Extended no-scale and ${\alpha'}^2$ corrections to the IIB action

[arXiv: 1306.1237]

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<u>Outline</u>:





Motivation:

String theory as a unifying framework for GR and SM Extended spacetimes: D=10,11,12



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Realistic phenomenology requires moduli stabilisation



Leading Order

Theory determined by Kahler potential and superpotential $K_{tree} = K(T) + K(S) + K(U)$ $W_{tree} = W(S, U)$

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[GKP:2001]

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Kahler moduli are flat directions



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T-moduli <u>lifted</u> by higher order corrections to K and W Assume



$\delta K = 0 \qquad \delta W \sim e^{-T}$

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[KKLT:2003]

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$$V_{KKLT} \sim \frac{aA^2 e^{-2a\tau}}{\tau^2} + \frac{aA e^{-a\tau} W_0}{\tau^2} + \frac{6a^2 A^2 e^{-2a\tau}}{\tau}$$

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DESY

[KKLT:2003]



Large Volume Scenario

AdS minimum with broken SUSY at

 $\langle \tau_s \rangle \propto rac{1}{g_s}$



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 $\langle \mathcal{V} \rangle \propto e^{1/g_s}$



Large Volume Scenario





Large Volume Scenario



How will other terms in K affect moduli stabilisation?



[von Gersdorff&Hebecker,2005] [Berg,Haack&Kors,2005] [Cicoli,Conlon&Quevedo,2007/08]

 $K = K_0 + \delta K$

$$\delta V_{(1,0)} = -\frac{|W_0|^2}{\mathcal{V}^2} \left\{ 2\tau_b \delta K_b + \tau_m \delta K_{mn} \tau_n \right\}$$



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 $t^a \frac{\partial \delta K}{\partial t^a} = n \delta K,$



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String loop corrections

[Grimm,Savelli&Weissenbacher:2013]

Quantum correction to the volume at order ${\alpha'}^2$

 $\tilde{\mathcal{V}} = \mathcal{V} - \frac{5}{64} \mathcal{V}_{D7 \cap O7}$



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$$\delta K \sim \frac{\delta \mathcal{V}}{\mathcal{V}} \sim \frac{1}{\tau} \sim \frac{1}{t^2}$$



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Effect on moduli stabilisation?





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$$\delta V = -\frac{675k^4}{64}\frac{W_0^2}{\tau^5} + 45k^2\frac{A^2ae^{-2a\tau}}{\tau^3} + 45k^2\frac{W_0Aae^{-a\tau}}{\tau^3} + 15k^2\frac{A^2a^2e^{-2a\tau}}{2\tau^2}$$





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$$\Delta = \langle \delta V / V_{KKLT} \rangle$$



























KKLT stability







































Example: $\mathbb{CP}_{11114}^4[8]$ [Grimm,Savelli&Weissenbacher:2013] $K = -\log\left[\frac{2}{9}\tau\left(\tau - \frac{15}{8}k^2\right)^2\right] \qquad k = 4$

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Δ	$\langle \tau \rangle$	W_0
1	60	-10^{-3}
1/10	600	-10^{-25}
1/100	6000	-10^{-258}

LVS stability

LVS on $\mathbb{CP}^4_{11169}[18]$:

 $\mathcal{V} = \frac{1}{18}\tau_1^{3/2} - \frac{1}{9}\sqrt{2}\tau_2^{3/2}$

 $\mathcal{V}_{O7\cap D7} = \frac{135}{8}\sqrt{\tau_1}$

New terms in V:

$$\delta V_{(1,0)} + \delta V_{(2,0)} = -\frac{18225}{16} \left(\frac{3}{2}\right)^{1/3} \frac{W_0^2}{\mathcal{V}^{10/3}}$$

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Compare to

$$\langle V_{LVS} \rangle \sim -\frac{\sqrt{\log \langle \mathcal{V} \rangle}}{6\sqrt{2} a^{3/2} \langle \mathcal{V} \rangle^3} |W_0|^2$$

DESY

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<u>LVS vacuum only safe</u> <u>@ very large volumes:</u>

Tree level effect
 Large numerical coeffs.

We have shown that:

Explored stability of KKLT and LVS moduli stabilisation,
 Large coeffs. & no g_s suppression,
 Safety can be achieved @ large volumes,
 Impacts on KKLT/LVS phenomenology,

