

# $H \rightarrow Z\gamma$ as a probe of the Higgs compositeness

Aleksandr Azatov

Dipartimento di Fisica, Università di Roma "La Sapienza"  
and INFN Sezione di Roma

SUSY 2013

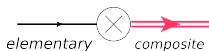
(A.A, R.Contino, A. Di Iura, J.Galloway) arXiv:1308.2676

# Composite Higgs setup

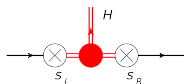
- Models where Higgs is a composite state give natural solution to the hierarchy problem
- Higgs must be lighter than the rest of the composite resonances , this can be achieved if it is a PNgB (*Georgi, Kaplan; Giudice, Grojean, Pomarol, Rattazzi*)
- EWPT  $\Delta\rho$  requires that the symmetry breaking structure should be  $SU(2)_L \times SU(2)_R / SU(2)_V$
- The minimal construction with custodial symmetry is realized in  $SO(5) \rightarrow SO(4)$  (*Contino, Agashe, Pomarol*)

# Fermions: Partial compositeness (Kaplan)

- SM fermions mix only linearly with composite fermions



- Fermion mass generation



need separate composite partner for each SM fermion

# Model assumptions

- Higgs is a PNGB ( we will consider only  $SO(5)/SO(4)$  cosets)
- SM fermion masses are generated by partial compositeness mechanism
- These models predict **separate** multiplet of the global group for every SM fermion thus we have a large multiplicity  $\sim N_F D$  of composite states at the scale of a few TeV, which strongly interact with Higgs
- Are there any indirect effects of these states on the Higgs physics?

- $h \rightarrow Z\gamma$

# Why $h \rightarrow Z\gamma$ ?

- SILH Lagrangian, parametrizes effects of new physics in terms of the higher dimensional operators, the operators relevant for the  $hgg$ ,  $h\gamma\gamma$ ,  $hZ\gamma$  interactions are

$$O_{HW} = i(D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i, \quad O_{HB} = i(D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$
$$O_g = (HH^\dagger) G_{\mu\nu} G^{\mu\nu}, \quad O_{BB} = (HH^\dagger) B_{\mu\nu} B^{\mu\nu}$$

- $O_{gg}$ ,  $O_{BB}$  are contributing to the  $hgg$ ,  $h\gamma\gamma$ ,  $hZ\gamma$ ,
- $O_{HW}$ ,  $O_{HB}$  contribute to the  $hZ\gamma$

# Higgs couplings to the gluons/photons

- $O_g = (HH^\dagger)G_{\mu\nu}G^{\mu\nu}$ ,  $O_{BB} = (HH^\dagger)B_{\mu\nu}B^{\mu\nu}$  violate the Goldstone symmetry and must be suppressed
- They must be proportional to the Goldstone Symmetry breaking parameters: SM fermions Yukawa couplings, gauge couplings
- Only composite partners of the third generation can contribute to the  $O_g, O_B$ 
  - If light fermions are composite their partners will contribute as well (Delaunay, Gorjean, Perez)

## Operators contributing to the $hZ\gamma$

$$O_{HW} = i(D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i, \quad O_{HB} = i(D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$
$$O_{BB} = (HH^\dagger) B_{\mu\nu} B^{\mu\nu}$$

- $O_{HW}$  and  $O_{HB}$  are not suppressed by the Goldstone symmetry, can get large corrections
- $hZ\gamma$  interaction is proportional  $c_{HB} - c_{HW}$ , symmetry reason?

$$O_{Z\gamma} = \frac{1}{2} c_{Z\gamma} \partial_\nu h Z_\mu \gamma_{\mu\nu}, \quad c_{Z\gamma} \propto (c_{HB} - c_{HW})$$

