\theta^*)|^2 + |d_{1-2}^2(\theta^*)|^2 = \frac{1}{2}(1 - \cos^4 \theta^*).$$

Summary

- After the discovery of a Higgs-like resonance at the LHC, the main focus of the analyses now is **the determination of the Higgs Lagrangian**.
- This includes
 - **the structure of the operators**, linked to the spin/parity of the ‘Higgs’ boson.
 - an independent measurement of **the coupling strength**.
- Our **FR/MG5 Higgs Characterisation model** is publicly available, which can provide a framework to perform SMS characterisation studies in a **consistent, systematic and accurate** way.
 - <http://feynrules.irmp.ucl.ac.be/wiki/HiggsCharacterisation>
 - contact to kentarou.mawatari@vub.ac.be

back-up

Effective Lagrangian \rightarrow Feynman rules

$$\begin{aligned}
 \mathcal{L} = \frac{1}{2} c_\alpha \kappa_{\text{SM}} g_{HZZ} Z_\mu Z^\mu X_0 &\longrightarrow i c_\alpha \kappa_{\text{SM}} g_{HZZ} g_{\mu\nu} \\
 -\frac{1}{4} \frac{1}{\Lambda} c_\alpha \kappa_{HZZ} Z_{\mu\nu} Z^{\mu\nu} &\longrightarrow i c_\alpha \frac{\kappa_{HZZ}}{\Lambda} (g_{\mu\nu} q_1 \cdot q_2 - q_{2\mu} q_{1\nu}) \\
 -\frac{1}{4} \frac{1}{\Lambda} s_\alpha \kappa_{AZZ} Z_{\mu\nu} \tilde{Z}^{\mu\nu} &\longrightarrow i s_\alpha \frac{\kappa_{AZZ}}{\Lambda} \epsilon_{\mu\nu\rho\sigma} q_2^\rho q_1^\sigma \\
 -\frac{1}{\Lambda} c_\alpha \kappa_{H\partial Z} Z_\nu \partial_\mu Z^{\mu\nu} &\longrightarrow i c_\alpha \frac{\kappa_{H\partial Z}}{\Lambda} [g_{\mu\nu} (q_1 \cdot q_1 + q_2 \cdot q_2) - q_{1\mu} q_{1\nu} - q_{2\mu} q_{2\nu}]
 \end{aligned}$$

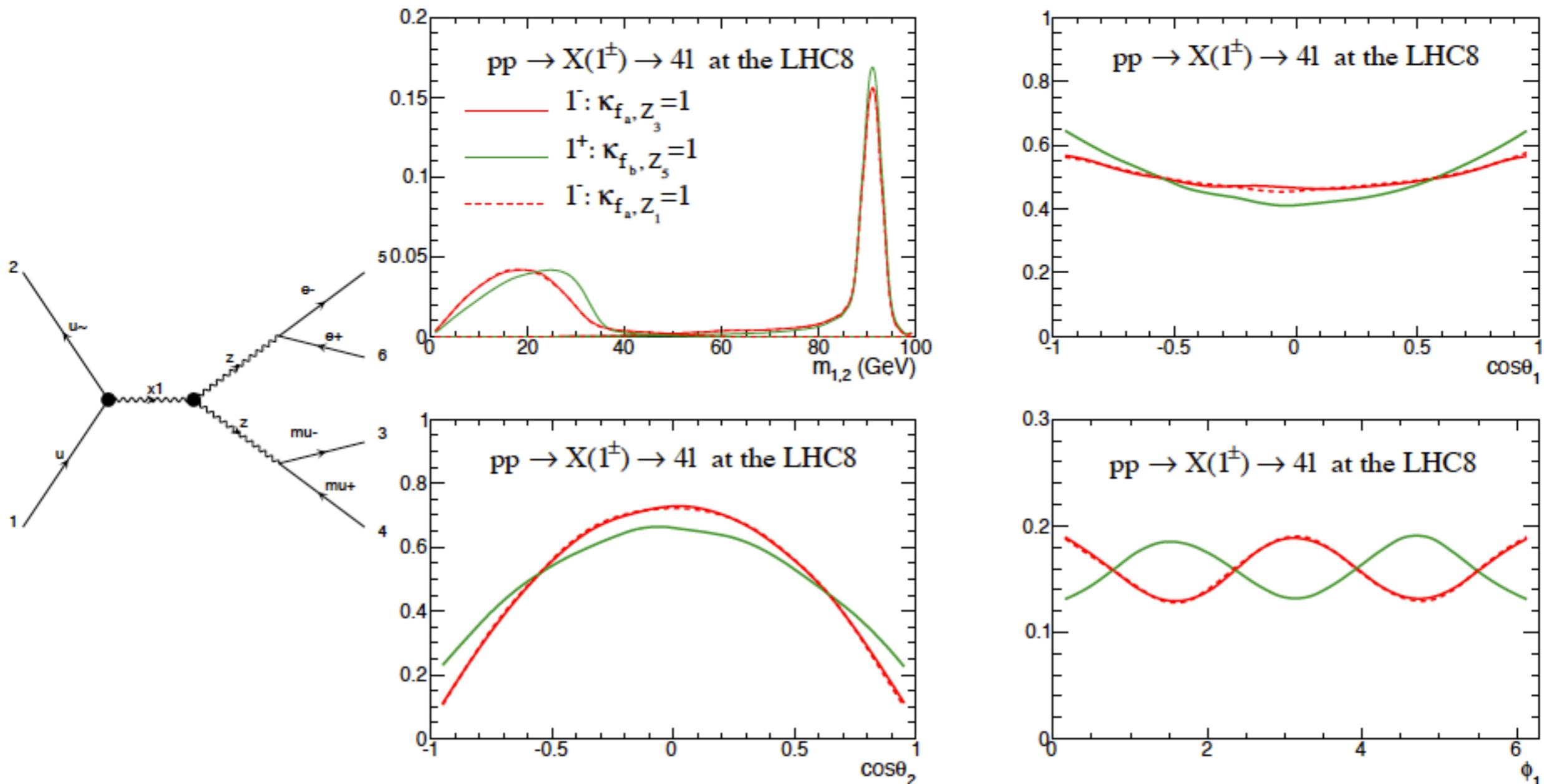
hyp. SM : SM-like coupling to the Z bosons

$$\kappa_{\text{SM}} = 1 \quad \kappa_{HZZ} = 0 = \kappa_{AZZ} \quad c_\alpha = 1$$

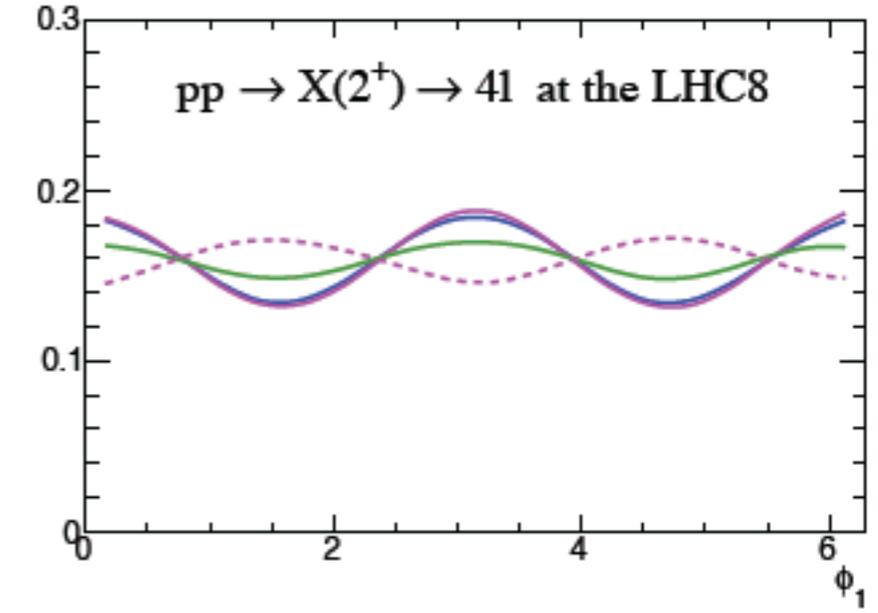
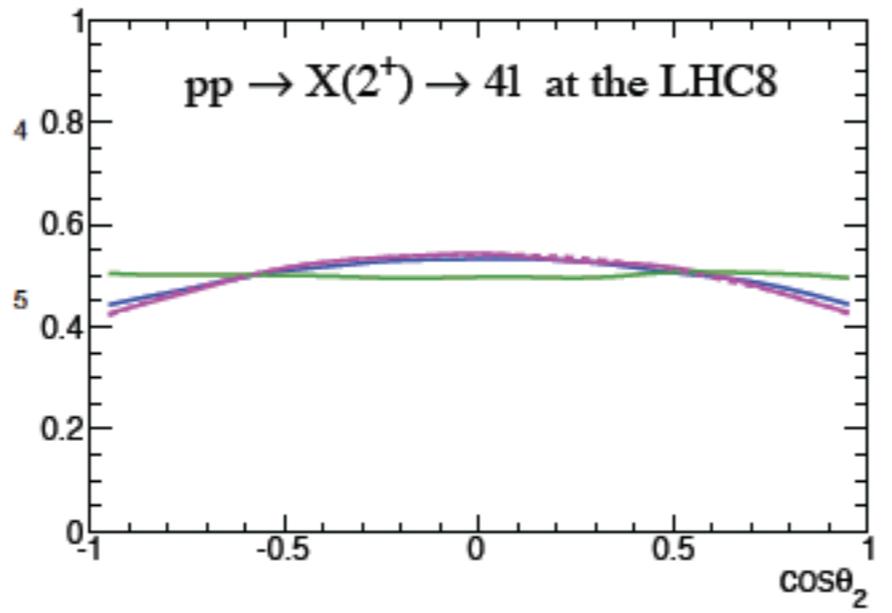
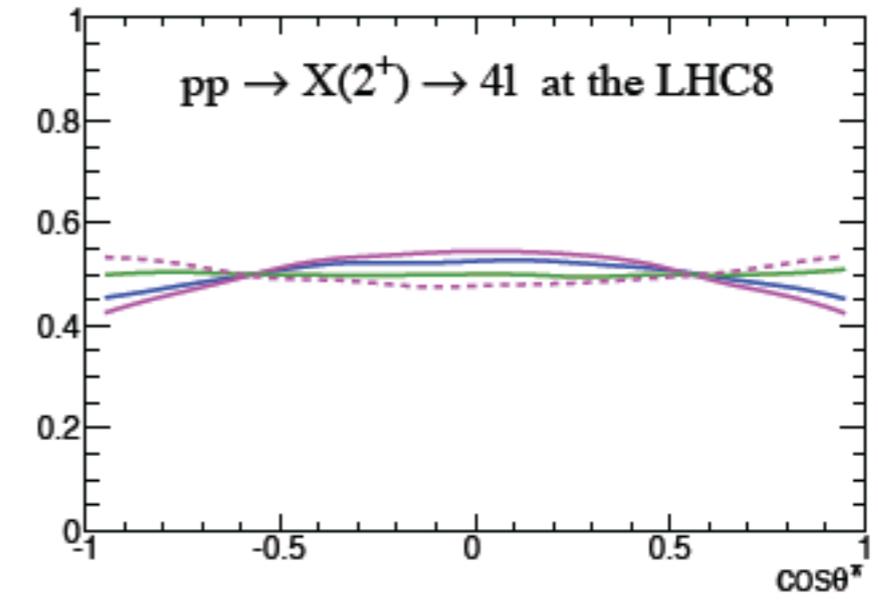
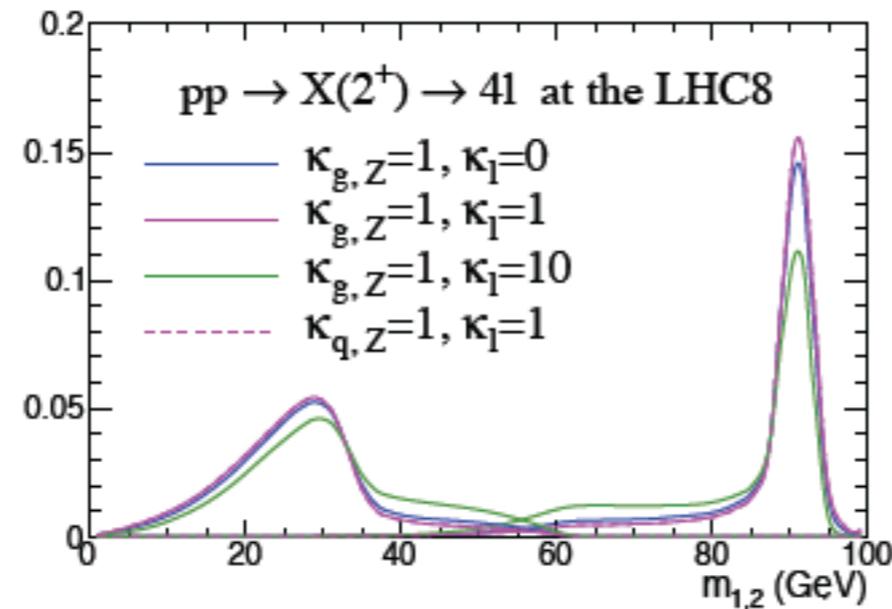
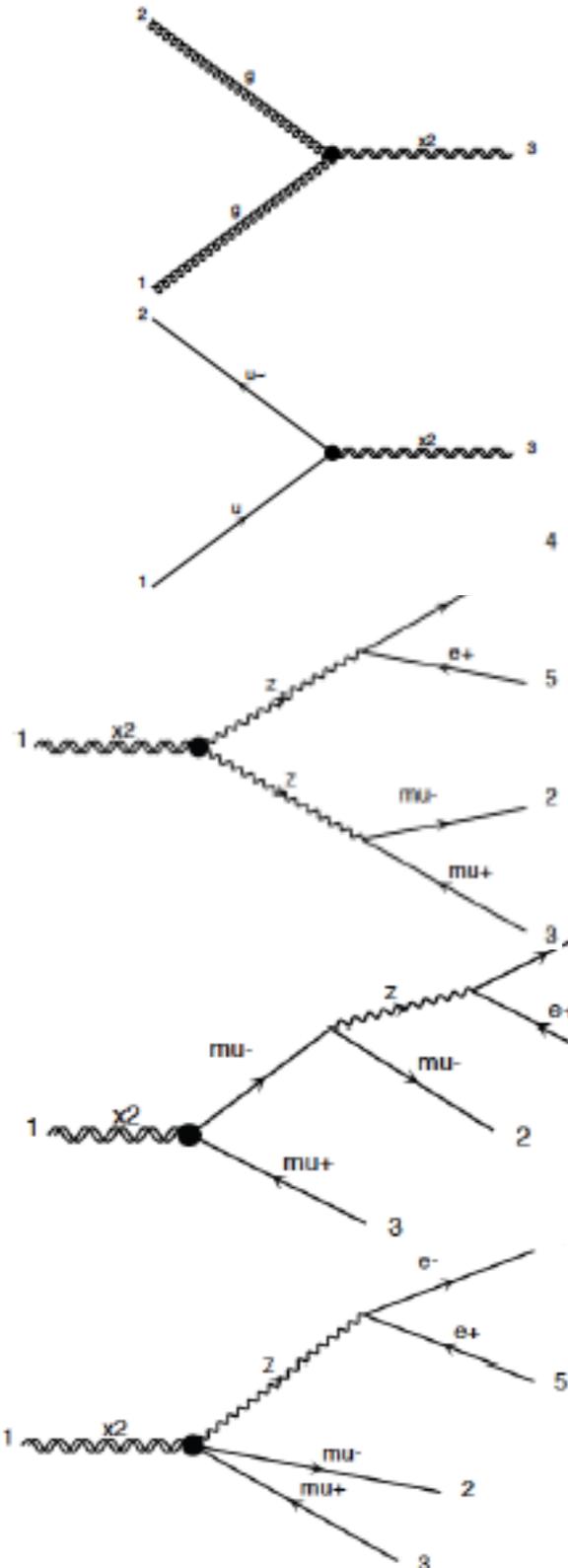
hyp. HD: coupling involving a superposition of HD operators $Z_{\mu\nu} Z^{\mu\nu}$ and $Z_{\mu\nu} \tilde{Z}^{\mu\nu}$

