HIGGS COMPOSITENESS: CURRENT STATUS (AND FUTURE STRATEGIES)

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Outline

- Strong vs Weak EWSB
- Current Status of Higgs Compositeness:
 - 1. Higgs mass
 - 2. EW Precision Tests
 - 3. Impact of Searches for top partners
 - 4. Impact of data on Higgs couplings

Strong vs Weak EWSB







$$A \sim \frac{E^2}{v^2} (1 - c_V^2) - c_V^2 \frac{m_h^2}{v^2} \frac{s}{s - m_h^2}$$









$$A \sim \frac{E^2}{v^2} \left(1 - \sum_i c_{Vi}^2 \right) + \dots$$
$$= 0$$

Elementary Higgses: (more than one)

• $\delta c_{Vi} \sim O(1)$ possible

• sum rule:
$$\sum_i c_{Vi} =$$

1



coupling strength grows with energy and saturates at $\,g_* \lesssim 4\pi$



Analogy with $\pi\pi$ scattering in QCD: $h\leftrightarrow\sigma$

Q: why light and narrow ?

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A: the Higgs is itself a (pseudo) NG boson

Georgi & Kaplan, '80 Kaplan, Georgi, Dimopoulos

ex: $\frac{SO(5)}{SO(4)} \rightarrow 4$ NGBs transforming as a (2,2) of SO(4)~SU(2)_LxSU(2)_R

Agashe, RC, Pomarol NPB 719 (2005) 165

$$f^{2} \left| \partial_{\mu} e^{i\pi/f} \right|^{2} = (\partial \pi)^{2} + \frac{(\pi \partial \pi)^{2}}{f^{2}} + \frac{\pi^{2} (\pi \partial \pi)^{2}}{f^{4}} + \dots$$

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$$f^{2} \left| \partial_{\mu} e^{i\pi/f} \right|^{2} = |D_{\mu}H|^{2} + \frac{c_{H}}{2f^{2}} \left[\partial_{\mu}(H^{\dagger}H) \right]^{2} + \frac{c'_{H}}{2f^{4}} (H^{\dagger}H) \left[\partial_{\mu}(H^{\dagger}H) \right]^{2} + \dots$$

Giudice et al. JHEP 0706 (2007) 045

 $h \leftrightarrow \sigma$ Analogy with $\pi\pi$ scattering in QCD:

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1. $O(v^2/f^2)$ shifts in tree-level Higgs couplings. E

Ex:
$$c_V = 1 - c_H \left(\frac{v}{f}\right)^2 + \dots$$

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Giudice et al. JHEP 0706 (2007) 045

2. Scatterings involving the Higgs also grow with energy



D.B. Kaplan NPB 365 (1991) 259 ... RS with bulk fermions

 Hypothesis: each SM fermion couples to a composite fermionic operator with the same SU(3)_cxSU(2)_LxU(1)_Y quantum numbers

$$\mathcal{L} = \lambda_L \, \bar{q}_L O_R + \lambda_R \, \bar{u}_R O_L + h.c.$$

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Quark masses need two such couplings



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Similar to linear couplings of elementary gauge fields:

$$\mathcal{L} = g A_{\mu} J^{\mu}$$

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Partial compositeness

D.B. Kaplan NPB 365 (1991) 259 ... RS with bulk fermions

Fermionic operators can excite composite fermions at low energy:

 $\langle 0|O|\chi\rangle = \lambda f$

same as for a conserved current:

$$\langle 0|J_{\mu}|\rho\rangle = \epsilon_{\mu}^{r} f_{\rho} m_{\rho}$$

Partial compositeness

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vector-like composite fermion $\sqrt[]{0|0|\chi} = \lambda f$