# Symmetry properties of $hZ\gamma$ interaction

- Composite sector must be invariant under  $SU(2)_L \times SU(2)_R$  symmetry because of the  $\Delta\rho$  constraints
- SM  $B_\mu$  couples to the  $T_R^3$  of the composite sector.
- $Z \sim B - W_3^L$ ,  $A \sim B + W_3^L \Rightarrow$  we can introduce the spurious symmetry  $P_{LR}$  under, which  $L \Leftrightarrow R$

$$Z \Leftrightarrow -Z, \quad A \Leftrightarrow A, \quad \langle H \rangle \Leftrightarrow \langle H \rangle$$

Higgs vev  $\langle H \rangle$  is invariant because it has vev along the  $(\pm 1/2, \mp 1/2)$  components,  $hZ\gamma$  interaction violates  $P_{LR}$

- SM Yukawa couplings, gauging of  $SU(2)_L$  and  $U(1)_Y$  break  $P_{LR}$ ,  $hZ\gamma$  is generated



## $hZ_\gamma$ in CCWZ language

- CCWZ construction allows to write down lagrangian for nonlinearly realized symmetry breaking  $\mathcal{G}/\mathcal{H}$
- Goldstone bosons of spontaneous symmetry breaking can be parametrized by the field

$$U(\Pi) = e^{i\Pi}, \quad \Pi = \Pi^{\hat{a}} T^{\hat{a}}$$

and by the Maurer-Cartan form

$$\begin{aligned} -iU^\dagger \partial_\mu U &= d_\mu^{\hat{a}} T^{\hat{a}} + E_\mu^a T^a \equiv d_\mu + E_\mu \\ d_\mu^{\hat{a}} &= A_\mu^{\hat{a}} + \frac{\sqrt{2}}{f} (D_\mu \pi)^{\hat{a}} + O(\pi^3) \\ E_\mu^a &= A_\mu^a - \frac{i}{f^2} (\pi \overleftrightarrow{D}_\mu \pi)^a + O(\pi^4) \end{aligned}$$

# List of operators in CCWZ

We can expand our effective lagrangian in number of derivatives since from NDA every derivative is suppressed by the power of a cut-off  $\frac{\partial_\mu}{\Lambda}$

- $O(p^2)$ -  $O_1 = f^2 \text{Tr}(d_\mu d^\mu) \Leftrightarrow W_\mu W^\mu \sin^2(\frac{h}{f})$
- $O(p^4)$  lagrangian (*Rattazzi, Contino, Pappadopulo, Marzocca*)

$$O_3^\pm = \text{Tr}(E_{\mu\nu}^L E_{\mu\nu}^L) \pm \text{Tr}(E_{\mu\nu}^R E_{\mu\nu}^R),$$

$$O_4^\pm = \text{Tr}(E_{\mu\nu}^L \pm E_{\mu\nu}^R) i[d_\mu, d_\nu], \quad O_4^- \rightarrow \partial_\nu h Z_\mu \gamma_{\mu\nu} \text{ interaction}$$

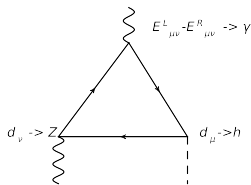
$$\mathcal{O}(d^4) \Leftrightarrow \text{dim } 8 \text{ operators}$$

- $P_{LR}$  properties

$$E_{L,R} \rightarrow P_{LR} E_{R,L} P_{LR}, \quad P_{LR} = \text{Diag}(-1, -1, -1, 1, 1)$$

$$d \rightarrow P_{LR} d P_{LR}$$

- $O_4^- = i\text{Tr}(E_{\mu\nu}^L - E_{\mu\nu}^R)[d_\mu, d_\nu]$
- Higgs comes from the covariant derivative,  $\partial_\mu h$  so this coupling will have no Goldstone suppression
- No elementary composite mixing is needed! Partners of the light fermions are important.
- Composite sector must violate  $P_{LR}$  in order to generate  $O_4^-$
- from NDA  $hZ\gamma$  is log divergent?