$$\kappa_{\text{SM}} = 0 \quad \kappa_{HZZ} = 1 = \kappa_{AZZ} \quad c_\alpha \text{ free}$$

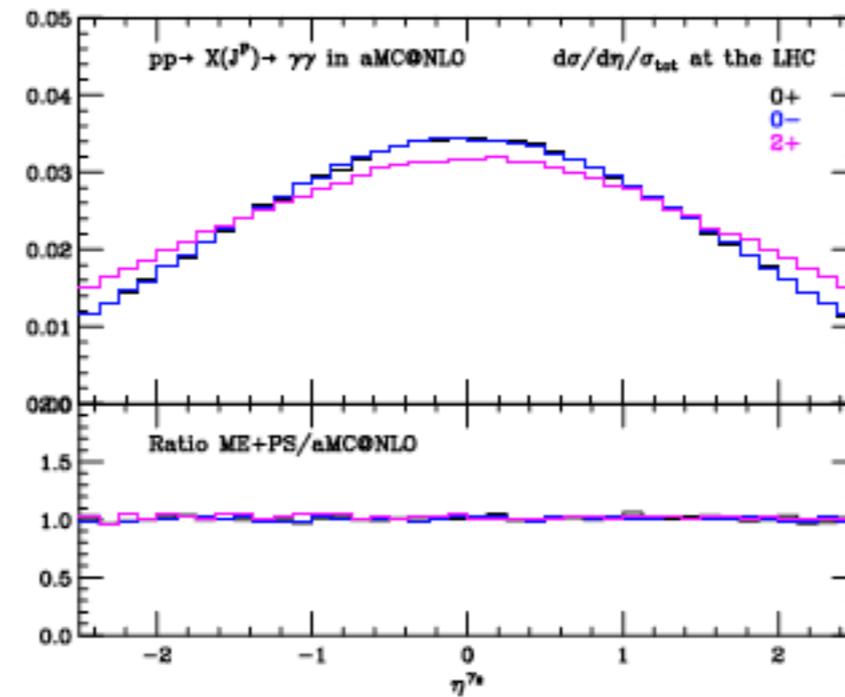
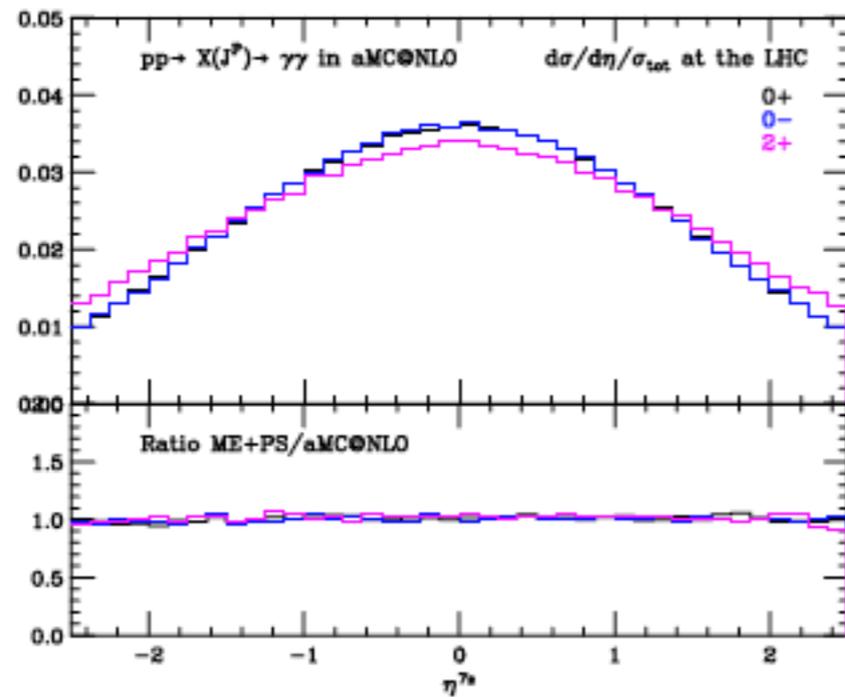
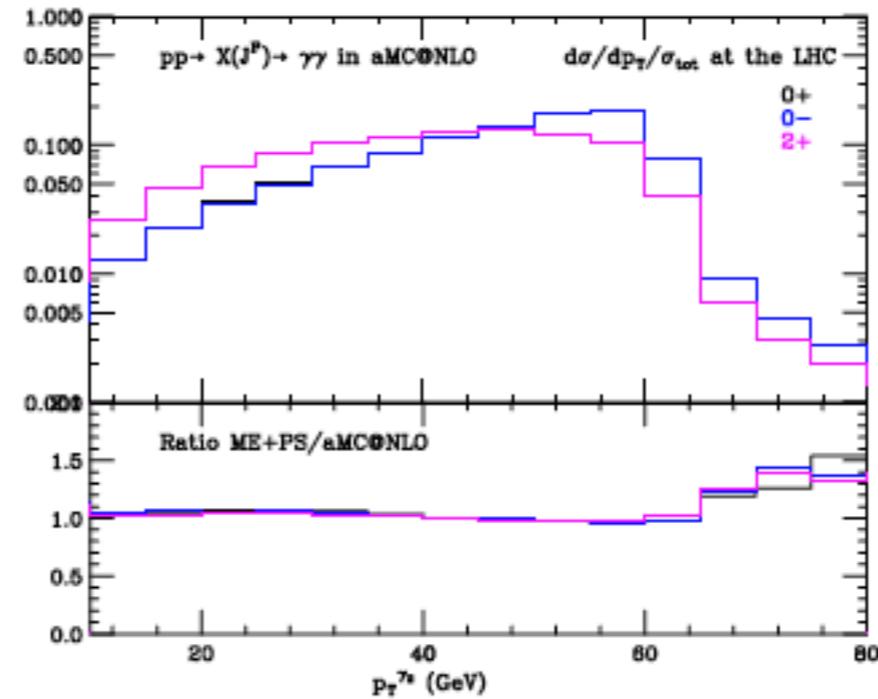
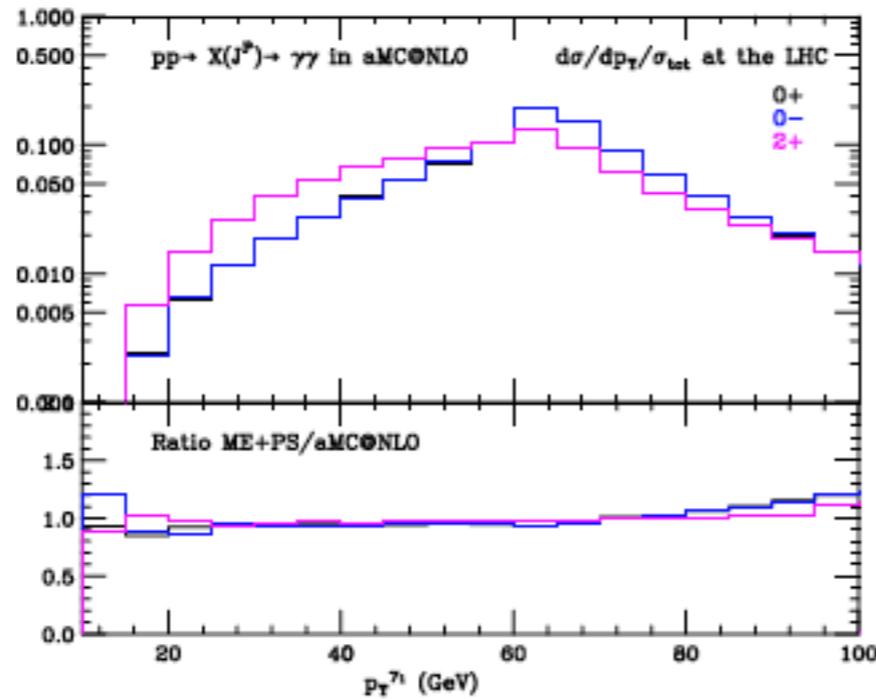
Mass and angular distributions -- spin 1