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 $\langle 0 |$

Linear couplings imply mass mixings:

$$\mathcal{L} = \bar{\psi} \, i \partial \!\!\!/ \psi + \bar{\chi} (\, i \nabla \!\!\!/ - m_*) \chi + \lambda f \, \bar{\psi} U(\pi) \chi + h.c.$$

vector-like composite fermion

 λf

$$\begin{pmatrix} \psi \\ \chi \end{pmatrix} \to \begin{pmatrix} \cos \varphi & \sin \varphi \\ \sin \varphi & \cos \varphi \end{pmatrix} \begin{pmatrix} \psi \\ \chi \end{pmatrix} \qquad \qquad \tan \varphi = \frac{\lambda f}{m_*}$$

 φ parametrizes the degree of compositeness of the SM fermions

$$|\mathrm{SM}\rangle = \cos\varphi \,|\psi\rangle + \sin\varphi \,|\chi\rangle$$
$$|\mathrm{heavy}\rangle = -\sin\varphi \,|\psi\rangle + \cos\varphi \,|\chi\rangle$$



Can a 125GeV Higgs be composite ?

Structure of the Higgs Potential

$$V(h) = \frac{m_*^4}{g_*^2} \frac{N_c}{8\pi^2} \left[\lambda^2 \sum_i A_i(h/f) + \lambda^4 \sum_i B_i(h/f) + \dots \right]$$

$$h\equiv \sqrt{H^{\dagger}H}$$



$$\frac{SO(5)}{SO(4)} = S^4$$
 vacuum manifold is
the 4-sphere

 $A_i(x), B_i(x)$ SO(4) structures

→ trigonometric functions:
$$\sin^2(x)$$

 $\sin^4(x)$
:

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explicit breaking of Goldstone
symmetry (spurion couplings)
$$A_i(x), B_i(x) \qquad \text{SO(4) structures} \qquad \rightarrow \text{ trigonometric functions: } \sin^2(x) \qquad \sin^4(x) \qquad \vdots$$

$$\frac{SO(5)}{SO(4)} = S^4$$
 vacuum manifold is the 4-sphere



 $\frac{SO(5)}{SO(4)} = S^4 \qquad \begin{array}{c} \text{vacuum manifold is} \\ \text{the 4-sphere} \end{array}$

To get EWSB (0 < x ≪ π) at least two SO(4) structures are needed plus some tuning

Structure of the Higgs Potential

 $\frac{SO(5)}{SO(4)} = S^4 \qquad \begin{array}{c} \text{vacuum manifold is} \\ \text{the 4-sphere} \end{array}$

Potential is FINITE - loop integral fully

$$FT = O\left(\frac{v^2}{f^2}\right)$$



$$\begin{split} t_{L,R} & V(h) \simeq \frac{m_*^4}{g_*^2} \frac{N_c}{8\pi^2} \lambda_{L,R}^2 A\left(\frac{h}{f}\right) \\ & &$$







📫 Talk by A. Parolini

■ If EWSB is triggered at $O(\lambda^2)$ + t_R fully composite

 t_R

 $y_t \sim \lambda_L$

If EWSB is triggered at $O(\lambda^2) + t_R$ fully composite



$$\underbrace{t_L} \quad t_R \quad y_t \sim \lambda_L$$

$$m_h^2 \sim \frac{N_c}{4\pi^2} g_*^2 y_t^2 v^2 = \left(175 \,\text{GeV} \times \left(\frac{g_*}{3}\right)\right)^2$$

m_H=125GeV implies top partners are naturally

- not too strongly coupled, hence
- not too heavy

Matsedonskyi, Panico, Wulzer JHEP 1301 (2013) 164 Redi, Tesi JHEP 1210 (2012) 166 Marzocca, Serone, Shu JHEP 1208 (2012) 013 Pomarol, Riva JHEP 1208 (2012) 135 Panico, Redi, Tesi, Wulzer JHEP 1303 (2013) 051 De Simone et al. JHEP 1304 (2013) 004 If EWSB is triggered at $O(\lambda^2) + t_R$ fully composite





 $m_h^2 \sim \frac{N_c}{4\pi^2} g_*^2 y_t^2 v^2 = \left(175 \,\text{GeV} \times \left(\frac{g_*}{3}\right)\right)^2$