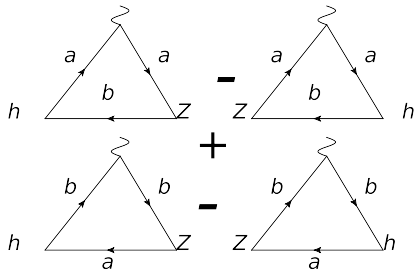


# Derivative couplings/absence of log divergence

It is useful to look at the  $U(1)_V$  subgroup of  $SO(4)$

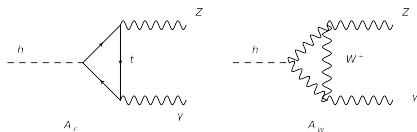
$$\mathcal{L}_{Z\gamma} = \sum_{a,b} \left[ \frac{\partial_\mu h}{f} \lambda_{ab}^h \bar{\psi}_a \gamma^\mu \psi_b + \lambda_{ab}^Z Z_\mu \bar{\psi}_a \gamma^\mu \psi_b + q_\psi \delta_{ab} A_\mu \bar{\psi}_a \gamma^\mu \psi_b \right]$$

- Loop function is antisymmetric in  $\mu, \nu$  (higgs and Z indices)  $\Rightarrow$   
Amplitude  
 $\sim \text{Tr}(\lambda^h \lambda^Z) - \text{Tr}(\lambda^Z \lambda^h) = 0$
- we need at least one mass insertion  $\Rightarrow$   
no log divergence



# $Z\gamma$ coupling in the SM

- This decay is generated by the loops of  $W^\pm$  and  $t$

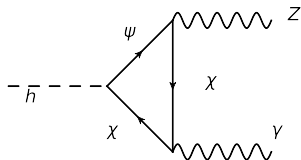


- $\Gamma(h \rightarrow Z\gamma) = \frac{1}{32\pi} |A|^2 m_h^2 \left(1 - \frac{m_Z^2}{m_h^2}\right)^3 A = \frac{\alpha g}{4\pi m_W} (A_F + A_W)$ .  
The SM loop is dominated by the contribution of  $W$ ,  $A_W/A_F \sim -18$
- top contribution is suppressed because top coupling to  $Z$  is small  
 $T_Z \sim T_L^3 - 2q_t \sin^2 \theta \sim 0.2$ , so new fermions can be very important

# $hZ\gamma$ vs $h\gamma\gamma$

What is the difference between  $h\gamma\gamma$  and  $hZ\gamma$  loops?

- Not all the fermions have the same couplings to  $Z$
- $Z$  can couple to two different mass eigenstates, so in the loop we can have two different fermions



## Model with 5

- under  $SU(2)_L \times SU(2)_R$ :  $\mathbf{5} = (2, 2) + 1$ , the breaking of the  $SO(5)$  does not break  $P_{LR} \Rightarrow$  no  $hZ\gamma$  in the absence of the elementary composite mixing
- top Yukawa coupling breaks down  $P_{LR}$  so these effects will be suppressed by  $O\left(\frac{\lambda^2 v^2}{M_*^2 f^2}\right)$ , however in the SM top contribution is much smaller than the  $W$  contribution.

$$A_{SM} \sim A_W \sim 20A_{top}$$

corrections from  $t'$  in the loops will be of the order of  $\lesssim 0.05 \frac{v^2}{f^2}$

- modification is dominated by the trigonometric rescaling of the  $W$  coupling,  $A_5 \approx A_{SM} \sqrt{1 - v^2/f^2}$

# Model with 10

- under  $SU(2)_L \times SU(2)_R$ :  $10 = (2, 2) + (3, 1) + (1, 3)$
- Different masses and interactions of  $(3, 1)$  and  $(1, 3)$  respect  $SU(2)_L \times SU(2)_R$  but break  $P_{LR}$
- Ignore elementary composite mixing

$$\mathcal{L} = m_4 \bar{4}4 + m_{(3,1)} (3, 1)^* (3, 1) + m_{(1,3)} (1, 3)^* (1, 3) \\ + \bar{10} (\not{\partial} - \not{E}) 10 - \zeta_{13} \bar{4} \not{d} (1, 3) - \zeta_{31} \bar{4} \not{d} (3, 1).$$