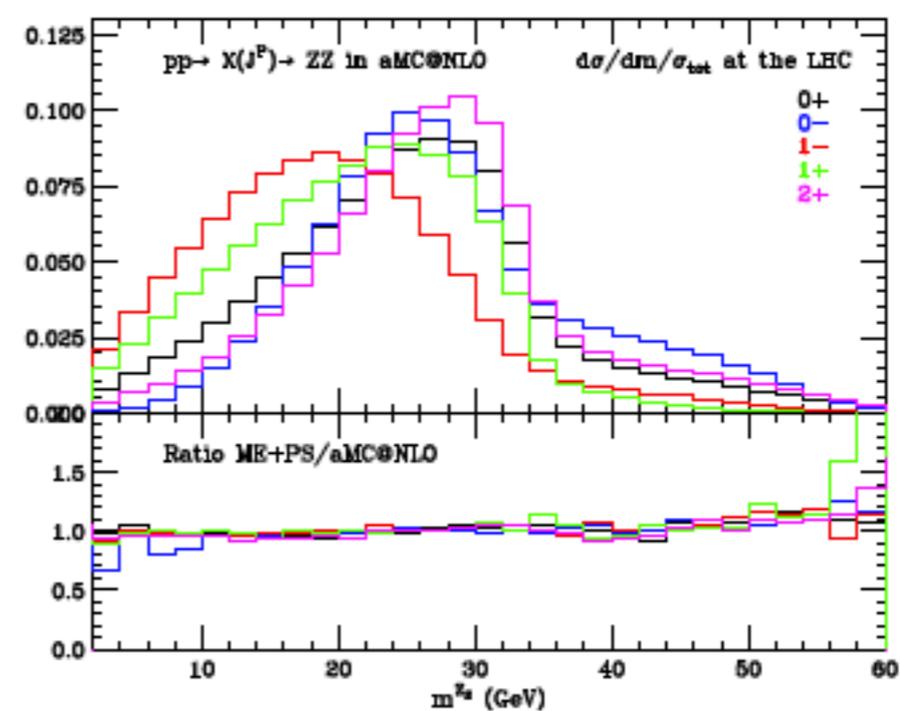
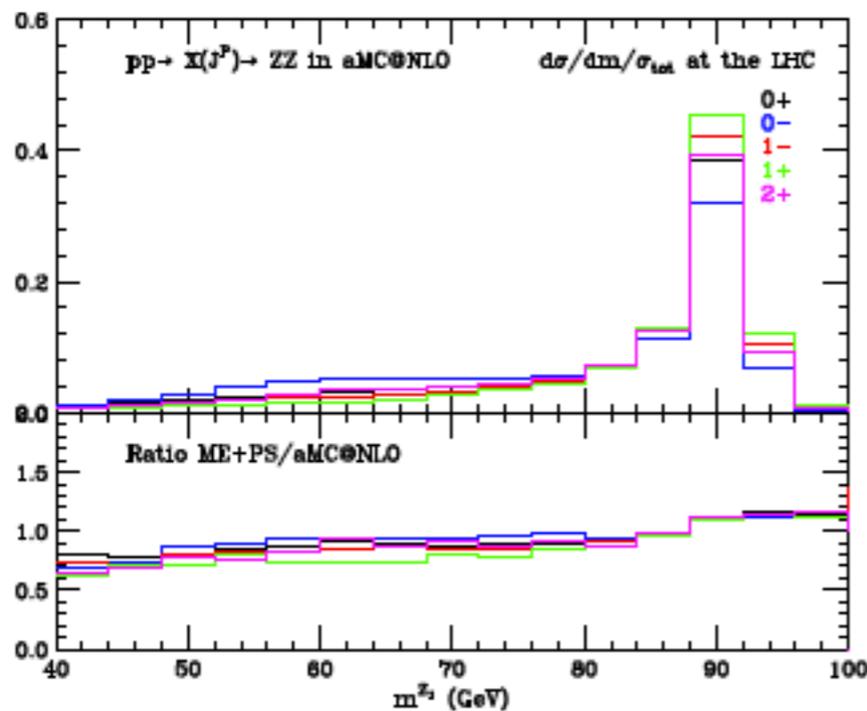
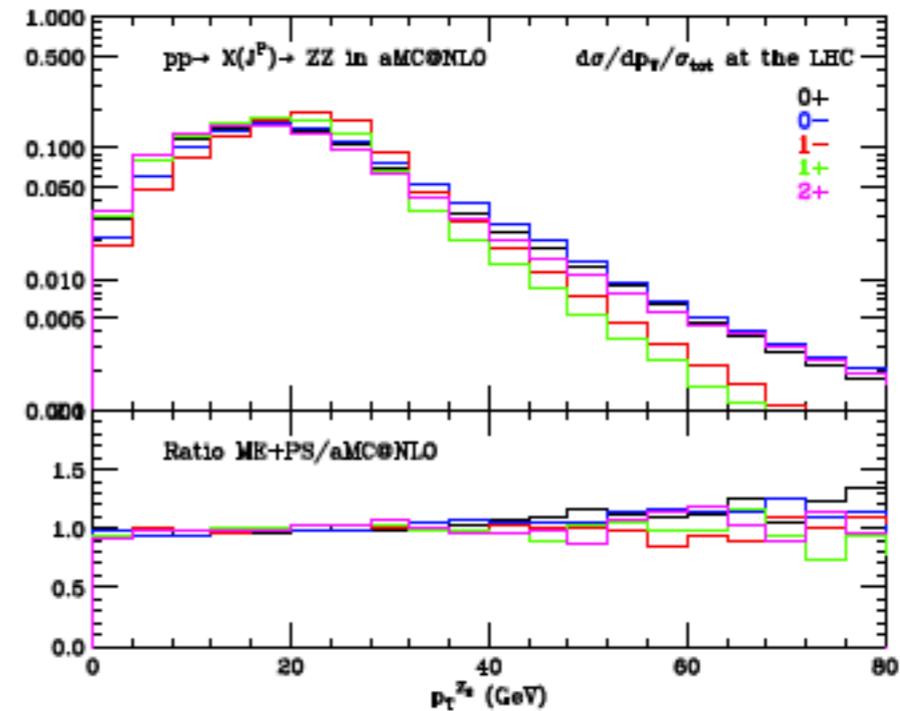
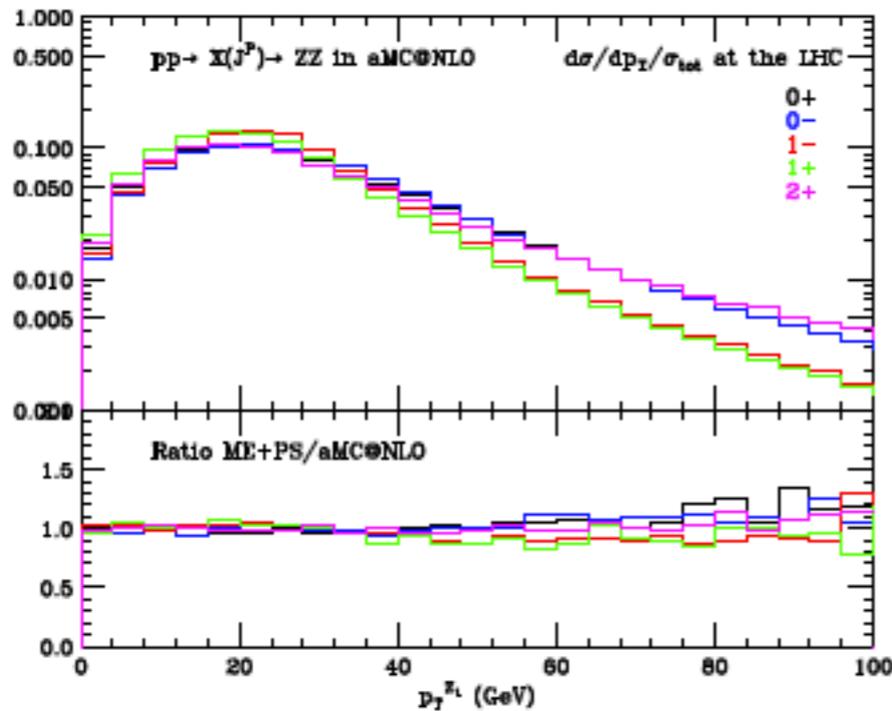
Mass and angular distributions -- spin2



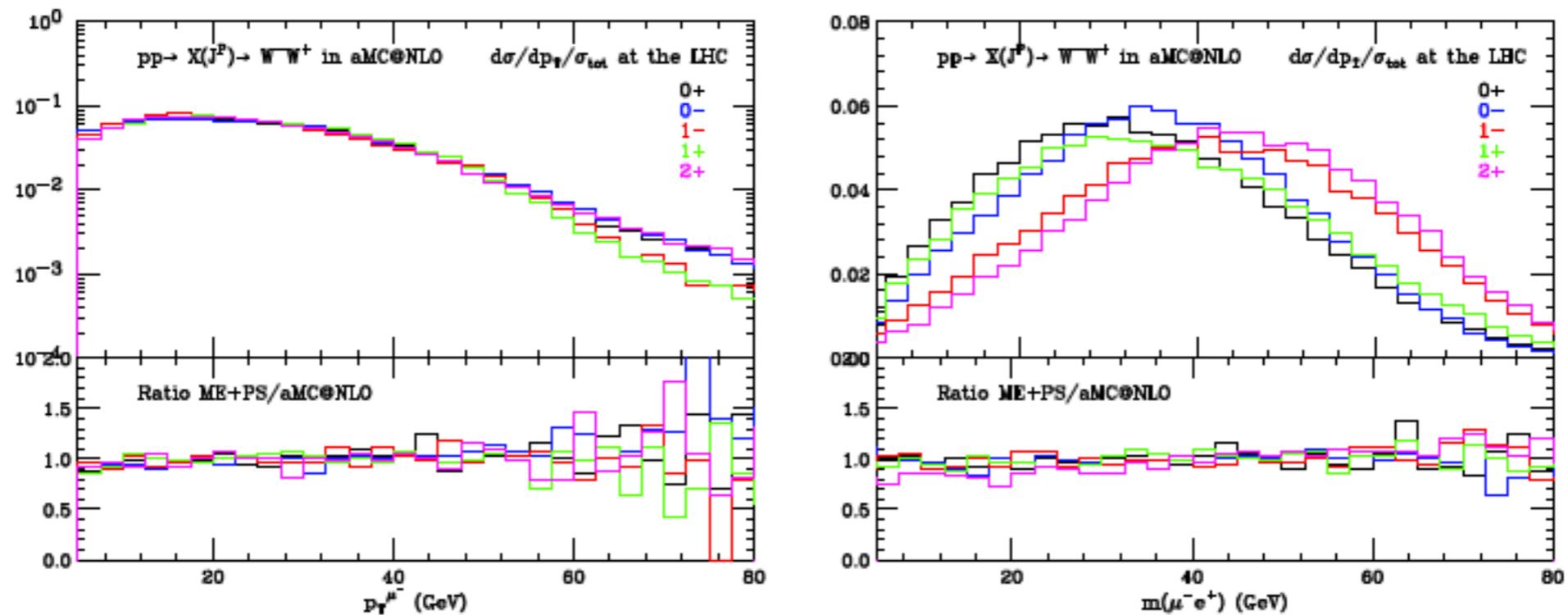
Accuracy with aMC@NLO/ME+PS merging



Accuracy with aMC@NLO/ME+PS merging



Accuracy with aMC@NLO/ME+PS merging



How can we get the spin/parity information?

1. $X \rightarrow \gamma\gamma$

2. $X \rightarrow VV^* \rightarrow 4l$

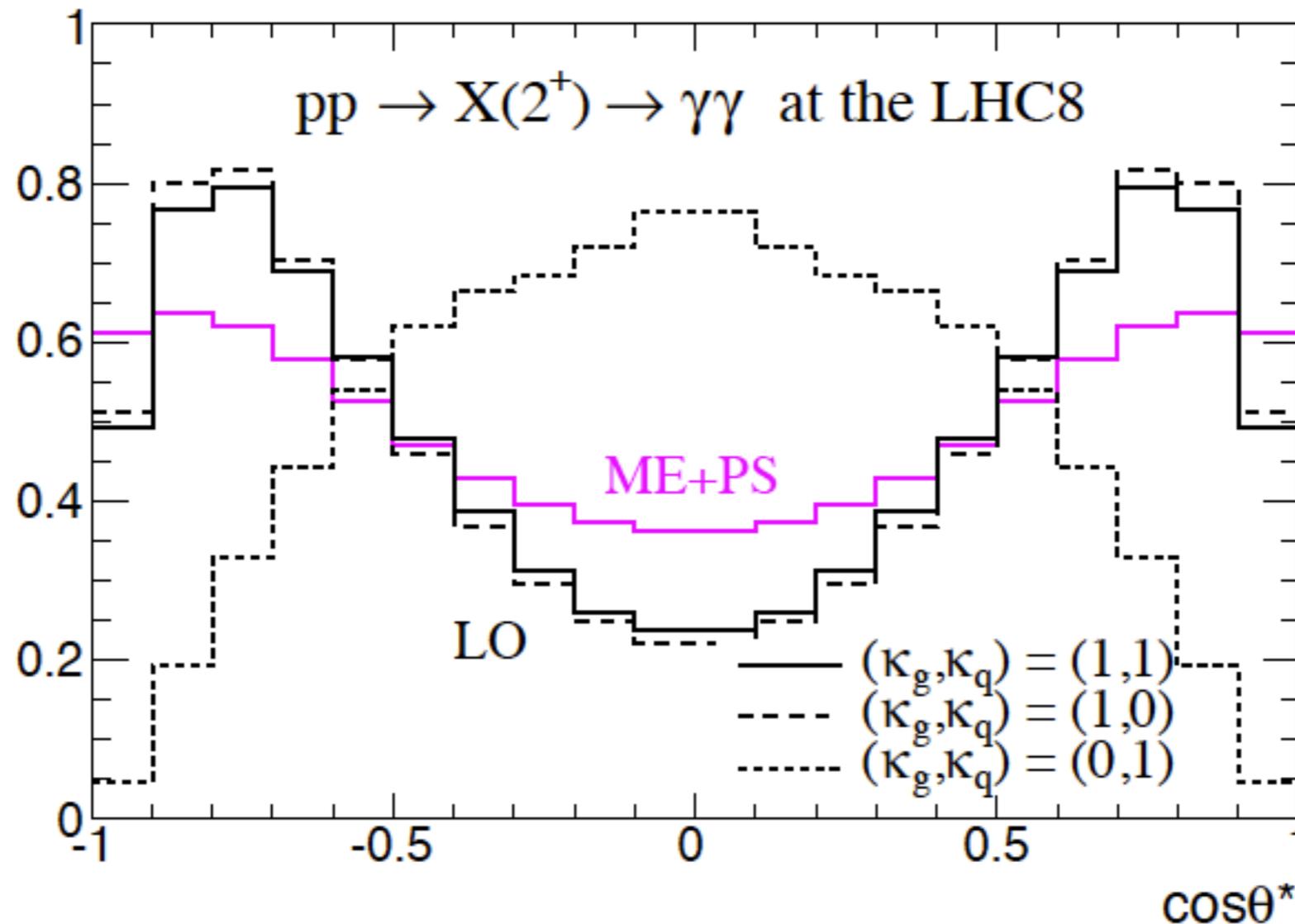
3. $pp \rightarrow jjX$

4. $pp \rightarrow VX$

5. $X \rightarrow \tau\tau$

Spin/parity determination

I. $X \rightarrow \gamma\gamma$



$$\frac{d\sigma(gg)}{d\cos\theta^*} \propto |d_{22}^2(\theta^*)|^2 + |d_{2-2}^2(\theta^*)|^2 = \frac{1}{8}(1 + 6\cos^2\theta^* + \cos^4\theta^*),$$

$$\frac{d\sigma(qq)}{d\cos\theta^*} \propto |d_{12}^2(\theta^*)|^2 + |d_{1-2}^2(\theta^*)|^2 = \frac{1}{2}(1 - \cos^4\theta^*).$$

Spin/parity determination

2. $X \rightarrow VV^* \rightarrow 4l$

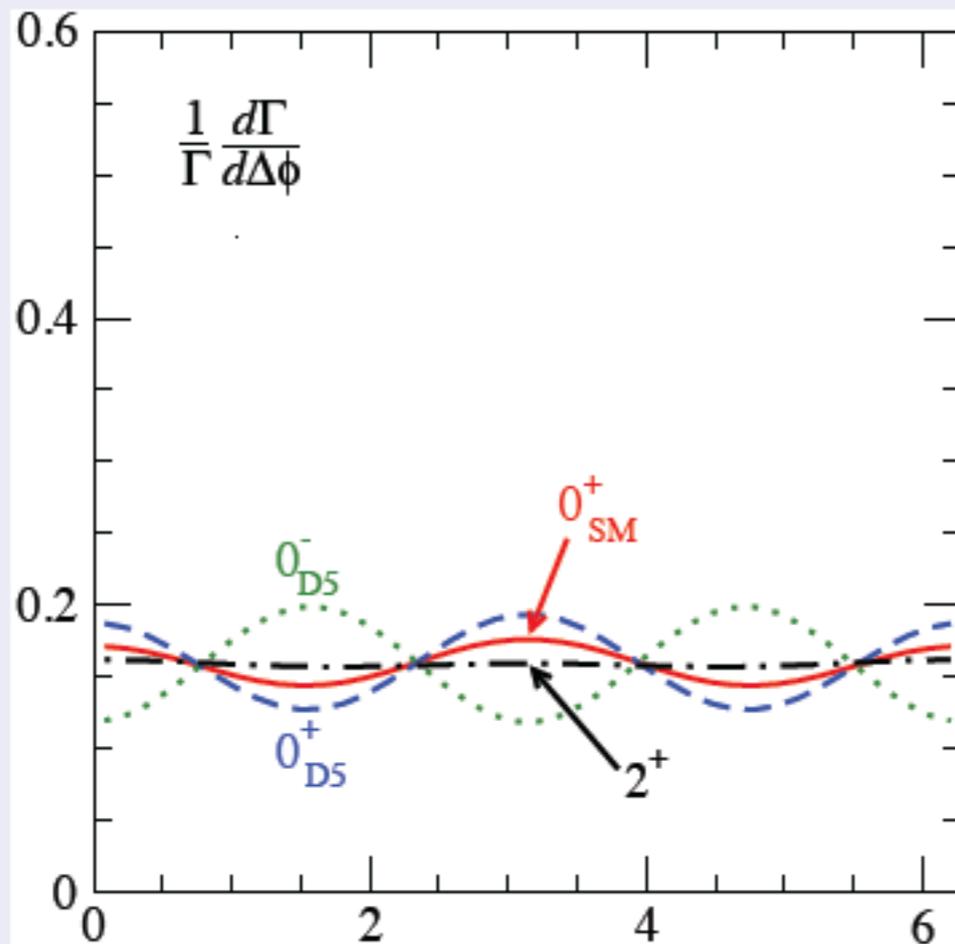
[Dell'Aquila, Nelson, PRD(1986)]

[Choi, Miller, Mühlleitner, Zerwas, PLB(2003)]

[Gao et al, PRD(2010)] ...