 $\lambda_L \simeq y_t$

$$FT \sim \frac{v^2}{f^2} \sim \frac{m_h^2}{m_*^2} \frac{4\pi^2}{N_c y_t^2} = \left(\frac{525 \,\text{GeV}}{m_*}\right)^2$$

- m_H=125GeV implies top partners are naturally
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 $V(h) \simeq \frac{m_*^4}{g_*^2} \frac{N_c}{8\pi^2} \left[\lambda_{L,R}^2 A\left(\frac{h}{f}\right) + \frac{\lambda_L^2 \lambda_R^2}{g_*^2} B\left(\frac{h}{f}\right) \right]$



extra tuning required to suppress $O(\lambda^2)$ terms down to $O(\lambda^4)$

$$V(h) \simeq \frac{m_*^4}{g_*^2} \frac{N_c}{8\pi^2} \left[\lambda_{L,R}^2 A\left(\frac{h}{f}\right) + \frac{\lambda_L^2 \lambda_R^2}{g_*^2} B\left(\frac{h}{f}\right) \right]$$



$$m_h^2 \sim \frac{N_c}{4\pi^2} \frac{m_*^2}{f^2} \frac{\lambda_L^2 \lambda_R^2}{g_*^2} v^2 \sim \frac{N_c}{4\pi^2} g_*^2 y_t^2 v^2 = \left(175 \,\text{GeV} \times \left(\frac{g_*}{3}\right)\right)^2$$



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$$FT \sim \frac{v^2}{f^2} \times \frac{\lambda^2}{g_*^2} \simeq \left(\frac{525 \,\mathrm{GeV}}{m_*}\right)^2 \times \frac{y_t}{g_*}$$

m_H automatically lighter but larger tuning to get EWSB

Panico, Redi, Tesi, Wulzer JHEP 1303 (2013) 051

EW Precision Tests


fit from: GFitter coll. Eur. Phys. J. C 72 (2012) 2205

$$\Delta \epsilon_1 = -\frac{3}{16\pi} \frac{\alpha_{em}}{\cos^2 \theta_W} \log \frac{\Lambda^2}{m_Z^2}$$
$$\Delta \epsilon_3 = +\frac{1}{12\pi} \frac{\alpha_{em}}{4 \sin^2 \theta_W} \log \frac{\Lambda^2}{m_Z^2}$$





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Ciuchini, Franco, Silvestrini, Mishima, arXiv:1306.4644



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Ciuchini, Franco, Silvestrini, Mishima, arXiv:1306.4644

See talk by S. Mishima on Thursday





Contribution from resonances REQUIRED to relax the bound



Ciuchini, Franco, Silvestrini, Mishima, arXiv:1306.4644

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S parameter
$$\hat{S} = \hat{S}_{IR} + \hat{S}_{UV}$$



$$\hat{S}_{IR} \sim \frac{v^2}{f^2} \frac{g^2}{16\pi^2} \log\left(\frac{\Lambda}{m_Z}\right) \qquad \qquad \hat{S}_{UV} \sim g^2 \frac{v^2}{f^2} \left[\frac{1}{g_*^2} + N_c N_F \frac{1}{16\pi^2} \log\left(\frac{\Lambda}{m_*}\right) + \dots\right]$$

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 $\hat{S}_{IR} \sim$



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tree-level (rho)

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$$\uparrow$$
tree-level (rho)
$$1-\text{loop (fermions)}$$

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1-loop contribution from fermions can be large (!)