# Model with 10

- At one loop  $O_{Z\gamma}$  is generated with the coefficient

$$C_{Z\gamma} \sim \frac{g^2}{4} \sin^2 \theta \left[ |\zeta_{13}|^2 (C(m_4, m_{(1,3)}) - C(m_{(1,3)}, m_4)) - |\zeta_{31}|^2 (C(m_4, m_{(3,1)}) - C(m_{(3,1)}, m_4)) \right]$$

- If we look at the ratio of the new physics effects to the contribution of the SM top in the limit  $\Delta m \ll m$  we will get

$$\frac{\text{NP}}{\text{SM top}} \Big|_{\Delta m \ll m} \sim 15 N_{\text{gener}} \times \left(\frac{v}{f}\right)^2 \frac{\Delta m}{m}$$

## $P_{LR}$ vs $Z\bar{b}b$ constraints

- Large modification to the  $hZ\gamma$  requires  $P_{LR}$  breaking in the composite sector.
- In order to reproduce the top mass, electroweak doublet  $q_L = (t_L, b_L)$  must mix strongly with the composite sector.  $Z\bar{b}b$  constraints require  $b_L$  to mix strongly only with the operator which respects  $P_{LR}$  (Agashe, Contino, Pomarol, DaRold) in MCHM5 ( $b_L - B(1/2, 1/2)$ )
- Model with **5** has an accidental  $P_{LR}$  (Contino, Rattazzi, Pappadopulo, Marzocca) symmetry due to the fact that

$$\mathbf{5} = \mathbf{1} + (\mathbf{2}, \mathbf{2})$$

$SO(5)/SO(4)$  breaking cannot split masses inside  $(\mathbf{2}, \mathbf{2})$

# Constructing realistic model with $P_{LR}$ breaking

- $q_L = (t, b)_L$  must mix with **5** in order to be protected from  $Z\bar{b}b$
- Take MCHM5 but mix  $b_R$  with **10** instead of **5**

## Minimal $P_{LR}$ model 10 + 5

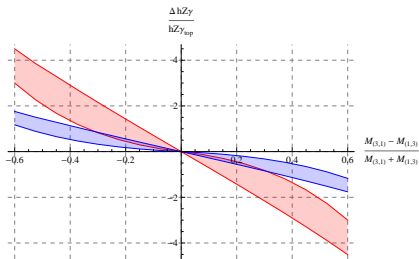
$q_L - \frac{\lambda_q^{10}}{10} - 10 - 10 - \frac{\lambda_b}{10} - b_R \Rightarrow m_b \sim \lambda_q^{10} \lambda_b$	$\lambda_q^{10} \ll \lambda_q^5, Z\bar{b}b$ is
$q_L - \frac{\lambda_q^5}{5} - 5 - 5 - \frac{\lambda_t}{5} - t_R \Rightarrow m_t \sim \lambda_q^5 \lambda_t$	

fine

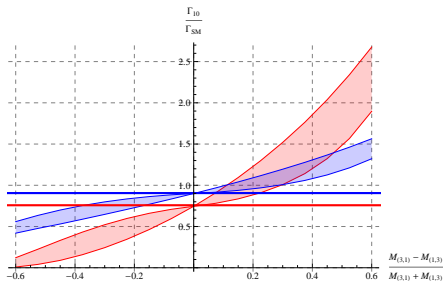
$$\mathcal{L}_{\text{mixing}} = \lambda_q^{10} \bar{q}_L P_q 10 + \lambda_q^5 \bar{q}_L P_q 5 + \lambda_b \bar{b}_R P_b 10 + \lambda_t \bar{t}_R P_t 5$$

Forbid mixing between 10 and 5 imposing different  $U(1)_X$  charges

# Model with 10, numerical calculation



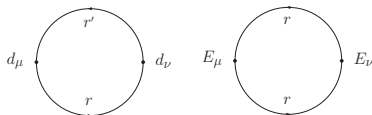
**Figure:** ratio of the  $A_{NP}/A_{top}$  for the model with 10 for one generation, red  $f = 500$ , blue  $f = 800$  GeV