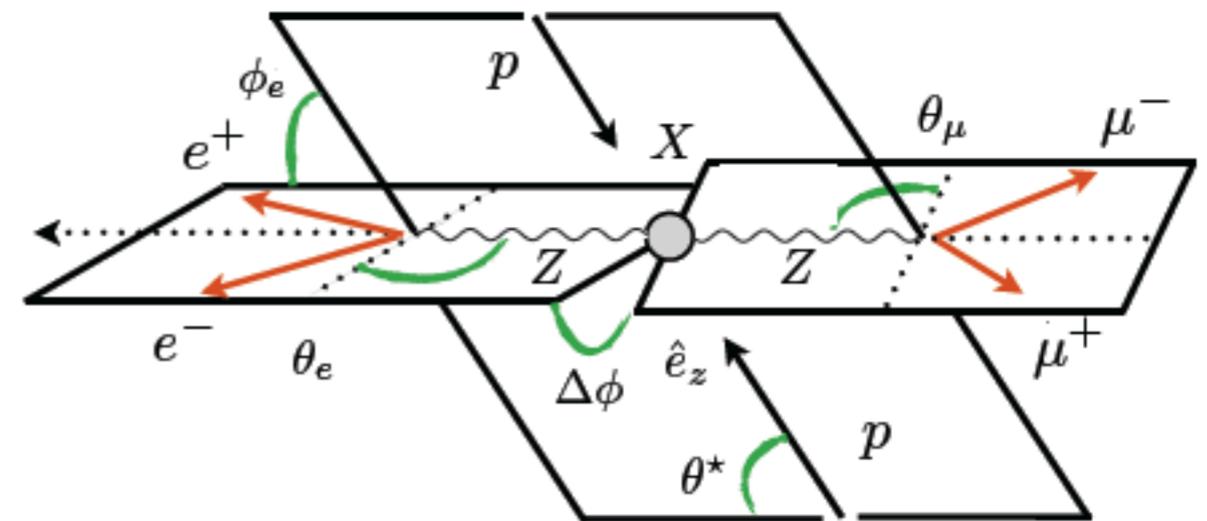
[Bolognesi et al, PRD(2012)]

$X \rightarrow ZZ^* \rightarrow 4l$



$d\sigma/d\Delta\phi \sim \text{const.}$ for 0^+_{SM} ,

$d\sigma/d\Delta\phi \sim 1 \pm A \cos 2\Delta\phi$ for 0^\pm_{D5} .



Spin/parity determination

$X \rightarrow 4l$ vs. VBF

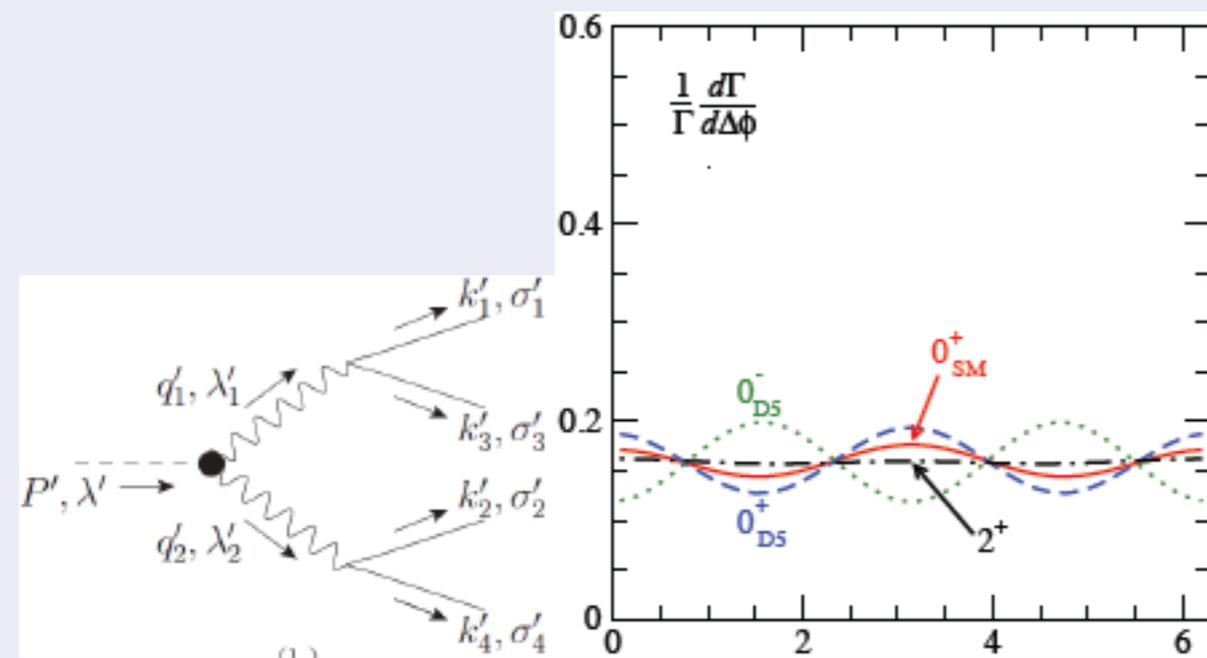
[Choi, Miller, Mühlleitner, Zerwas, PLB(2003)]
[Gao et al, PRD(2010)] ...

[Plehn, Rainwater, Zeppenfeld, PRL(2002)]
[Hagiwara, Li, KM, JHEP(2009)] ...

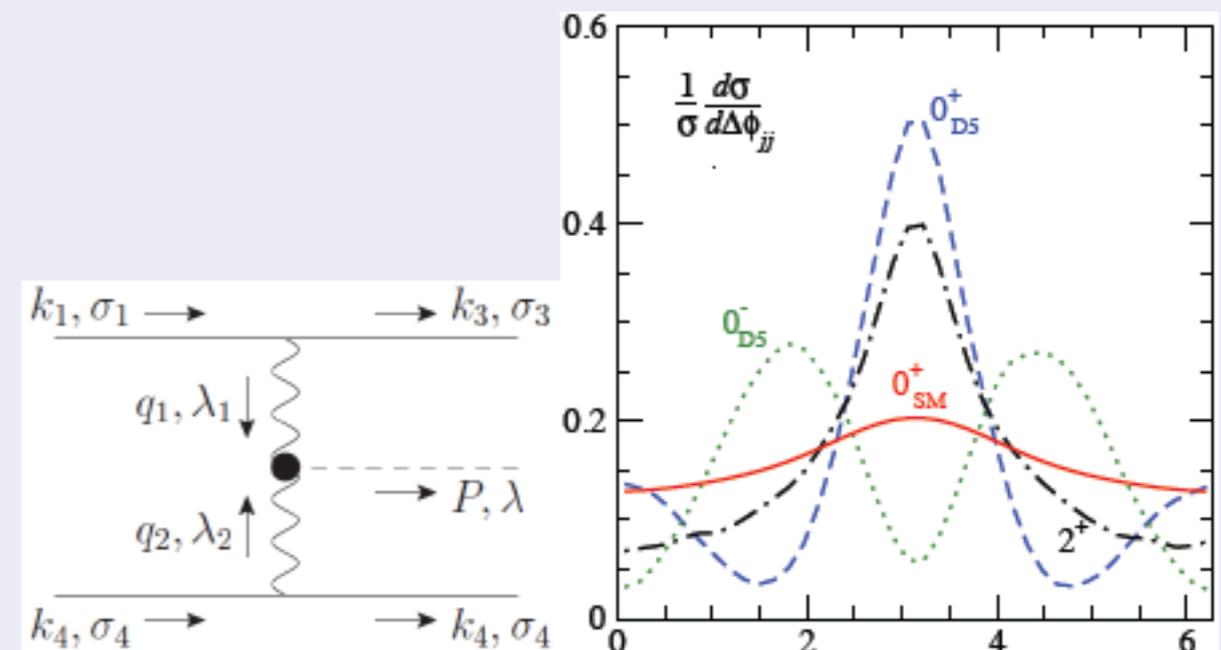
[Bolognesi et al, PRD(2012)]

[Englert, Goncalves-Netto, KM, Plehn, JHEP(2013)]

$X \rightarrow ZZ^* \rightarrow 4l$



Vector boson fusion (VBF)



$$d\sigma/d\Delta\phi \sim \text{const. for } 0_{SM}^+, \quad d\sigma/d\Delta\phi \sim 1 \pm A \cos 2\Delta\phi \text{ for } 0_{D5}^\pm.$$

Nontrivial azimuthal angle correlations of the decay planes ($X \rightarrow ZZ$) and the jets (VBF) can be explained as the quantum interference among different helicity states of the intermediate vector-bosons.

Spin/parity determination

3. $pp \rightarrow jjX$

X/jet distributions

Englert, Goncalves-Netto, KM, Plehn (2013)