Golden, Randall, NPB 361 (1991) 3 Barbieri, Isidori, Pappadopulo, JHEP 0902 (2009) 029 Grojean, Matsedonskyi, Panico, arXiv:1306.4655 Azatov, RC , Di Iura, Galloway, arXiv:1308.2676



Best seen using a dispertion relation:

Orgogozo and Rychkov, JHEP 1306 (2013) 014

$$\hat{S}_{UV} = \frac{g^2}{4}\sin^2\theta \int \frac{ds}{s} \left[\rho_{LL}(s) + \rho_{RR}(s) - 2\rho_{BB}(s)\right]$$

$$i \int d^4x \, e^{iq \cdot (x-y)} \langle 0|T(J_\mu(x)J_\nu(y))|0\rangle = (q^2\eta_{\mu\nu} - q_\mu q_\nu)\Pi(q^2) \qquad \qquad \rho(s) = \frac{1}{\pi} \mathrm{Im}(\Pi(s))$$



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$$\hat{S}_{UV} = \frac{g^2}{4}\sin^2\theta \int \frac{ds}{s} \left[\rho_{LL}(s) + \rho_{RR}(s) - 2\rho_{BB}(s)\right] - \frac{1}{2}\rho_{BB}(s)$$

negative contribution from spectral function of broken SO(5)/SO(4) currents

$$i \int d^4x \, e^{iq \cdot (x-y)} \langle 0|T(J_{\mu}(x)J_{\nu}(y))|0\rangle = (q^2 \eta_{\mu\nu} - q_{\mu}q_{\nu})\Pi(q^2)$$

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Example: [Azatov, RC, Di lura, Galloway, arXiv:1308.2676]

$$\psi_5 = (1,1) + (2,2) \qquad \qquad \mathcal{L} = \bar{\psi}_1 (i \not \!\!\!D - m_1) \psi_1 + \bar{\psi}_4 (i \not \!\!\!\!\nabla - m_4) \psi_4 - \zeta \, \bar{\psi}_4 \gamma^{\mu} d_{\mu} \psi_1 + h.c.$$





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Orgogozo and Rychkov, JHEP 1306 (2013) 014

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A+





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Orgogozo and Rychkov, JHEP 1306 (2013) 014

$$\hat{S}_{UV} = \frac{g^2}{4} \sin^2\theta \int \frac{ds}{s} \left[\rho_{LL}(s) + \rho_{RR}(s) - 2\rho_{BB}(s) \right] - \frac{\text{negative constrained on spectral function}}{\text{SO(5)/SO(1)}}$$

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$$\hat{S}_{UV} = \frac{8}{3} \frac{m_W^2}{16\pi^2 f^2} N_c N_F \left(1 - |\zeta|^2\right) \log\left(\frac{\Lambda^2}{m_{(2,2)}^2}\right) + \text{finite terms}$$

SO(5)/SO(4) model:

 $\psi_5 = (1,1)_{2/3} + (2,2)_{2/3}$

$$\psi_{10} = (2,2)_{-1/3} + (1,3)_{-1/3} + (3,1)_{-1/3}$$



from: Azatov, RC, Di lura, Galloway arXiv:1308.2676

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Ex: for $f = 800 \,\text{GeV}$ $g_{\rho} = 3$ $\Delta S_{\rho} \simeq 0.13$ $\Delta S_{\psi} \simeq 0.8 \times (1 - |\zeta|^2)$

strong sensitivity on ζ

tuning $\sim 10\%$ required to go back into the exp. ellipse

T parameter $\hat{T} = \hat{T}_{IR} + \hat{T}_{UV}$





$$\hat{T}_{IR} \sim -\frac{v^2}{f^2} \frac{g^2}{16\pi^2} \log\left(\frac{\Lambda}{m_Z}\right) \qquad \qquad \hat{T}_{UV} \sim \frac{v^2}{f^2} \left[\frac{g^2}{16\pi^2} \log\left(\frac{\Lambda}{m_\rho}\right) + N_c \frac{\lambda_L^2}{16\pi^2} \frac{\lambda_L^2}{g_*^2} + \dots\right]$$

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$$\hat{T}_{IR} \sim -\frac{v^2}{f^2} \frac{g^2}{16\pi^2} \log\left(\frac{\Lambda}{m_Z}\right) \qquad \qquad \hat{T}_{UV} \sim \frac{v^2}{f^2} \left[\frac{g^2}{16\pi^2} \log\left(\frac{\Lambda}{m_\rho}\right) + N_c \frac{\lambda_L^2}{16\pi^2} \frac{\lambda_L^2}{g_*^2} + \dots\right]$$