**Figure:** ratio of the  $\Gamma_{NP}/\Gamma_{SM}$  in the model with 10 with three generations

# Contribution to the S parameter (talk by Contino)

- Corrections to the S parameter will be generated by the loop of the composite particles, no elementary composite mixing is necessary (Golden,Randall;Barbieri,Isidori,Pappadopulo; Grojean, Matsedonskyi,Panico;AA,Contino,Dilura,Galloway )



$$\mathcal{L} = \sum_r \bar{\chi}_r (i\nabla - m_r) \chi_r - \zeta_{rr'} \chi_r \not{d} \chi_{r'}$$

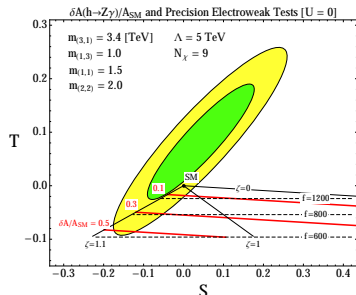
$$\Delta S = -\frac{8\pi}{gg'} \left( -\Pi'_{33} \sin^2 \theta + \frac{1}{2} \Pi'_{3L3L} \sin^2 \theta + \frac{1}{2} \Pi'_{3R3R} \sin^2 \theta \right)$$

$$\Delta S \simeq \frac{N_\chi \sin^2 \theta}{3\pi} (1 - |\zeta|^2) \log \frac{\Lambda^2}{m^2} + \text{finite}$$

- $\Delta S$  is finite when  $\zeta = 1$ , because in this limit we can remove derivative Higgs interactions by the fermion field redefinition.

# Contribution to the S parameter

- S parameter is given by the operator  $O_3^+ = Tr(E_{\mu\nu}^L E_{\mu\nu}^L) + Tr(E_{\mu\nu}^R E_{\mu\nu}^R)$ , no  $P_{LR}$  violation is required, generically  $O_4^-$  and  $O_3^+$  are independent
- However assuming no cancellations between different contributions we can look at the correlation between  $\Delta S$  and  $\delta A(h \rightarrow Z\gamma)$
- The fermion contribution to the S parameter can be of both signs, and the negative sign contribution can relax the current constraints from EWPT.



# Outlook

- We studied  $hZ\gamma$  in the Composite Higgs models
- $h \rightarrow Z\gamma$  decay receives large new physics corrections that are not suppressed by the Goldstone symmetry arguments.
- Contribution of the strong dynamics to the  $h \rightarrow Z\gamma$  is controlled by the  $P_{LR}$  breaking. If the modification of the  $Z\bar{b}b$  coupling is isolated from the  $P_{LR}$  breaking, viable model can be constructed with  $O(1)$  modification of the  $h \rightarrow Z\gamma$  decay.
- Similar processes lead to the contribution to the  $S$  parameter. Negative  $\Delta S$  can relax the current EWPT bounds and at the same time accommodate large  $h \rightarrow Z\gamma$

## $hZ\gamma$ from integrating out $\rho$

- minimal CCWZ lagrangian for the vector  $\rho$  with an additional operator  $Q_1$

$$\mathcal{L} = -\frac{1}{4g_{\rho L}}{}^2 \text{Tr}(\rho_{\mu\nu}^L \rho^{L,\mu\nu}) + \frac{m_{\rho L}^2}{2g_{\rho L}^2} \text{Tr}(\rho_\mu^L - E_\mu^L)^2 \\ + \alpha_1^L \text{Tr}(\rho_L^{\mu\nu} i[d_\mu, d_\nu]) + (L \Leftrightarrow R)$$

- Integrating out  $\rho$  at tree level we will get

$$c_{Z\gamma} = \frac{g^2}{2} \sin^2 \theta (\alpha_1^L - \alpha_1^R)$$