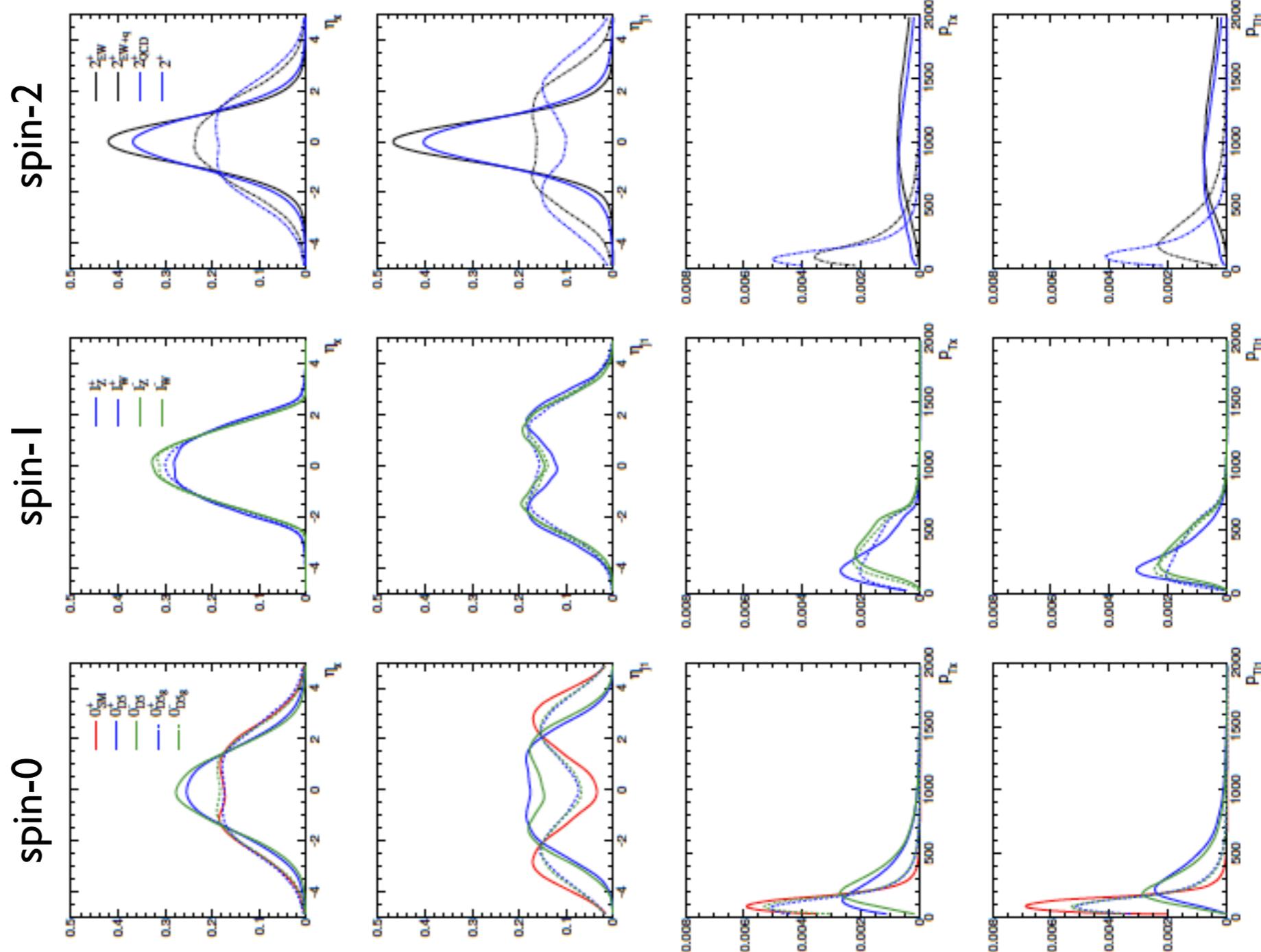
$$\sqrt{s} = 14 \text{ TeV}$$

$$p_{T_j} > 20 \text{ GeV}$$

$$\Delta R_{jj} > 0.6$$

$$|\eta_j| < 5$$

$$m_{jj} > 600 \text{ GeV}$$

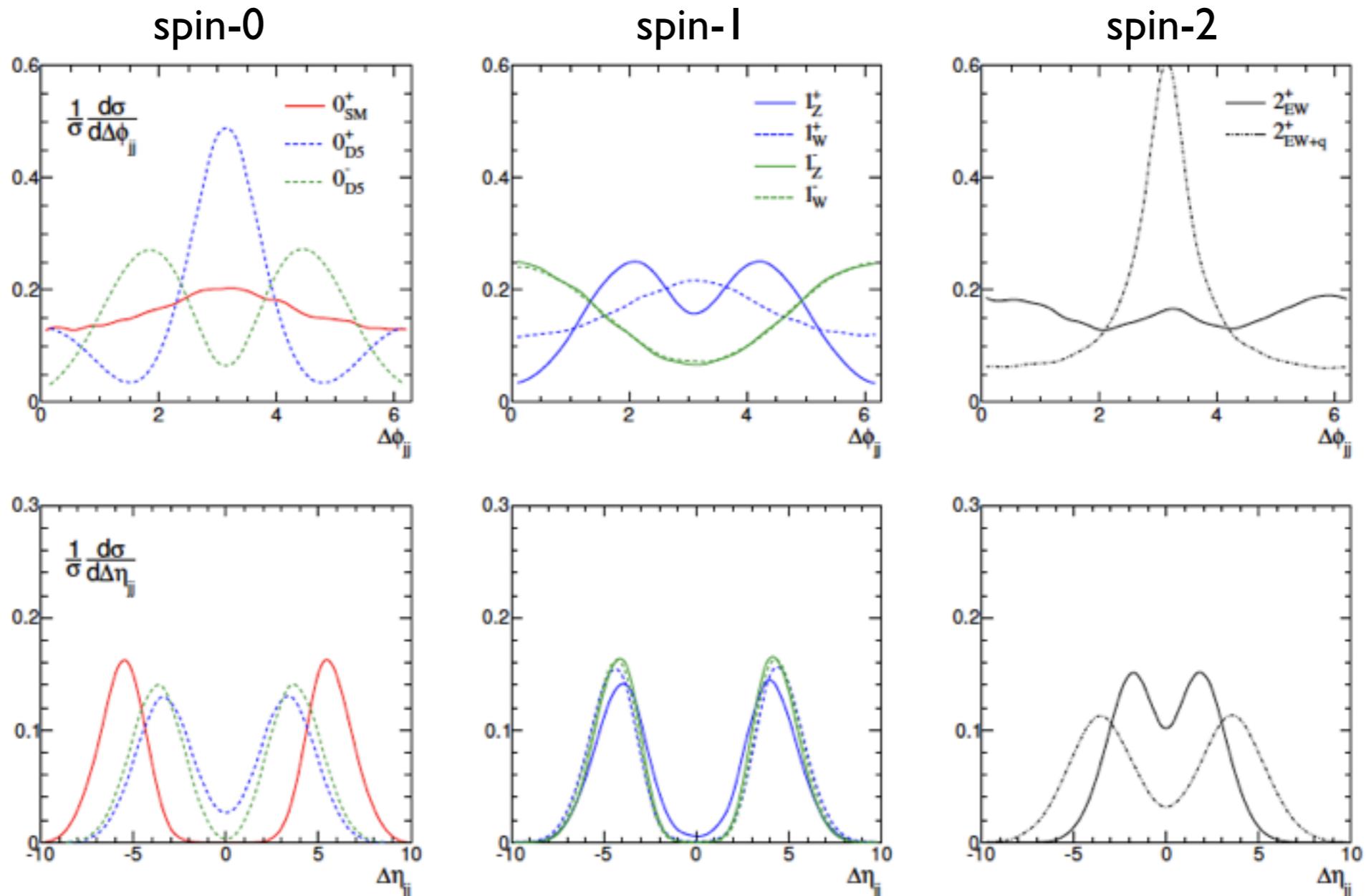


Spin/parity determination

3. $pp \rightarrow jjX$

di-jet correlations

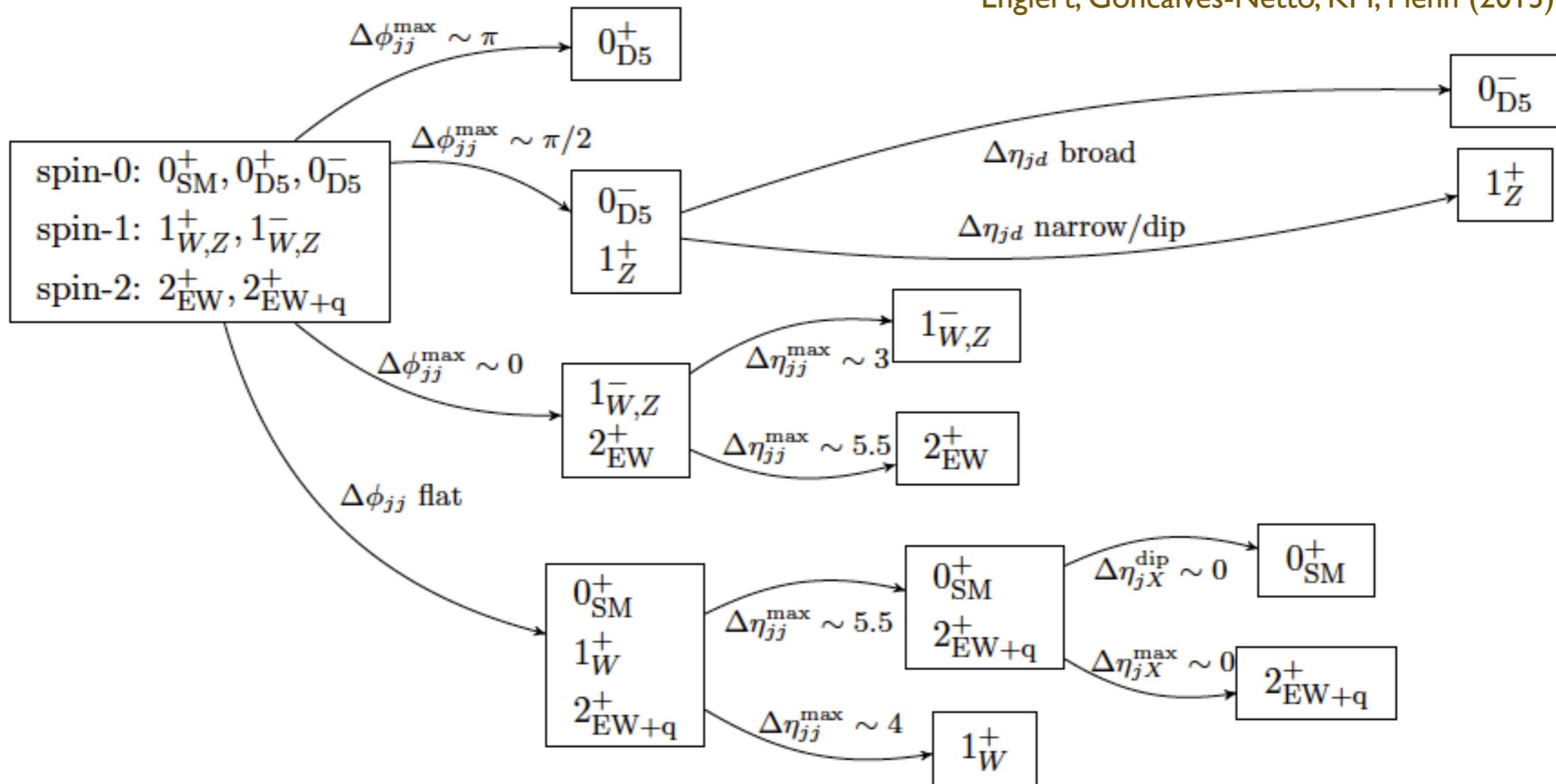
Englert, Goncalves-Netto, KM, Plehn (2013)



$\Delta\eta$ as well as $\Delta\Phi$ are the powerful observables.

Obs-by-obs based strategy in VBF

Englert, Goncalves-Netto, KM, Plehn (2013)

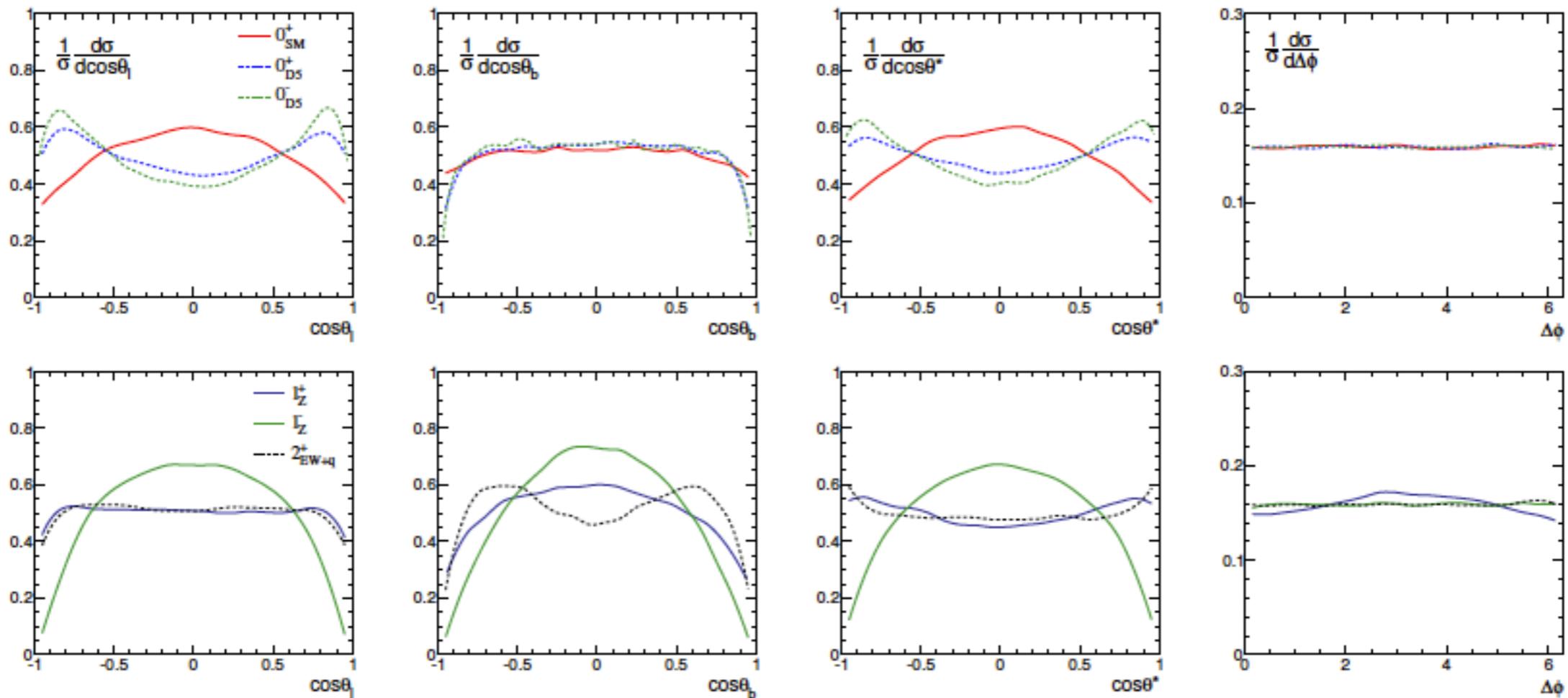


The di-jet correlations are the most decisive, in particular to separate the different scalar coupling structures.