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$$1\text{-loop (rho)}$$

$$1\text{-loop (fermions)}$$

- Custodial symmetry implies:
 - 1. No \hat{T} at tree-level
 - 2. fermion correction is *finite* and starts at $O(\lambda_L^4)$ (only top partners contribute)



$\Delta \hat{T} > 0$ possible though not fully generic

Example: model with $\psi_4 = (2,2)_{2/3} + t_R$ composite

 $\mathcal{L} = \bar{q}_L i \not\!\!D q_L + \bar{t}_R i \not\!\!D t_R + \bar{\psi}_4 (i \not\!\!\nabla - m_4) \psi_4$ $+ i \zeta \, \bar{\psi}_4^i \gamma^\mu d^i_\mu t_R + y_{Lt} f \, \bar{q}_L U(\pi) t_R + y_{L4} f \, \bar{q}_L U(\pi) \psi_4 + h.c.$

Carena, et al. NPB 759 (2006) 202; PRD 76 (2007) 035006 Barbieri et al. PRD 76 (2007) 115008 Lodone JHEP 0812 (2008) 029 Pomarol, Serra, PRD 78 (2008) 074026 Gillioz PRD 80 (2009) 055003 : Grojean, Matsedonskyi, Panico arXiv:1306.4655



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Searches of top partners

Typical spectrum of top partners



Typical spectrum of top partners



Two main production modes:







EW single production

 $g \mod$

 $\overline{t}/\overline{b}$

Typical spectrum of top partners



Two main production modes:





from: De Simone, Matsedonskyi, Rattazzi, Wulzer JHEP 1304 (2013) 004



EW single production





- Current experimental status in a nutshell
 - 1. Almost all decays looked for
 - 2. Analyses optimized on pair production



0

0

0

0

0

28





CMS B2G-12-015 CMS B2G-12-012



- Current experimental status in a nutshell 0
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Limits in the 700-800 GeV range



CMS B2G-12-015 CMS B2G-12-012



0

0

0

0

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28





Once recast on (simplified) theory space exp. bounds already exclude a big portion of the natural region

De Simone et al. JHEP 1304 (2013) 004

Blue region:

$$y_{L4} = 3 \ (m_B \gg m_{X_{5/3}})$$

Green region:

$$y_{L4} = 0.3 \ (m_B \gtrsim m_{X_{5/3}})$$

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Stronger sensitivity from optimizing exp. analyses to include single production Once recast on (simplified) theory space exp. bounds already exclude a big portion of the natural region

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Stronger sensitivity from optimizing exp. analyses to include single production

Т 1555 767 В 767 1627 $X_{5/3}$ 638 1025 $X_{2/3}$ 638 1025 \tilde{T} 437 524 M [GeV] 1000 500 1500

limits for $\xi = 0.1, \ \zeta = 1, \ y_{L4} = 1$

Multiplicity of states, connection among masses and inclusion of single production amplify limits on individual particles
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Stronger sensitivity from optimizing exp. analyses to include single production

Multiplicity of states, connection among masses and inclusion of single production amplify limits on individual particles

1TeV masses typically excluded

LHC has already eaten up a big part of the natural region

 $y_{L4} = 0.3 \ (m_B \gtrsim m_{X_{5/3}})$

---- limits for
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Higgs couplings

$$c_V = 1 + F\left(\frac{v^2}{f^2}\right) + O\left(\frac{v^2}{f^2} \frac{g_{\mathcal{G}}^2}{g_*^2}\right)$$

$$c_{\psi} = 1 + F_{\psi}\left(\frac{v^2}{f^2}, \frac{m_i}{m_j}\right) + O\left(\frac{v^2}{f^2} \frac{\lambda^2}{g_*^2}\right)$$

$$O(v^2/f^2) \text{ from Higgs nl}{\sigma}$$

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$$\psi_L \qquad \psi_R + \psi_L \qquad \psi_R + \cdots$$