Spin/parity determination

4. $pp \rightarrow ZX$

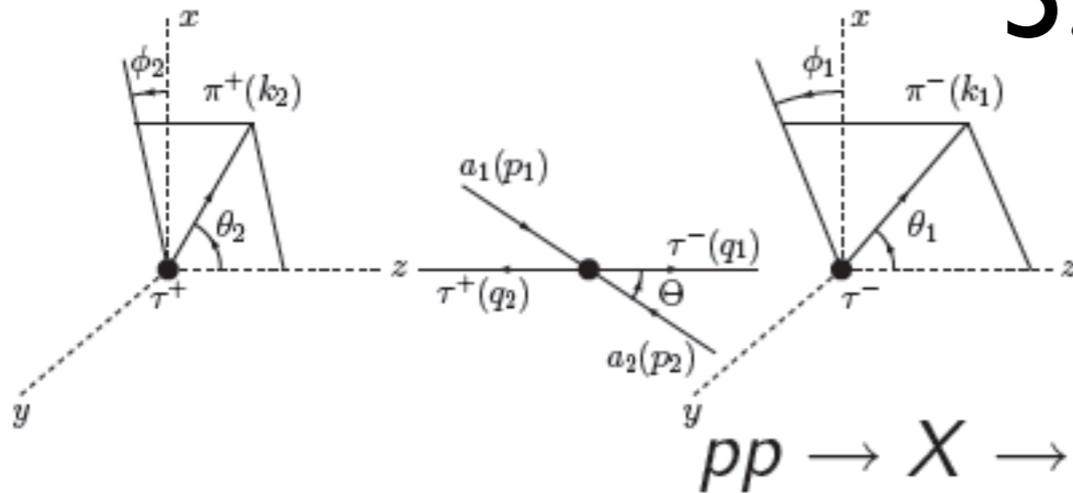
Englert, Goncalves-Netto, KM, Plehn (2013)



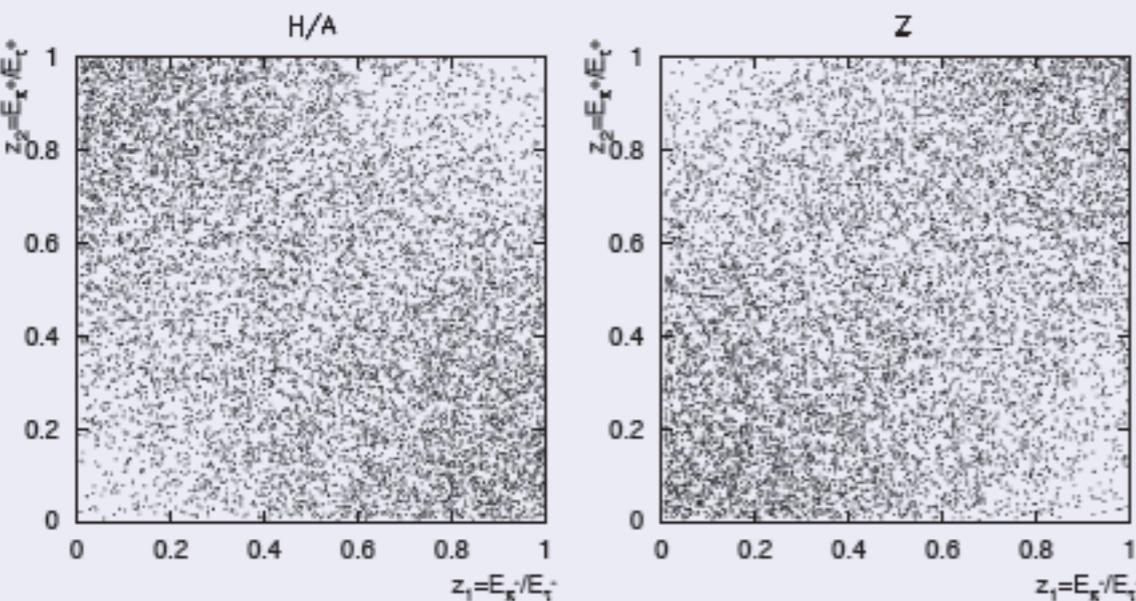
Spin/parity determination

5. $X \rightarrow \tau\tau$

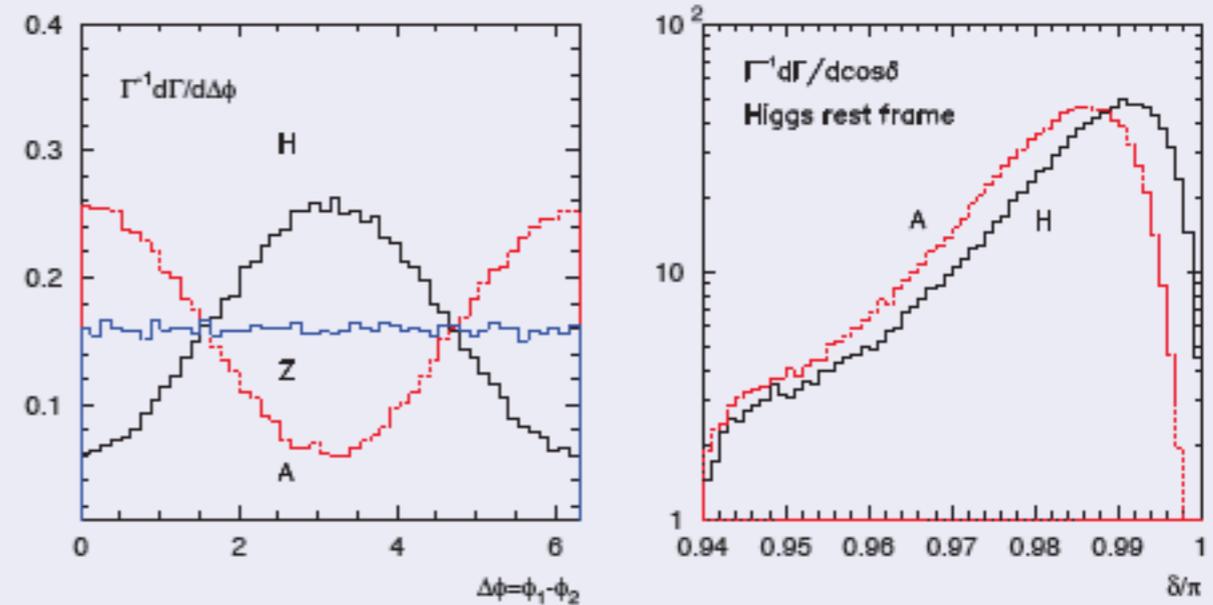
[Bullock, Hagiwara, Martin, NPB(1993)]
 [Krämer, Kühn, Stong, Zerwas, ZPC(1994)]
 [Pierzchala, Richter-Was, Was, Worek, APPB(2001,2002,...)]
 [Hagiwara, Li, KM, Nakamura, 1212.6247]



Longitudinal spin (helicity) effect



Transverse spin effect



$$d^2\Gamma/dz_1 dz_2 \sim 1 \mp z_1 z_2 \text{ for spin-0/1, } d\Gamma/d\Delta\phi \sim 1 \mp A \cos \Delta\phi \text{ for } 0^\pm$$

τ could be a spin/parity analyzer!

TauDecay

a library to simulate polarized tau decays via FeynRules/MadGraph5

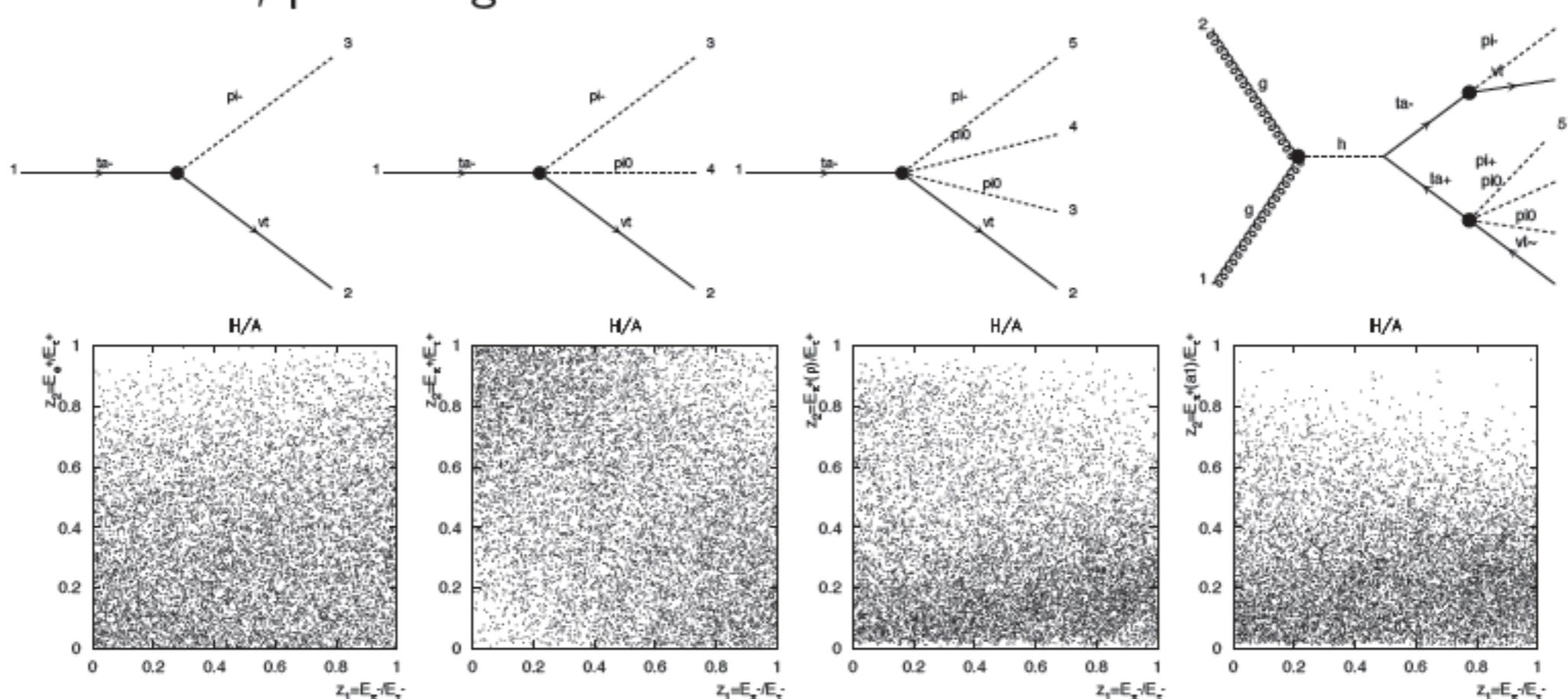
We implemented the effective Lagrangians

[Hagiwara, Li, KM, Nakamura, 1212.6247]

$$\mathcal{L}_\pi = \sqrt{2}G_F f_\pi \cos\theta_C \bar{\tau}\gamma^\mu P_L\nu_\tau \partial_\mu\pi^- + h.c.$$

$$\mathcal{L}_\rho = 2G_F \cos\theta_C F_\rho(Q^2) \bar{\tau}\gamma^\mu P_L\nu_\tau (\pi^0\partial_\mu\pi^- - \pi^-\partial_\mu\pi^0) + h.c.$$

into **FEYNRULES**, providing the model file for **MADGRAPH5**.



Full spin correlations for any kinds of new physics models can be generated for free.

Specific channel: X_0 into 4 charged leptons

- ▶ **generation of $X_0 \rightarrow \mu^+ \mu^- e^+ e^-$ events:** ME+matching approach (validated with aMC@NLO + parton shower), basic cuts on the leptons ($p_T > 7$ GeV, $|y| < 2.4$)
- ▶ 1M pseudo-experiments with **N=10 events** under each assumption (SM or HD)
- ▶ Discriminating variable for the **statistical test SM versus HD** is set to the **likelihood ratio**, built upon 1-dimension distribution or upon the matrix elements

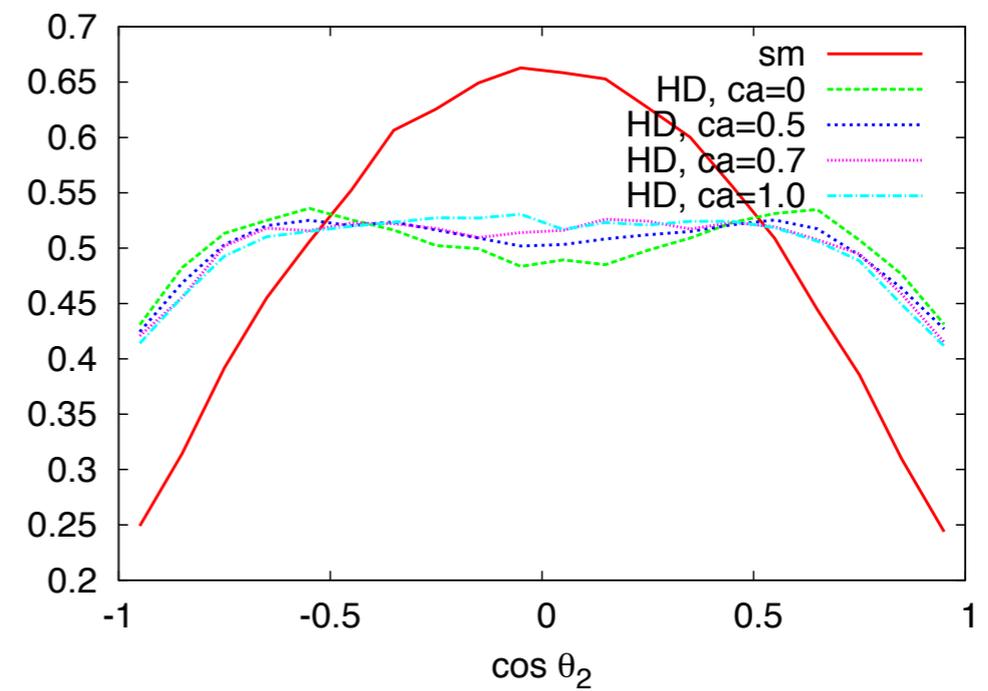
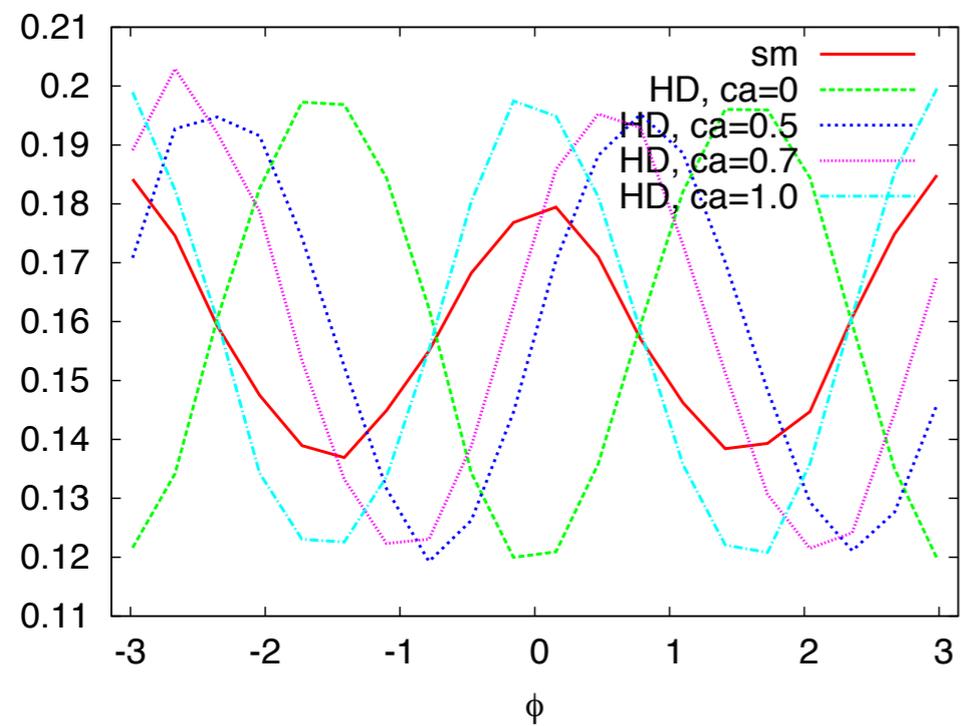
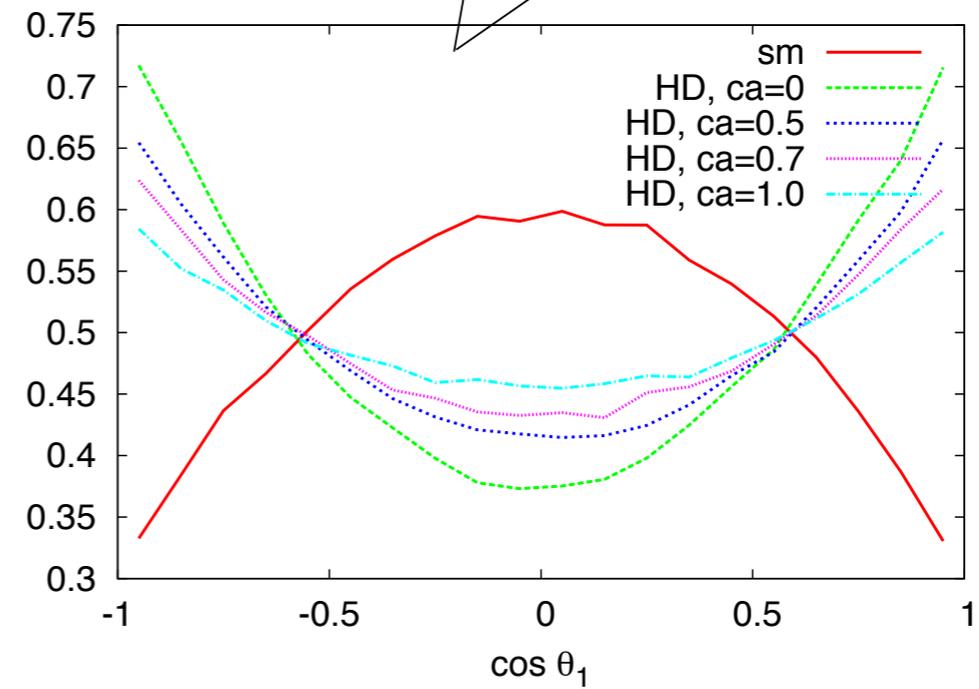
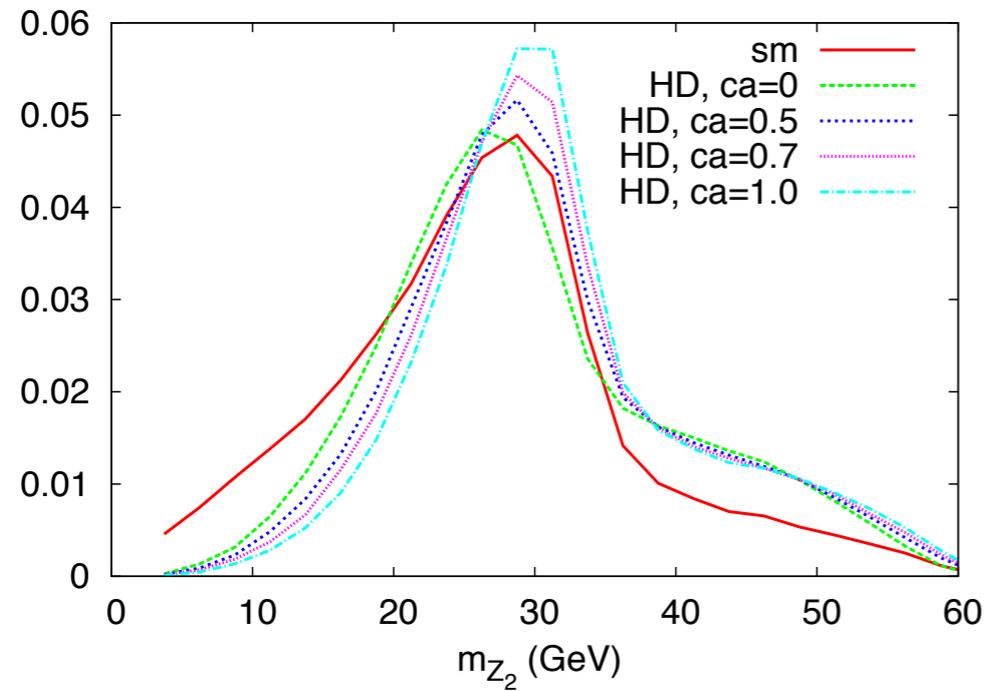
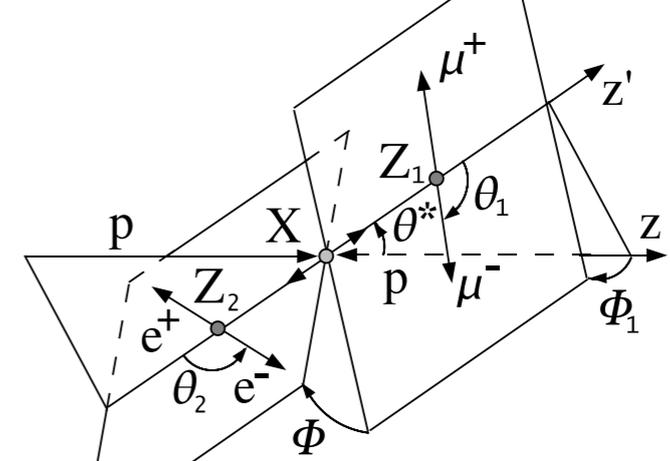
$$L_{\mathcal{O}} = \prod_i^N \frac{\sigma_{\text{HD}(c_\alpha)}^{-1} \frac{d\sigma_{\text{HD}(c_\alpha)}}{d\mathcal{O}}(\mathcal{O}_i)}{\sigma_{\text{SM}}^{-1} \frac{d\sigma_{\text{SM}}}{d\mathcal{O}}(\mathcal{O}_i)}.$$

likelihood ratio based
on 1-dim. distribution

$$L_{\text{MEM}} = \prod_i^N \frac{|M_{\text{HD}(c_\alpha)}(i)|^2}{|M_{\text{SM}}(i)|^2}$$

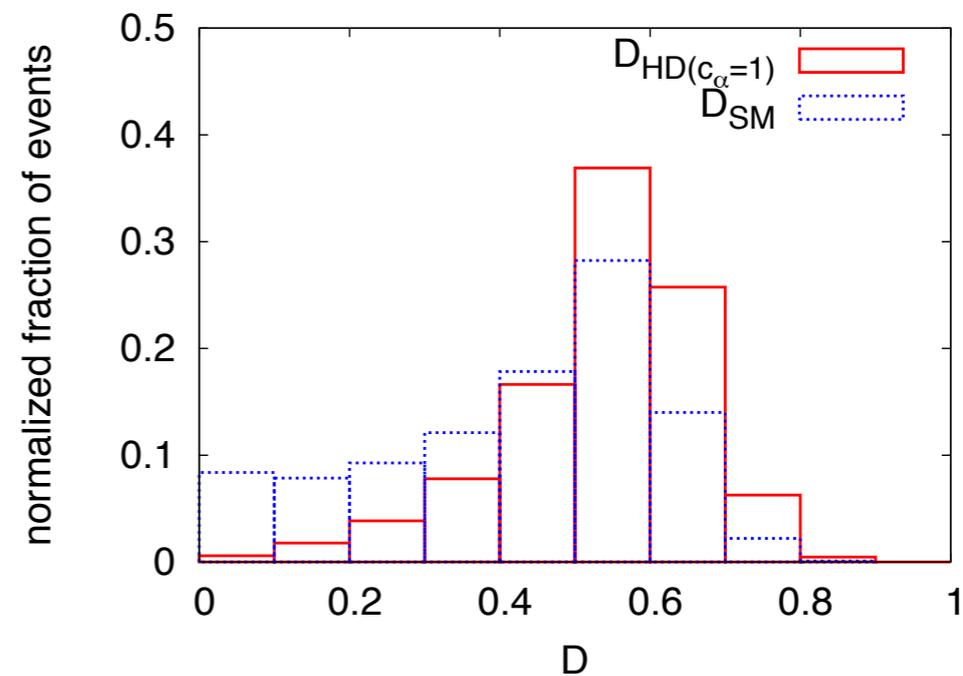
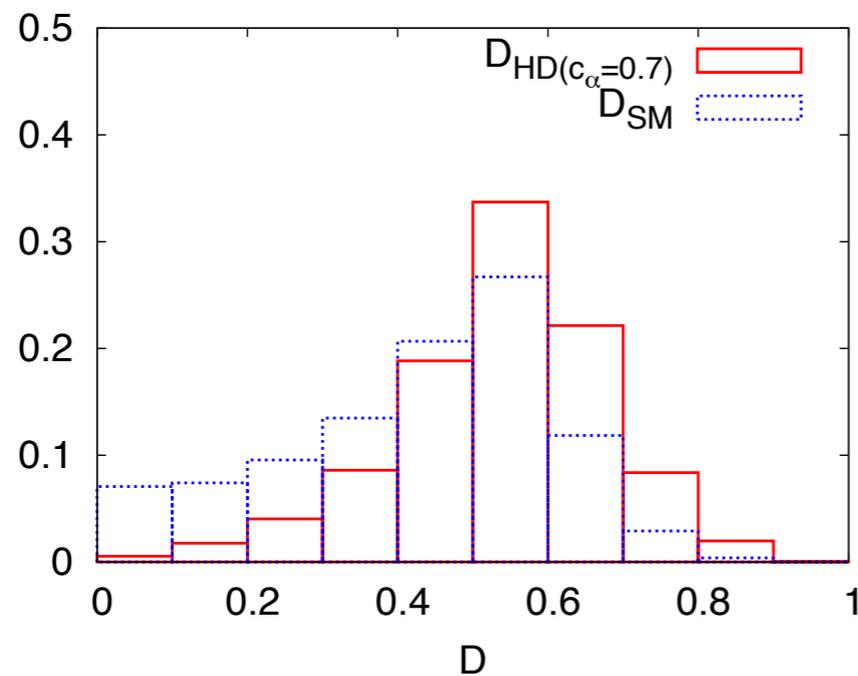
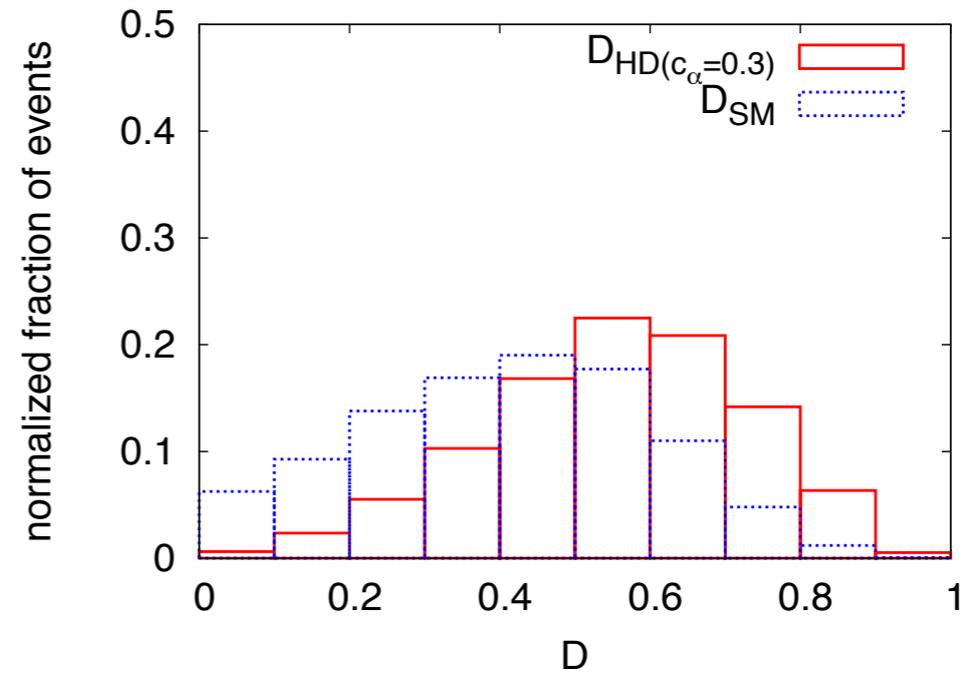
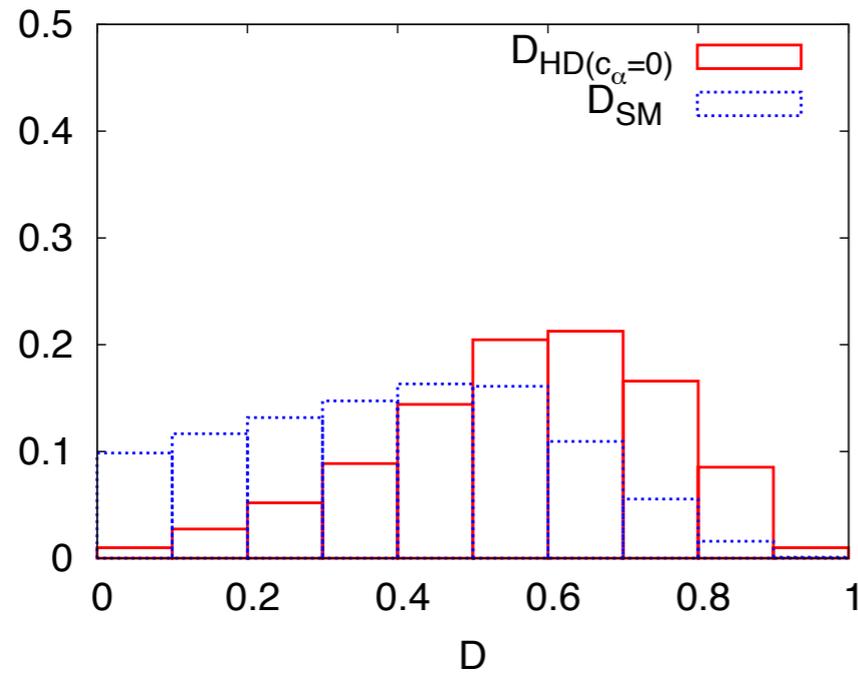
likelihood ratio based
on matrix elements