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$$c_{V} = 1 + F\left(\frac{v^{2}}{f^{2}}\right) + O\left(\frac{v^{2}}{f^{2}}\frac{g_{\mathcal{G}}^{2}}{g_{*}^{2}}\right) \leftarrow \text{ from heavy} \text{ resonances} \qquad h \qquad h$$
in the simplest models
$$c_{\psi} = 1 + F_{\psi}\left(\frac{v^{2}}{f^{2}}\right) + O\left(\frac{v^{2}}{f^{2}}\frac{\lambda^{2}}{g_{*}^{2}}\right)$$

$$\psi_{L} \qquad \psi_{R} + \psi_{L} \qquad \psi_{R} + \cdots$$



$$\xi \equiv \frac{v^2}{f^2}$$

MCHM4:
$$c_V = c_\psi = \sqrt{1-\xi}$$

MCHM5:

Agashe, RC, Pomarol, NPB 719 (2005) 165

RC, DaRold, Pomarol, PRD 75 (2007) 055014 Carena, Ponton, Santiago, Wagner, PRD 76 (2007) 035006



 $c_V = \sqrt{1-\xi} \qquad c_\psi = \frac{1-2\xi}{\sqrt{1-\xi}}$

Red points at $\xi \equiv (v/f)^2 = 0.2, \ 0.5, \ 0.8$





 Modifications to loop-level couplings ggh, yyh suppressed due to the Goldstone symmetry



Effective operators violate the Higgs shift symmetry:

$$\begin{array}{c} g \\ g \\ g \\ \hline g \\ \hline 0 0 0 0 \end{array} \qquad h \qquad G_{\mu\nu}^2 H^{\dagger} H \end{array}$$

$$H^i \to H^i + \zeta^i$$

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Azatov, RC , Di lura, Galloway, arXiv:1308.2676

$$\frac{\delta\Gamma(Z\gamma)}{\Gamma_{SM}(Z\gamma)} = O\left(\frac{v^2}{f^2}\right) + O\left(\frac{g_*^2v^2}{m_*^2}\right)$$

Relevant operator is $O_{HW} - O_{HB}$

 $O_{HB} = (D^{\mu}H)^{\dagger} (D^{\nu}H) B_{\mu\nu}$ $O_{HW} = (D^{\mu}H)^{\dagger} \sigma^{i} (D^{\nu}H) W^{i}_{\mu\nu}$



- 1. Invariant under Higgs shift symmetry
- 2. Odd under LR exchange

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$$A(h \to Z\gamma) = A_{SM} \times F(\xi) + \delta A$$

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shift of tree-level
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Higgs mass term (FT)

Finite in CH $m_H^2 \sim \frac{3\lambda^2}{8\pi^2} m_*^2$ Log divergent in SUSY $m_{H_u}^2 \sim \frac{3y_t^2}{4\pi^2} m_{\tilde{t}}^2 \log \frac{\Lambda^2}{m_{\tilde{t}}^2}$

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Higgs quartic coupling

CH: tends to be too large
$$\lambda_4 \sim \frac{3}{8\pi^2} g_*^3 y_t$$

SUSY: tends to be too small $\lambda_4 \simeq \frac{g^2 + g'^2}{4} + \frac{3y_t^4}{8\pi^2} \log \frac{m_t^2}{m_t^2}$

Bounds on "top partners" from direct searches

- SUSY: stops $\gtrsim 700 \, {\rm GeV}$
- CH: heavy tops/bottoms $\gtrsim 1 \,\mathrm{TeV}$

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- Largest effects in Higgs sector expected in:
 - SUSY: coupling to bottom (c_b); $\gamma\gamma$ and gg rates; production of Heavy Higgses
 - CH: tree-level couplings; $h \rightarrow Z\gamma$ rate; double Higgs production ($gg \rightarrow hh$)