I-dimension distributions



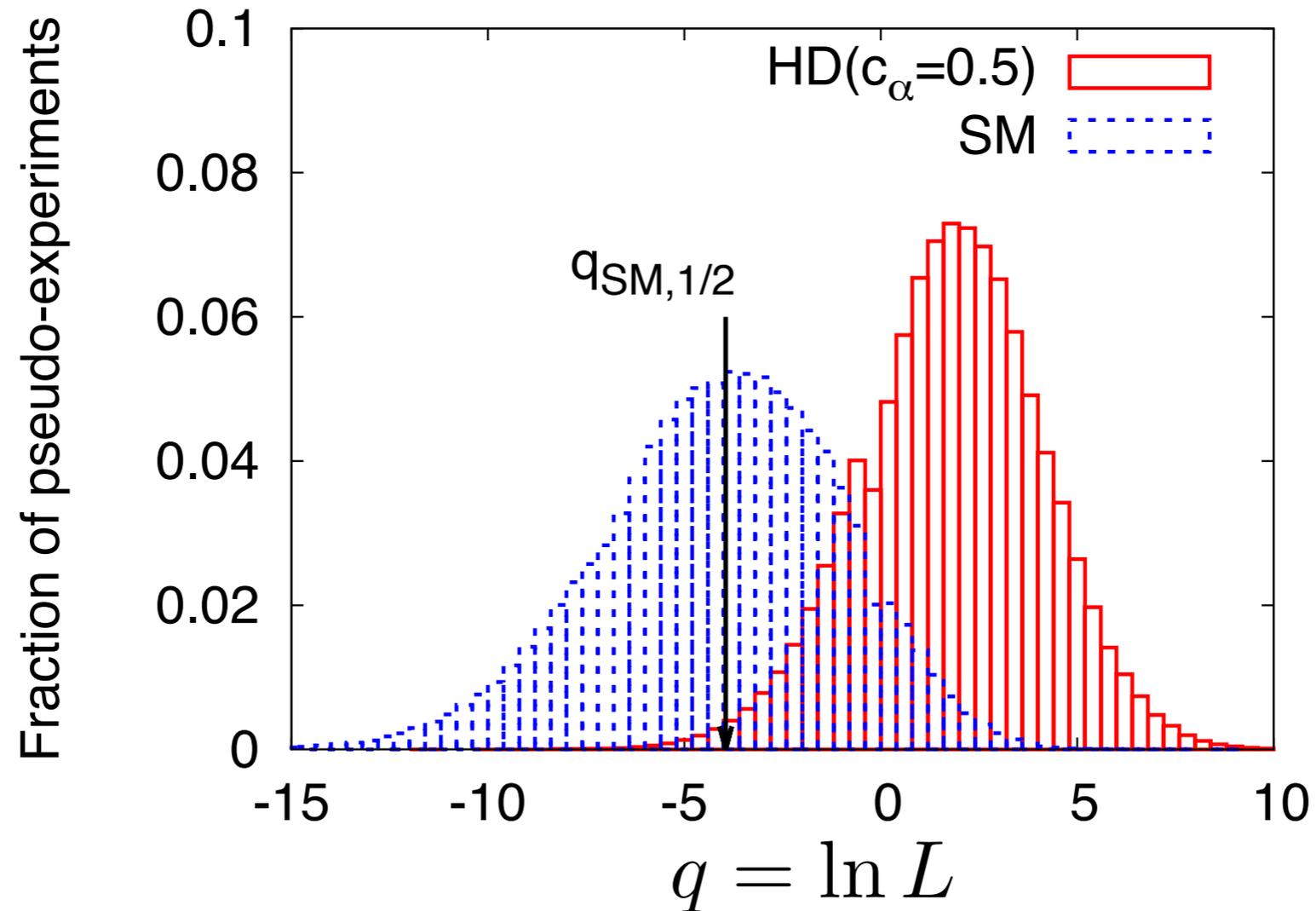
MEM discriminator

$$D(i) = \frac{|M_{HD}(c_\alpha)(i)|^2}{|M_{HD}(c_\alpha)(i)|^2 + |M_{SM}(i)|^2}$$



Distribution of SM and HD events with respect to the MEM-based discriminator D

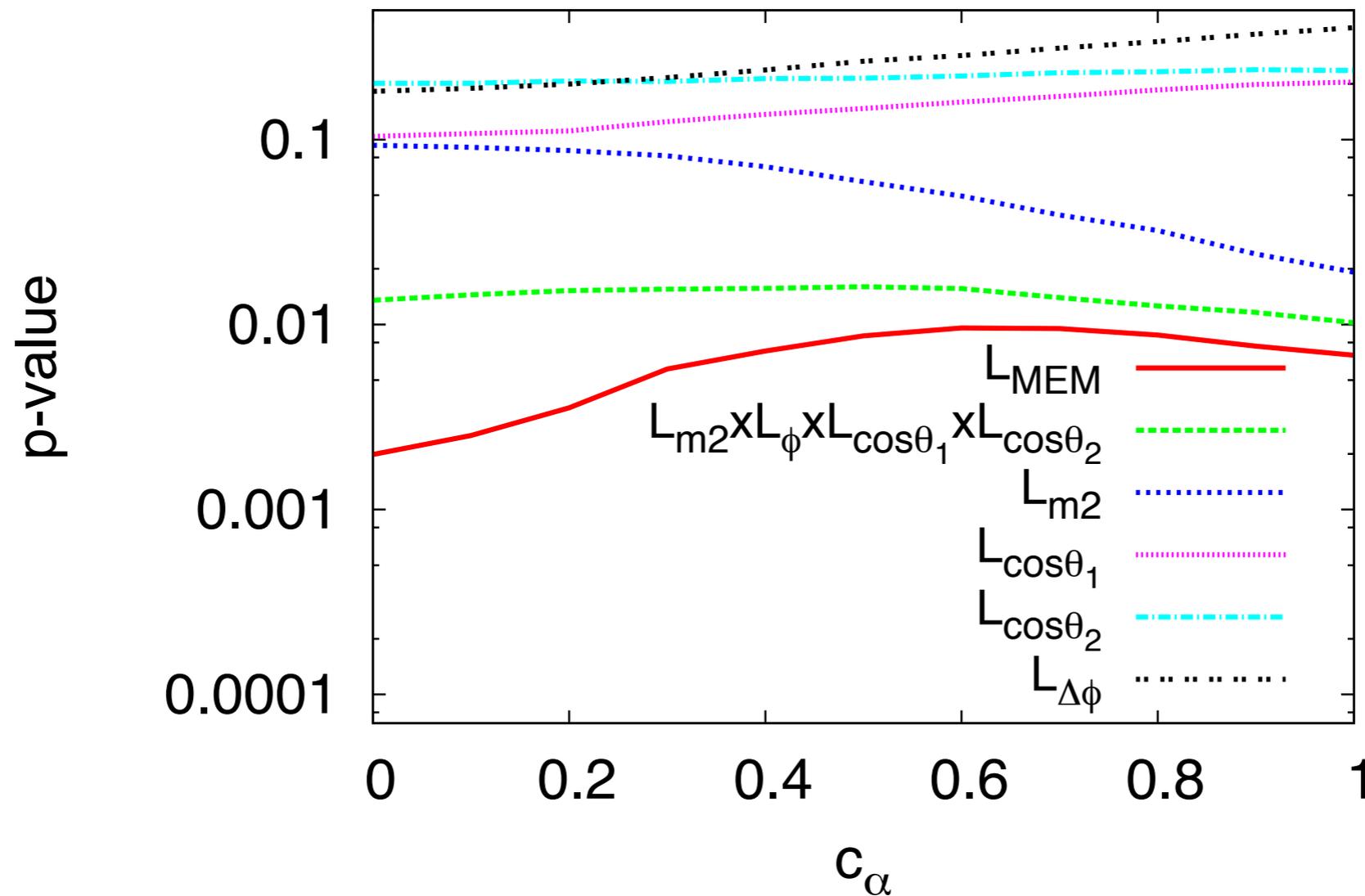
Significance



Significance estimated by calculating the **median** $q_{SM,1/2}$ of the SM distribution and by counting the **fraction of pseudo-experiments** in the HD distribution with $q < q_{SM,1/2}$

This fraction = expected **p-value** associated with the test of **rejecting hypothesis HD** if the **SM hypothesis is realized**.

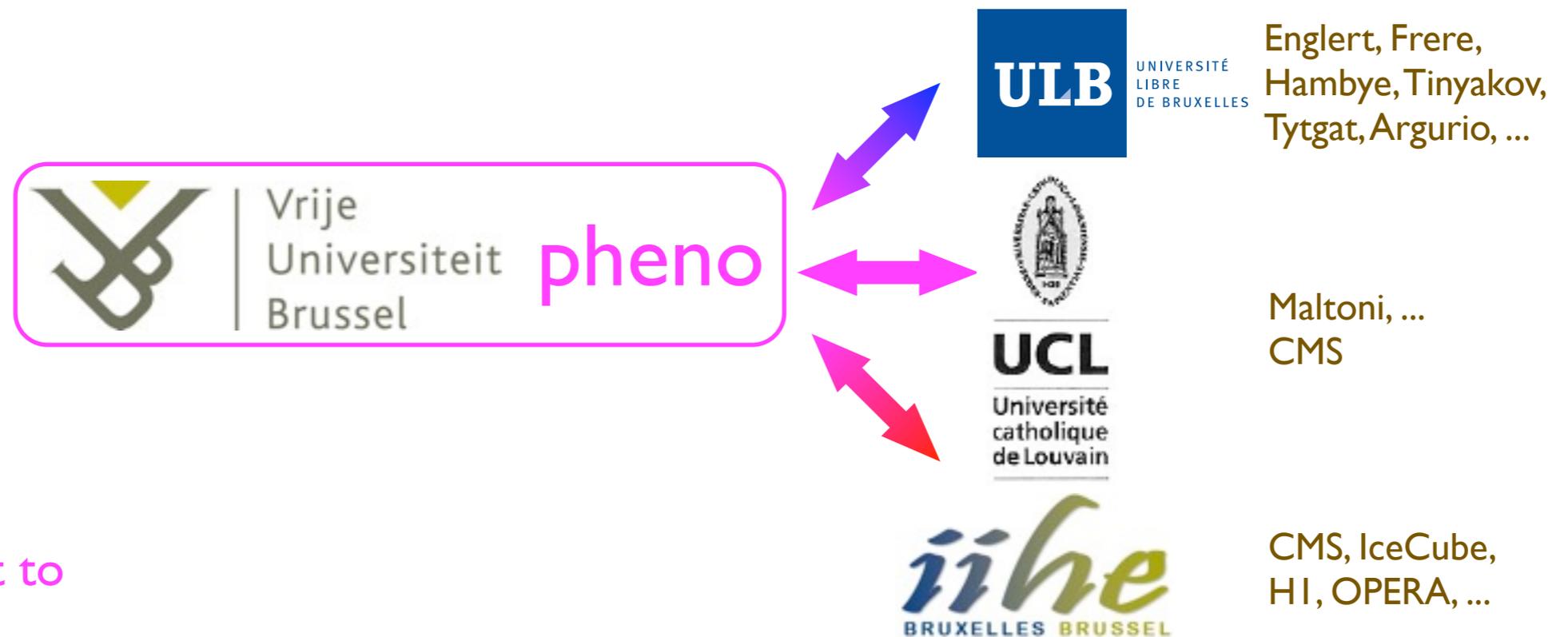
Significance



The **optimal significance** is reached with the **MEM-based** likelihood approach

Phenomenology group at the Vrije Universiteit Brussel

- Since October 2010, to make a chain between the theoretical and experimental groups at the VUB.



- Contact to

▶ <http://we.vub.ac.be/HEPVUB/>

▶ pheno@vub.ac.be, kentarou.mawatari@vub.ac.be

HEP@VUB

High Energy Physics Research Centre @ VUB

- The 5-year pheno project was rearranged into a larger framework in January 2013
 - Theory: Ben Craps, Alexander Sevrin (string/cosmology)
 - Collider physics: Jorgen D'Hondt, Freya Blekman, Steven Lowette (CMS)
 - Astor-particle physics: Catherine De Clercq, Nick Van Eindhoven (IceCube)
 - Phenomenology: Kentarou Mawatari
- **Pheno members**
 - Kentarou Mawatari - Project leader since 2010
 - Laura Lopez Honorez - PD since 2012
 - Priscila de Aquino - PD since 2012
 - Bettina Oexl - PhD since 2010
 - Karen De Causmaecker - PhD since 2011
 - Pantelis Tziveloglou (from Ecole Polytechnique, CPHT) - PD since 2013
 - Jonathan Lindgren (from Chalmers U. of Tech) - PhD since 2013